

INTERCOMPARISON OF NUMERICAL SIMULATION CODES FOR GEOLOGIC DISPOSAL OF CO₂

*Karsten Pruess¹, Julio García¹, Tony Kavscek², Curt Oldenburg¹,
Jonny Rutqvist¹, Carl Steefel³, Tianfu Xu¹*

¹ Lawrence Berkeley National Laboratory (LBNL), Berkeley, CA 94720, U.S.A.

² Stanford University, Stanford, CA 94305, U.S.A.

³ Lawrence Livermore National Laboratory (LLNL), Livermore, CA 94550, U.S.A.

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ABSTRACT

Numerical simulation codes were exercised on a suite of eight test problems that address CO₂ disposal into geologic storage reservoirs, including depleted oil and gas reservoirs, and brine aquifers. Processes investigated include single- and multi-phase flow, gas diffusion, partitioning of CO₂ into aqueous and oil phases, chemical interactions of CO₂ with aqueous fluids and rock minerals, and mechanical changes due to changes in fluid pressures. Representation of fluid properties was also examined. In most cases results obtained from different simulation codes were in satisfactory agreement, providing confidence in the ability of current numerical simulation approaches to handle the physical and chemical processes that would be induced by CO₂ disposal in geologic reservoirs. Some discrepancies were also identified and can be traced to differences in fluid property correlations, and space and time discretization.

EXECUTIVE SUMMARY

Mathematical models and numerical simulation codes are playing an important role in evaluating the feasibility of geologic disposal of greenhouse gases, and they will be necessary tools for designing and operating future disposal systems. In order to serve these functions, simulation codes must be tested to demonstrate that they can adequately represent the physical and chemical processes that would be induced by injection of CO₂ and other gases into geologic formations.

The present code intercomparison study aimed at such testing and demonstration. The study was initiated and designed by LBNL in the framework of the GeoSeq project. The overall approach was as follows. In a first step, we designed a number of test problems that would probe major issues relating to geologic disposal of greenhouse gases. Actual field applications will involve three-dimensional flows in media with multi-scale hydrologic and chemical heterogeneity, and coupled processes involving fluid dynamics, chemical reactions, mechanical deformation, and thermal effects. It was considered that establishing confidence in the capabilities of numerical simulators would be an iterative process, proceeding from simple to complex. Accordingly, the test problems posed for the present study were intentionally designed to be simplified prototypes of actual field problems.

The main issues addressed in this work are as follows. Do we understand the fundamental physical and chemical processes that would play a role in geologic disposal of greenhouse gases? Do we have valid mathematical models for them? Can currently available numerical simulators obtain reliable and accurate numerical solutions for conditions and parameters of practical interest?

As to the actual execution of the study, the initiators decided that worldwide participation would be sought, and that participants would work with their own funding and using codes available to them. It was hoped that the study would provide a win-win opportunity where all participants could benefit by testing and comparing their codes, learn from one another, and identify areas where additional research and improvements in simulation capabilities would be needed. The initiators of the study could not offer funding support to prospective participants, but were hoping that the potential benefits to be obtained from participation would be sufficient inducement to attract a sizable number of participants.

The approach outlined above was implemented and proved successful. The intercomparison study was started by sending a solicitation to participate to approximately 150 organizations worldwide. Additional solicitation was made at technical conferences, such as the First National Conference on

Carbon Sequestration which was held in May 2001 in Washington, DC. At that meeting we also presented an overview of the proposed study in hopes of attracting additional participants. A set of eight proposed test problems were posted on the Internet (<http://www-esd.lbl.gov/GEOSEQ/>). Our efforts resulted in participation of ten research groups from six countries. Communication among participants was done by e-mail and through a workshop that was held in Berkeley in October 2001. The workshop provided a forum for clarifying some of the technical issues in the test problems, presenting and intercomparing first preliminary results, and arriving at a consensus for detailed specifications of the results that were to be submitted.

The proposers of the individual test problems served as coordinators, who handled the collection of results and communication with submitting organizations. The problem coordinators then produced writeups with presentation and intercomparison of results for their respective test problems, which were collated and merged by LBNL into the present final report of the project.

The eight problems posed in the study address processes that would be induced by CO₂ injection into depleted gas reservoirs, saline formations, and oil reservoirs. Before we give brief problem-by-problem summaries of the individual test problems, we first attempt a brief overall summary of outcomes and lessons learned. Important observations are:

1. A considerable number of numerical simulation codes is capable of simulating, in realistic, quantitative detail, the important flow and transport processes that would accompany geologic sequestration.
2. Agreement between results from different groups and different codes ranges from fair to good.
3. All codes attempt to represent fluid properties and thermodynamic data in a realistic fashion, but there are some considerable disagreements between fluid parameters in different codes.
4. Agreement between simulations of fluid flow and transport, and hydromechanical and geochemical effects, ranged from fair to good. Where discrepancies persisted they were usually traced to differences in fluid property descriptions.

5. The hydro-mechanical test problem was solved by only one code. The interplay of hydrology and geomechanics plays an important role in the integrity of potential geologic disposal sites, and capabilities for modeling such processes need to be strengthened.
6. Code developers should also aim for a more accurate description of fluid properties, including PVT data, as well as transport and caloric properties, using up-to-date experimental data.
7. Although further improvements in fluid property descriptions are important, it is recognized that in actual practice it would be uncertainties in the conceptual model at a given site that would most strongly affect simulation results.
8. The problems investigated here were simplified prototypes of field problems. Further modeling studies should be undertaken on problems that approach the full realism and complexity of actual field problems, to more fully establish the usefulness and credibility of numerical simulation codes for geologic sequestration.

Problems 1 and 2 examined interdiffusion and mixing of CO₂ and CH₄, as affected by highly non-linear fluid property dependencies on temperature, pressure, and composition. Results were submitted by four groups, using four different simulation codes. Agreement for fluid property estimations ranged from fair to good. Agreement between flow simulations ranged from fair to good also, which is attributed to considerable disagreement in some fluid parameters. Code developers should aim for a more accurate description of fluid properties, including PVT data, as well as transport and caloric properties.

Problems 3 and 4 involve introduction of CO₂ into a single-phase saline formation. Both problems probe similar aspects of thermodynamic and transport properties of brine-CO₂ mixtures, including mutual solubility of brine and CO₂. While fluid properties used in different codes are generally in good agreement, within a few percentage points, there are also occasional disagreements in excess of 50 %. Problem 3 studies CO₂ injection into a saline formation from a vertical well in one-dimensional radial flow geometry. This represents the basic prototype of a CO₂ disposal problem. Predictions from different codes for fluid pressures and advancement of the CO₂ injection front generally show satisfactory agreement, with existing differences largely attributable to fluid property data.

Problem 4 represents a prototype of the basic leakage problem. The problem simulates the extremely non-linear processes whereby CO₂ lost from storage would be migrating up a fault zone. A similar evaluation as for Problem 3 applies, i.e., agreement between different codes is generally satisfactory.

Problem 5 examines chemical interactions between rock minerals and an aqueous phase with high CO₂ partial pressure. There was satisfactory agreement between three different codes in the predictions of mineral dissolution and precipitation, and aqueous phase chemistry.

The hydromechanical Problem 6 was solved by only one group, in spite of considerable efforts on the part of the organizers to attract additional solutions. Few existing codes seem capable of simulating these practically very important processes.

Problem 7 was the most complex of the flow problems, representing a simplified model of the Sleipner Vest CO₂ injection site in the Norwegian sector of the North Sea. The problem involves CO₂ injection into a 2-D model of alternating sand-shale layers. Predictions for shape and growth of the CO₂ injection plume showed good agreement between different codes.

Problem 8 addressed CO₂ injection into a multi-component oil reservoir. The flow geometry is very simple, a single 1-D tube, but very complex fluid phase behavior must be accurately represented. Agreements between four participating groups and “exact” results obtained from a semi-analytical solution is from fair to good. In this problem, there is a strong interaction between fluid phase behavior and effects from finite space discretization. Accurate solution requires very fine discretization that may not be practical for 3-D field problems.

Overall it can be stated that numerical simulation capabilities are available now that can describe the complex non-linear processes that would be induced by CO₂ injection into various types of potential disposal reservoirs. In general agreement between different simulators was satisfactory. In the process of the study a number of bugs were identified and remedied in different codes. There is considerable scatter in the representation of fluid properties, such as densities, viscosities, and partitioning of components among phases. This is an area that needs more work and close interplay with experimental data.

Future development and demonstration of simulation codes should be directed towards a more comprehensive description of processes in more realistic settings. It will also be necessary to go beyond "paper problems," and to conduct field tests of proposed disposal schemes. Carefully

controlled and monitored field experiments integrated with modeling are required on a range of space and time scales, to build a bridge towards practical disposal systems that would generate very large subsurface plumes of CO₂.

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1. Introduction

Geologic sequestration of CO₂ can be accomplished by separating CO₂ from flue gases and subsequently injecting it into a variety of storage reservoirs, including brine aquifers, producing or depleted oil and gas reservoirs, and coalbeds. Injection of greenhouse gases into such formations will give rise to complex coupled processes of fluid flow, mechanical and chemical changes, and heat transfer. Mathematical models and numerical simulation tools will play an important role in evaluating the feasibility of CO₂ storage in subsurface reservoirs, in designing and analyzing field tests, and in designing and operating geologic CO₂ disposal systems. In order to establish credibility for numerical simulators as practical engineering tools, it is necessary to demonstrate that they can model accurately and reliably the important physical and chemical processes that are induced by injection of CO₂ into potential disposal reservoirs. This can be accomplished by running simulators on a series of test problems that engage the processes, fluid properties, and geologic features of interest. Code intercomparison studies have been successfully used as a means for establishing confidence in simulation tools in related technical fields such as petroleum engineering (Firoozabadi and Thomas, 1989) and geothermal reservoir engineering (Stanford, 1980), and in nuclear waste management (Larsson, 1992; Chapman et al., 1994; Jing et al., 1995; Stephansson et al., 1996).

Depending on the storage reservoir of interest and the composition of the waste gas stream (pure CO₂ vs. mixtures of CO₂ with other gases), injection of CO₂ in geologic formations may give rise to a number of physical and chemical phenomena, such as miscible or immiscible displacement of native fluids, dissolution of injected fluids into reservoir fluids, changes in effective stress with associated porosity and permeability change and the possibility of inducing seismic activity, chemical interactions between fluids and solids, and nonisothermal effects. Key issues arising in process simulation include (1) thermodynamics of sub- and supercritical CO₂, and PVT properties of mixtures of CO₂ with other fluids, including (saline) water, oil, and natural gas; (2) fluid mechanics of single and multi-phase flow when CO₂ is injected into aquifers, oil reservoirs, and natural gas reservoirs; (3) coupled hydro-chemical effects due to interactions between CO₂, reservoir fluids, and primary mineral assemblages; and (4) coupled hydro-mechanical effects, such as porosity and permeability change due to increased fluid pressures from CO₂ injection. Additional topics that need to be addressed include space and time discretization and their impacts on the solution of the underlying mathematical model, and the dependence of processes and parameters on space and time scale.

We report here on the results of a code intercomparison study whose purpose was to evaluate key processes in CO₂ geologic disposal and to test the capabilities of numerical simulators

to model these processes. The present study was initiated and coordinated by Lawrence Berkeley National Laboratory (Pruess et al., 2000, 2001). It was decided to include only brine formation, oil, and gas reservoir problems, for which well-developed simulation capabilities are available. Coalbed methane simulators are the subject of a separate study (Law et al., 2002). A set of eight simulation problems was adopted. The issues addressed by these problems are summarized in Table 1.1. Detailed problem specifications are given in the appendix; they include formation properties, initial and boundary conditions, and sinks and sources. (The appendices are reproduced essentially unchanged from the original report, Pruess et al., 2000, except that some typographical errors were corrected and references updated.) No prescriptions were given for fluid properties to be used, nor were there any specifications of space discretization (gridding) and time stepping. The choice of

Table 1.1 Issues addressed by the different test problems

property/process storage reservoir	PVT data	fluid flow	transport (diffusion, dispersion)	chemical reactions	mechanical couplings
brine aquifer	3, 4, 7	3, 4, 6, 7		5	6
oil	8	8	8		
gas	1, 2	1, 2	1, 2		
coalbed					

these parameters was left to the participants, and was to be evaluated as part of the intercomparison of simulation results. The test problems studied and reported here should be considered an initial set specifically designed to address basic processes in different potential disposal reservoirs. Accordingly, problem specifications were kept relatively simple. Most problems are for 1-D homogeneous media, although a heterogeneous 2-D problem was included also. Problems with more complex and realistic features, such as 3-D heterogeneous flows systems, will be addressed in future studies.

Participation in the code intercomparison study was solicited through mailings, personal contacts, and the Internet (<http://www-esd.lbl.gov/GEOSEQ/code/index.html>). All participants worked with their own funding, and used codes available to them. Participants were free to choose any subset of problems they wanted to tackle. Reporting requirements had been included as part of the original problem specifications (see appendix), and were further refined during a two-day workshop that was held at the Lawrence Berkeley National Laboratory in October, 2001. The proposers of each of the test problems served as coordinators and communicated with the various participating groups in obtaining and collating results.

Results were submitted by ten groups from six countries, as follows.

- Lawrence Berkeley National Laboratory (LBNL), U.S.A., using the TOUGH2/ECO2, TOUGHREACT and TOUGH-FLAC codes;
- University of Stuttgart, Germany, using the MUFTE_UG code;
- CSIRO Petroleum, Australia, using an in-house version of TOUGH2/ECO2;
- Institut Français du Pétrole (IFP), France, using the SIMUSCOPP code;
- Stanford University, U.S.A., using an unnamed research code;
- Alberta Research Council (ARC), Canada, using the GEM code of the Computer Modeling Group (CMG) of Calgary, Alberta;
- Los Alamos National Laboratory (LANL), U.S.A., using the FLOTRAN and ECLIPSE 300 codes;
- Lawrence Livermore National Laboratory (LLNL), U.S.A., using the NUFT code;
- Industrial Research Limited (IRL), New Zealand, using an in-house version of TOUGH2 and the CHEM-TOUGH code;
- Pacific Northwest National Laboratory (PNNL), U.S.A., using the STOMP code.

We now proceed through a problem-by-problem presentation and discussion of results, that had previously only been summarized in abbreviated form (Pruess et al., 2002). In the presentation we include those data that most clearly highlight areas of agreement as well as disagreement between different codes. A separate report is available with a more detailed presentation of the results obtained by LBNL for the saline aquifer flow problems (#3, 4, and 7; Pruess and García, 2002b). A stand-alone report on the gas reservoir problems is presented in Oldenburg et al. (2002).

2. CO₂ Disposal in Depleted Gas Reservoirs¹

The main processes of interest for CO₂ storage in gas reservoirs are advection of a gas phase consisting of CO₂ and CH₄, interdiffusion of these two components, and gas dissolution in residual liquid. This section presents two gas flow problems that examine the interplay of these processes, accompanied by strong real gas effects during mixing.

Four numerical simulation codes have been used for physical property estimation and the test problems. These are as follows: CHEMTOUGH, developed by Industrial Research Limited, New Zealand, a geochemical modeling extension of TOUGH2 (Pruess et al., 1999); GEM, a reservoir simulator developed by Computer Modelling Group (CMG), Canada; SIMUSCOPP, a reservoir simulator developed by Institut Français du Pétrole (IFP), France; and TOUGH2/EOS7C, a special gas module for the TOUGH2 reservoir simulator (Pruess et al., 1999) developed by Lawrence Berkeley National Laboratory (LBNL), USA. Each of these codes uses its own methods for calculating physical properties of gas mixtures. Only CHEMTOUGH and TOUGH2/EOS7C share a common heritage and thus calculate flow and transport by the same methods.

2.1 Problem Description

The results of reservoir simulation are strongly dependent on the real gas properties of the gas mixtures. The first part of this study involved comparison of densities, viscosities, and solubilities from different simulators for the pure end-member gases (CO₂ and CH₄) and 50% mole fraction mixtures. Two test problems were defined that engage key processes involved in CO₂-CH₄ mixing (Figure 2.1). Problem 1 considers the mixing by molecular diffusion and advection of a stably stratified one-dimensional column 100 m in height with the light gas (CH₄) on the top and the heavy gas (CO₂) on the bottom. Mixing around the interface is mostly by molecular diffusion, although nonzero permeability allows minor advection to occur as gas pressures increase upon mixing at the interface. Problem 2 considers the mixing by advection and diffusion of gases initially side by side in a vertical 100 m x 100 m reservoir. Gravity effects cause the dense CO₂ gas to flow downward while the lighter CH₄ migrates upward.

2.2 Comparison of Physical Property Estimates

To the extent that physical properties strongly affect flow and transport, the first comparison we present is for density (ρ), viscosity (μ), and solubility of CO₂ and CH₄ gas mixtures. Carbon dioxide undergoes large changes in density and viscosity as it passes through the critical region. The critical pressure and temperature of CO₂ (73.8 bars, 31.0 °C) will be reached in the subsurface

¹ proposed by Curt Oldenburg; e-mail: CMOldenburg@lbl.gov

at depths greater than approximately 800 m. Thus CO₂ will most commonly be supercritical in the subsurface. Therefore, we present estimates of physical properties at both subcritical (40 bars) and supercritical (100 bars) conditions. For brevity, we present in Tables 2.1 and 2.2 physical properties only for the end members and 50-50 mixtures. We have included reference values either from published data or from more detailed estimation methods as noted.

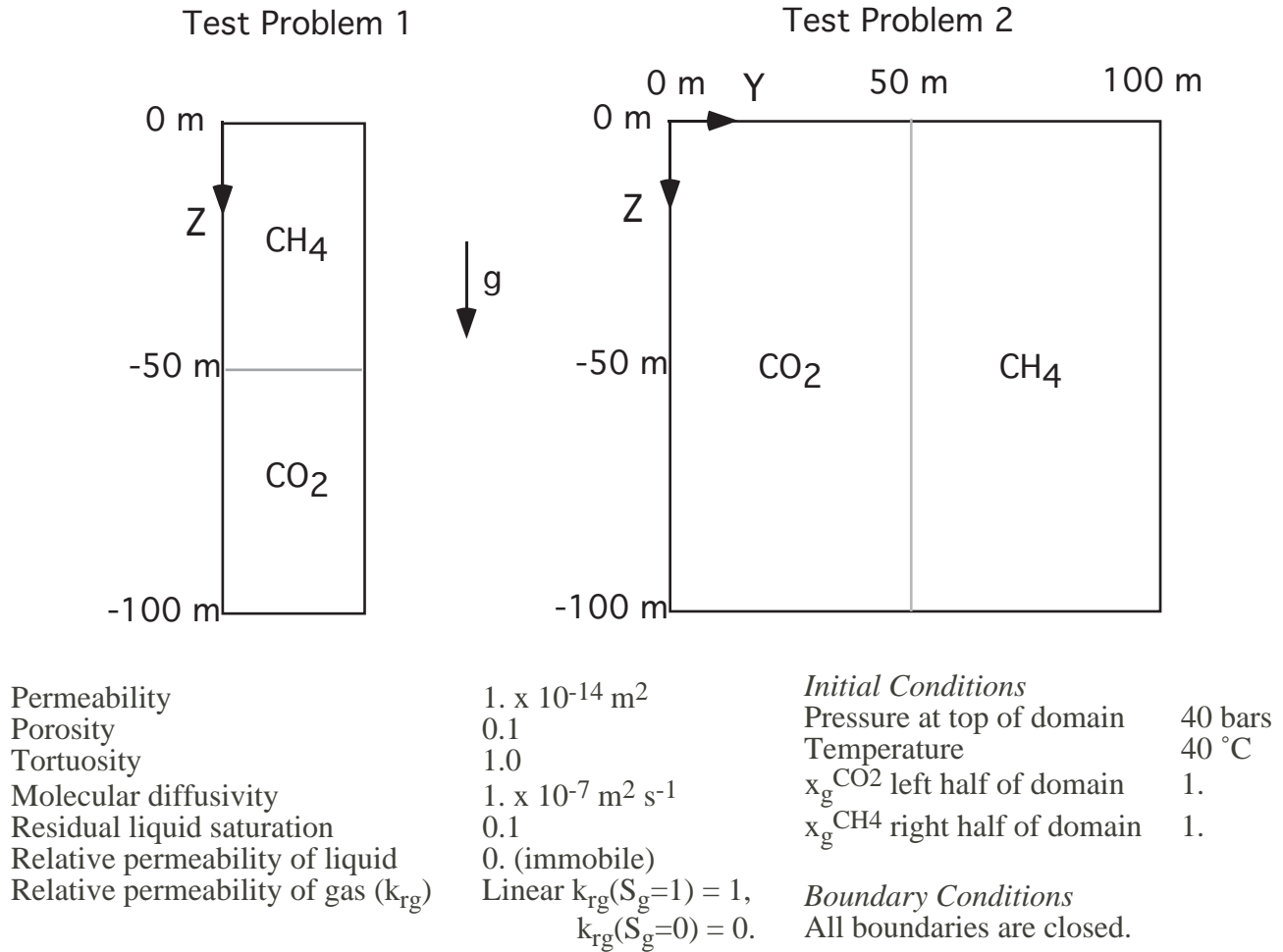


Figure 2.1 Schematic of test problems 1 and 2.

2.3 Results for Problem 1. Mixing of Stably Stratified Gases

In this problem, CO₂ and CH₄ gases are placed in contact one on top of the other and allowed to mix as controlled by diffusion and associated flow at 40 bars, 40 °C. Mixing in the one-dimensional system is limited because the denser gas (CO₂) is on the bottom and the lighter gas (CH₄) is on the top. The domain, properties, boundary and initial conditions are shown in Figure 2.1. All of the boundaries are closed and the problem is considered isothermal. Although the

problem is dominated by diffusion, small advective fluxes arise as diffusive mixing around the interface leads to density changes that affect gas pressure.

The results of Problem 1 are shown in Figure 2.2a by the gas mole fraction of CO₂ ($x_g^{CO_2}$), where $x_g^{CH_4} = 1 - x_g^{CO_2}$ in this binary system. As shown in Figure 2.2a, the fundamental process of binary diffusive mixing is captured by all of the codes, with slight differences in diffusion rate. Note in Figure 2.2b that the pressure in the system increases, a result of the mixing between CO₂ and CH₄. In direct relation to the overestimate of pure CO₂ density and the underestimate of gas mixture density by CHEMTOUGH (see Table 2.1), this code predicts larger pressure increases than any of the other codes. Variations in the results are likely due mostly to differences in physical property estimates rather than to differences in modeling of the physical process of molecular diffusion and advection.

Table 2.1 Properties of CO₂-CH₄ gas mixtures and aqueous solubility at 40 bars, 40 °C.

Simulation Code	gas phase				aqueous phase	
	$x_g^{CH_4}$	$x_g^{CO_2}$	ρ (kg m ⁻³)	μ (Pa s)	$x_l^{CH_4}$	$x_l^{CO_2}$
CHEMTOUGH	0.	1.	105.39	1.49×10^{-5}	0.	1.64×10^{-2}
GEM	0.	1.	85.41	1.75×10^{-5}	0.	1.50×10^{-2}
SIMUSCOPP	0.	1.	85.35	1.02×10^{-5}	0.	1.24×10^{-2}
TOUGH2/EOS7C	0.	1.	85.45	1.70×10^{-5}	0.	1.62×10^{-2}
Reference Values	0.	1.	83.79 (a)	1.73×10^{-5} (a)	0.	1.37×10^{-2} (b)
CHEMTOUGH	0.5	0.5	46.88	1.34×10^{-5}	4.08×10^{-4}	7.45×10^{-3}
GEM	0.5	0.5	52.26	1.53×10^{-5}	3.82×10^{-4}	7.64×10^{-3}
SIMUSCOPP	0.5	0.5	52.29	1.11×10^{-5}	3.90×10^{-4}	6.20×10^{-3}
TOUGH2/EOS7C	0.5	0.5	51.97	1.44×10^{-5}	3.73×10^{-4}	8.07×10^{-3}
Reference Values	0.5	0.5	51.33 (a)	1.67×10^{-5} (a)	3.66×10^{-4} (c, d, e, f)	6.74×10^{-3} (c, d, e, f)
CHEMTOUGH	1.	0.	24.58	1.16×10^{-5}	7.49×10^{-4}	0.
GEM	1.	0.	26.48	1.22×10^{-5}	7.51×10^{-4}	0.
SIMUSCOPP	1.	0.	26.46	1.26×10^{-5}	7.81×10^{-4}	0.
TOUGH2/EOS7C	1.	0.	26.42	1.21×10^{-5}	7.43×10^{-4}	0.
Reference Values	1.	0.	26.10 (a)	1.23×10^{-5} (a)	7.22×10^{-4} (c, d, e, f)	0.

(a) NIST, 1992.

(d) Johnson et al., 1992.

(b) Wiebe and Gaddy, 1940.

(e) Shock et al., 1989.

(c) Spycher and Reed, 1988.

(f) Wagman et al., 1982.

Table 2.2 Properties of CO₂-CH₄ gas mixtures and aqueous solubility at 100 bars, 40 °C.

Simulation Code	gas phase				aqueous phase	
	$x_g^{CH_4}$	$x_g^{CO_2}$	ρ (kg m ⁻³)	μ (Pa s)	$x_l^{CH_4}$	$x_l^{CO_2}$
CHEMTOUGH	0.	1.	432.33	2.88×10^{-5}	0.	4.09×10^{-2}
GEM	0.	1.	564.82	4.35×10^{-5}	0.	2.39×10^{-2}
SIMUSCOPP	0.	1.	561.44	3.59×10^{-5}	0.	2.30×10^{-2}
TOUGH2/EOS7C	0.	1.	566.00	4.35×10^{-5}	0.	4.03×10^{-2}
Reference Values	0.	1.	631.90 (a)	5.04×10^{-5} (a)	0.	2.19×10^{-2} (b)
CHEMTOUGH	0.5	0.5	130.58	1.41×10^{-5}	1.14×10^{-3}	1.61×10^{-2}
GEM	0.5	0.5	158.10	1.88×10^{-5}	8.27×10^{-4}	1.33×10^{-2}
SIMUSCOPP	0.5	0.5	158.44	1.46×10^{-5}	9.08×10^{-4}	1.15×10^{-2}
TOUGH2/EOS7C	0.5	0.5	155.16	1.81×10^{-5}	9.43×10^{-4}	2.00×10^{-2}
Reference Values	0.5	0.5	153.97 (a)	1.94×10^{-5} (a)	7.95×10^{-4} (c, d, e, f)	1.21×10^{-2} (c, d, e, f)
CHEMTOUGH	1.	0.	61.45	1.16×10^{-5}	1.87×10^{-3}	0.
GEM	1.	0.	71.78	1.39×10^{-5}	1.58×10^{-3}	0.
SIMUSCOPP	1.	0.	71.66	1.43×10^{-5}	1.82×10^{-3}	0.
TOUGH2/EOS7C	1.	0.	71.57	1.41×10^{-5}	1.86×10^{-3}	0.
Reference Values	1.	0.	70.03 (a)	1.41×10^{-5} (a)	1.54×10^{-3} (c, d, e, f)	0.

(a) NIST, 1992.

(b) Wiebe and Gaddy, 1940.

(c) Spycher and Reed, 1988.

(d) Johnson et al., 1992.

(e) Shock et al., 1989.

(f) Wagman et al., 1982.

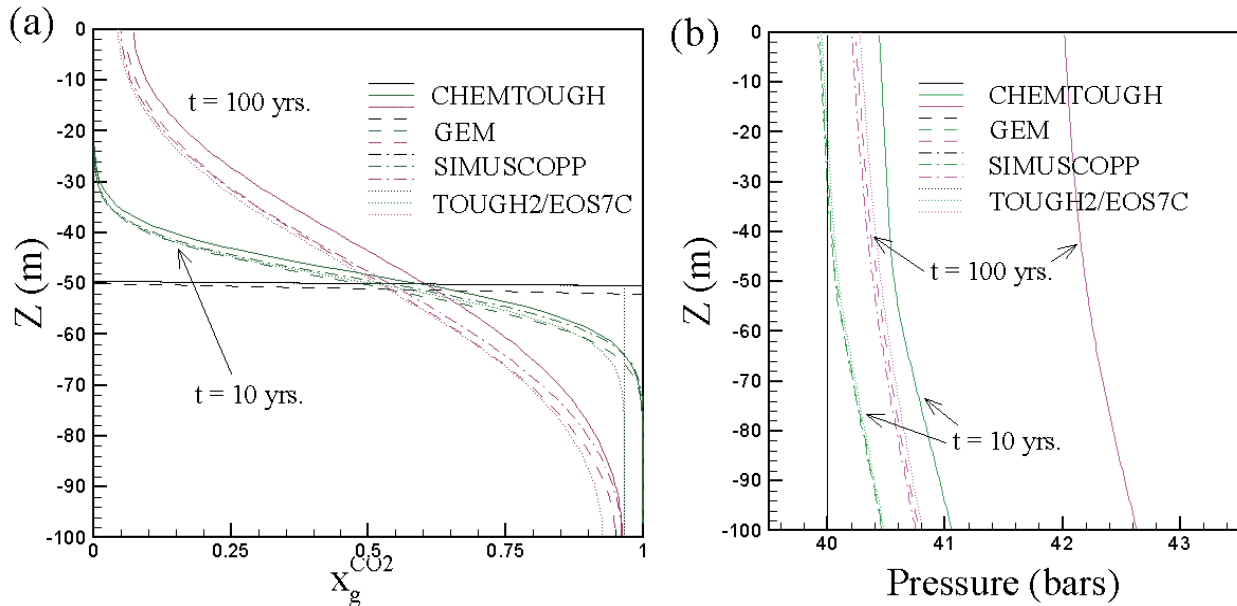


Figure 2.2 Mole fraction of CO₂ in gas (a) and pressure (b) as a function of elevation Z for problem 1 at t = 0, 10, and 100 yrs.

2.4 Results for Problem 2. Advective-Diffusive Mixing due to Lateral Density Gradient

In this problem, CO₂ and CH₄ gases are placed side-by-side and allowed to mix. The strong lateral density gradient between the dense CO₂ gas and the relatively light CH₄ gas causes a strong density-driven flow where CO₂ tends to move downward and CH₄ tends to move upward to the top of the reservoir. Problem specifications and domain schematic are presented in Figure 2.1. An example of the computed results at $t = 1$ yr is shown in Figure 2.3a by the density field as computed by GEM. Comparison of results is presented in Figure 2.3b as horizontal profiles of mole fraction of CO₂ in the gas at two different times. As shown in Figure 2.3b, variations in results between the four codes are more pronounced than for Problem 1, showing that larger differences can be expected for cases of more complex flow and transport. It should be noted, however, that concentrations along the profile at $Z = -50$ m are very sensitive to small variations in the simulation at late times since the interface between the gases is located in this region, and the profile effectively follows this interface.

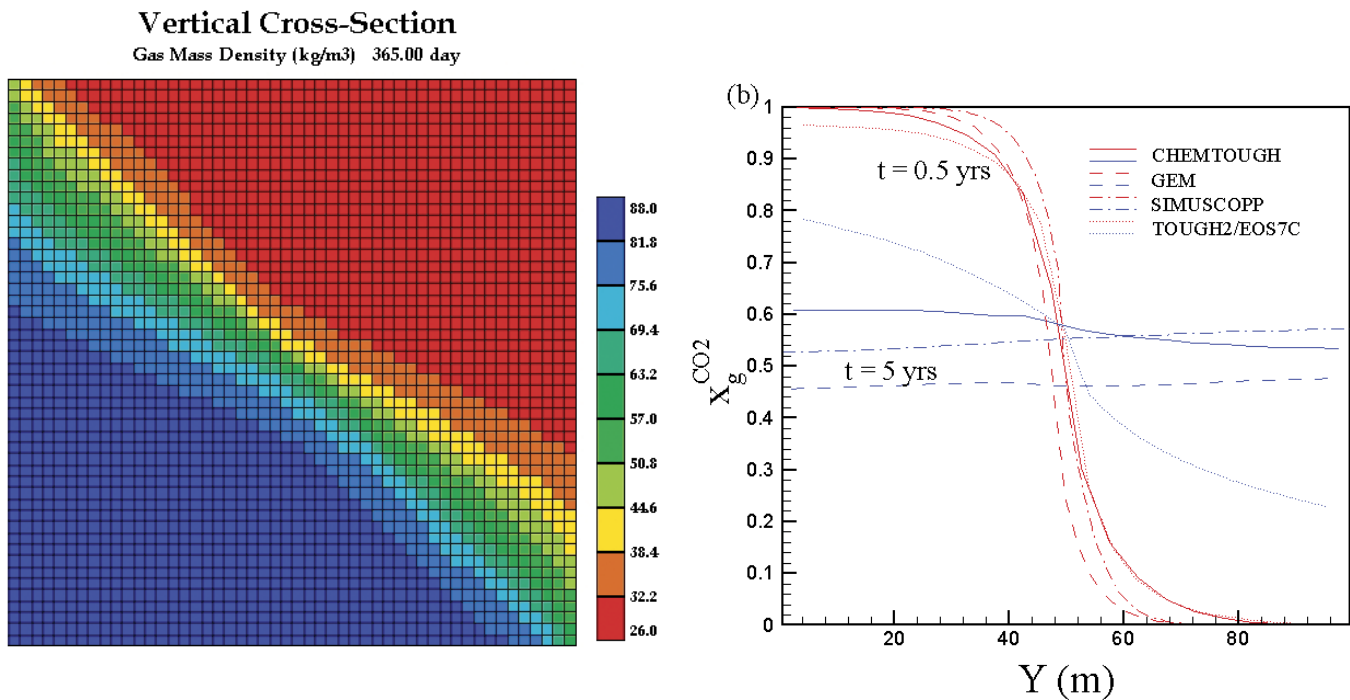


Figure 2.3 Two-dimensional density field (a) and horizontal profiles of $x_g^{\text{CO}_2}$ at elevation $Z = -50$ m (b) for Problem 2.

2.5 Discussion and Conclusions

Physical property estimates and simulation results for the mixing of CO₂ and CH₄ gases show fair to good agreement. Overall, the four simulation codes model the general processes of molecular diffusion and density-driven flow and advective mixing similarly, although results differ in details. This comparison has brought to light differences in physical property estimates to which differences in simulated results are likely attributable. While process description and problem setup are subjective since they are influenced by the experience and approach of the analyst, physical properties are objective and relatively well known. Code developers should endeavor to make physical property estimates more accurate. Nevertheless, in the actual practice of numerical simulation of subsurface processes, the largest differences between simulation results will likely be due to the conceptual models used, including assumptions about reservoir heterogeneity, as opposed to the algorithmic details of codes or physical property estimates.

3. Test Problem 3. Radial Flow from a CO2 Injection Well²

3.1 Problem Description

This is a basic CO2 injection problem that addresses two-phase flow of CO2 and water for simplified flow geometry and medium properties. The aquifer into which injection is made is assumed infinite-acting, homogeneous, and isotropic. Gravity and inertial effects are neglected, injection is made at a constant rate, and flow is assumed 1-D radial (line source). The list of processes studied includes:

- Two-phase flow of CO2 and water subject to relative permeability and capillary effects.
- Change of fluid density, viscosity, and CO2 solubility with pressure and salinity.
- Formation dry-out with precipitation of salt.

Problem specifications are given in Appendix C and in the original intercomparison report (Pruess et al., 2000). Variations are limited to two cases, namely, with and without salinity. During the CO2 Code Comparison Workshop held at Lawrence Berkeley National Laboratory in October, 2001, five groups presented preliminary results (LBNL, LANL, IFP, IRL, and CSIRO). At the workshop, reporting requirements were altered from the original specifications and were agreed upon as follows. *“Results are to be given for pressure, gas saturation, dissolved CO2 mass (or mole) fraction, and “solid saturation” (fraction of pore volume containing solid precipitate). The problem as posed is known to have a similarity solution, with all parameters depending on radial distance R and time t only through the similarity variable $\xi = R^2/t$. Results can be given either as radial profiles at a fixed time, or as time series at a fixed radial distance. It is preferred that both kinds of results should be submitted, to allow checking on the similarity property. It is desired that results should be provided for such a range of times and distances that the similarity variable covers the range $10^{-8} \text{ m}^2/\text{s} \leq \xi \leq 10^1 \text{ m}^2/\text{s}$. In addition, fluid property data should be given at $T = 45^\circ \text{C}$ for pressures $P = 120, 160, 200, \text{ and } 240 \text{ bar}$, for aqueous phase salinities of 0 and 15 weight-%, and for phase conditions of (a) single-phase aqueous, (b) two-phase aqueous-gas. The fluid property data should include densities and viscosities of aqueous and gas phases, and CO2 mass (or mole) fractions in the aqueous phase.”*

3.2 Results Without Salinity

This report includes results from LBNL, CSIRO, IFP, IRL, ARC³ and PNNL. A brief overview of the submitted results and simulation codes used is provided in Table 3.1. All results

² proposed by Karsten Pruess; e-mail: K_Pruess@lbl.gov

³ David Law of ARC wishes to acknowledge help from Peter Sammon and Mohamed Hassam with the GEM simulations.

were reported according to the requirements specified during the 2001 code comparison workshop at LBNL.

Table 3.1 Reported Results

GROUP	CODE	Comments and Observations ¹
LBNL ^a	TOUGH2-ECO2	Preliminary version of Module ECO2 (Pruess and García, 2002a, b; Pruess et al. 1999) Density of liquid phase according to García (2001) Solubility includes fugacity correction and Poynting effect
CSIRO ^a	modified TOUGH2	CO2 module modified from an early version of ECO2 Span and Wagner's (1996) equation of state for CO ₂ Solubility includes fugacity correction and Poynting effect
IFP ^a	SIMUSCOPP	No salt precipitation and no dry-out modeled Water viscosity function of temperature and salinity only Gas properties are defined using Peng-Robinson EOS Soreide & Whitson (1992) EOS equilibrium constants for CO ₂ -H ₂ O
IRL ^b	modified TOUGH2	Solubility includes fugacity correction and Poynting effect
ARC ^b	GEM	GEM is a general-purpose compositional simulator
PNNL ^a	STOMP	

¹ Based on personal communication via email

^a Results with and without salinity

^b Results without salinity only

Figure 3.1 shows the evolution of the gas saturation front for times of up to 10,000 days (LBNL results). An important advantage of this radial flow problem is that it admits a similarity solution, even when taking into account all the non-linearities due to PVT properties and two-phase flow (O'Sullivan, 1981; Doughty and Pruess, 1992). The space discretization employed for finite difference simulation will violate the rigorous R^2/t invariance, so that the similarity property will be maintained only approximately. Accuracy of the numerical simulation can be checked by plotting the results as a function of the similarity variable R^2/t . Figure 3.2 shows the results for pressure as a function of the similarity variable. Simulated results are presented at four different times ($t = 30$,

100, 1000, 10000 days) and two fixed locations ($R = 25.25, 1011 \text{ m}$). The agreement is good, confirming the similarity property of the numerical solution. Figures 3.3 and 3.4 show simulated results for gas saturation and dissolved CO_2 mass fraction plotted as a function of the similarity variable. Gas saturation results show three distinct regions emerging from the CO_2 injection process. The first region, $R^2/t \leq 5 \times 10^{-7} \text{ m}^2/\text{s}$, corresponds to a zone where complete dry-out of the aqueous phase has occurred. This region is followed by an intermediate region extending to $R^2/t \approx 10^{-2} \text{ m}^2/\text{s}$, where liquid and gas phases coexist. Finally, in the outer region with $R^2/t > 10^{-2} \text{ m}^2/\text{s}$ single-phase liquid conditions prevail.

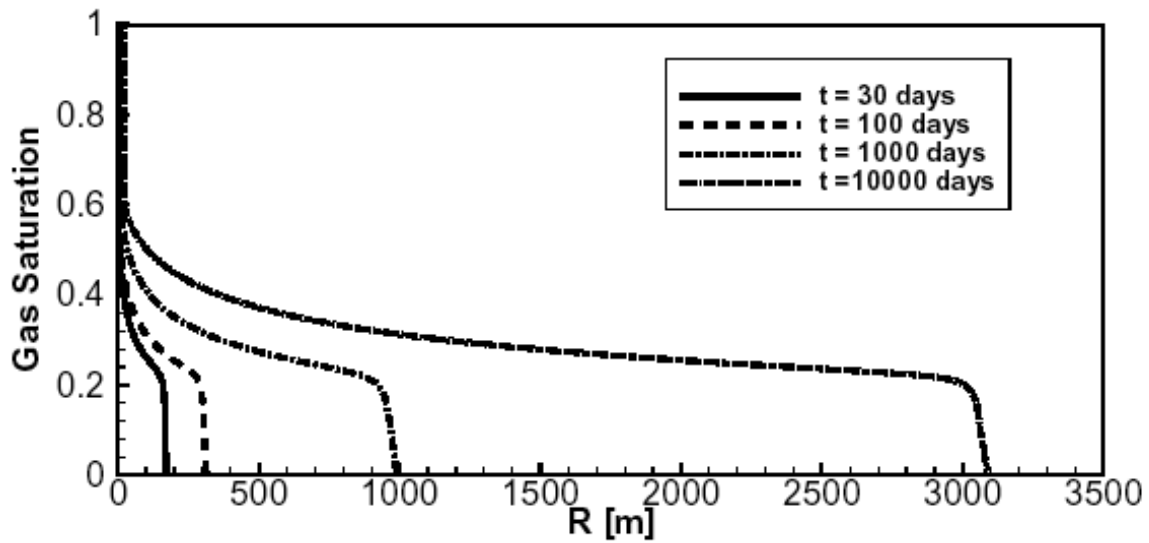


Figure 3.1 Simulated gas saturation front (no salinity, results from LBNL group).

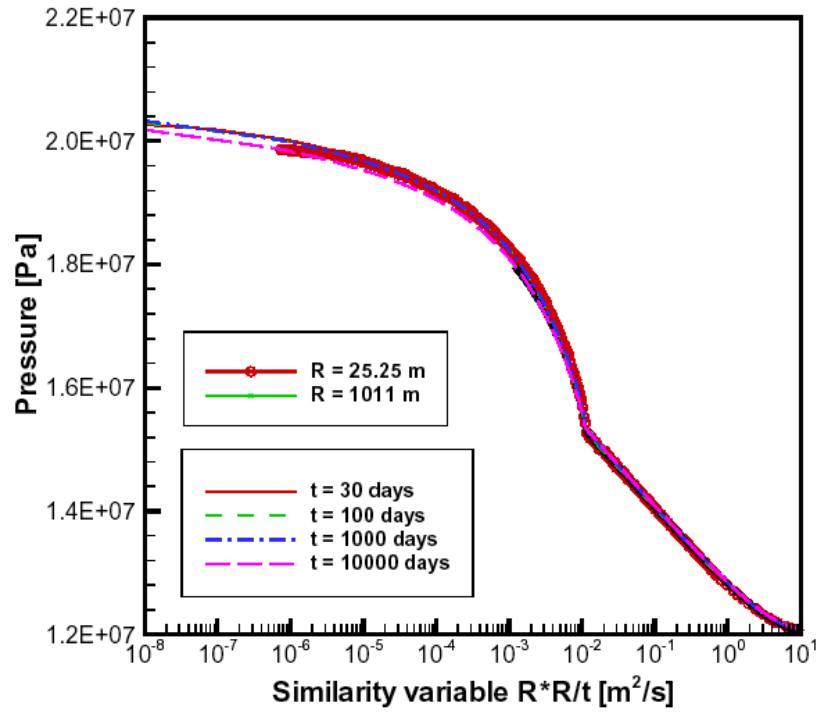


Figure 3.2 Simulated pressures as a function of the similarity variable (no salinity, results from LBNL group).

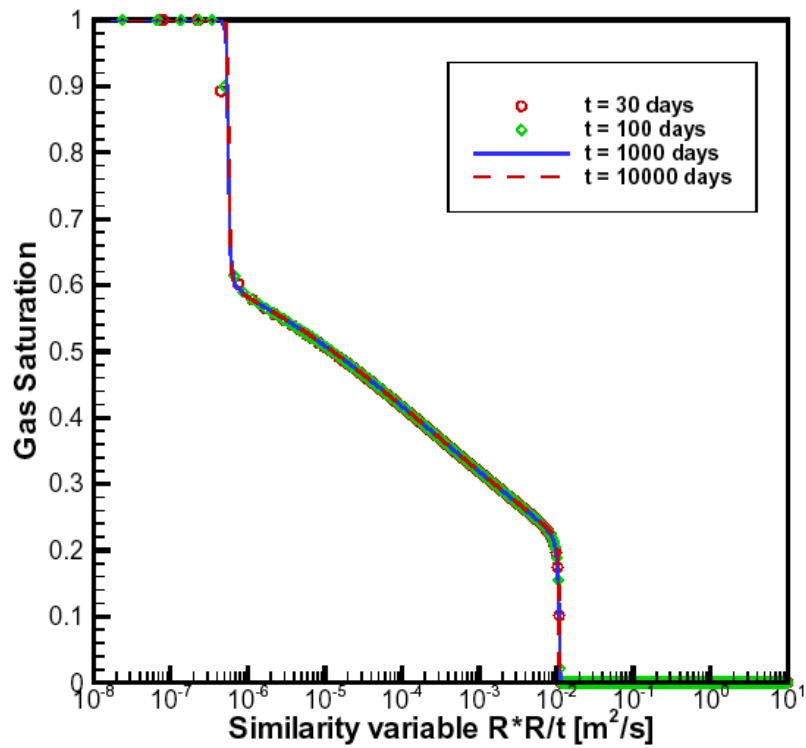


Figure 3.3. Simulated gas saturation as a function of similarity variable (no salinity, results from LBNL group).

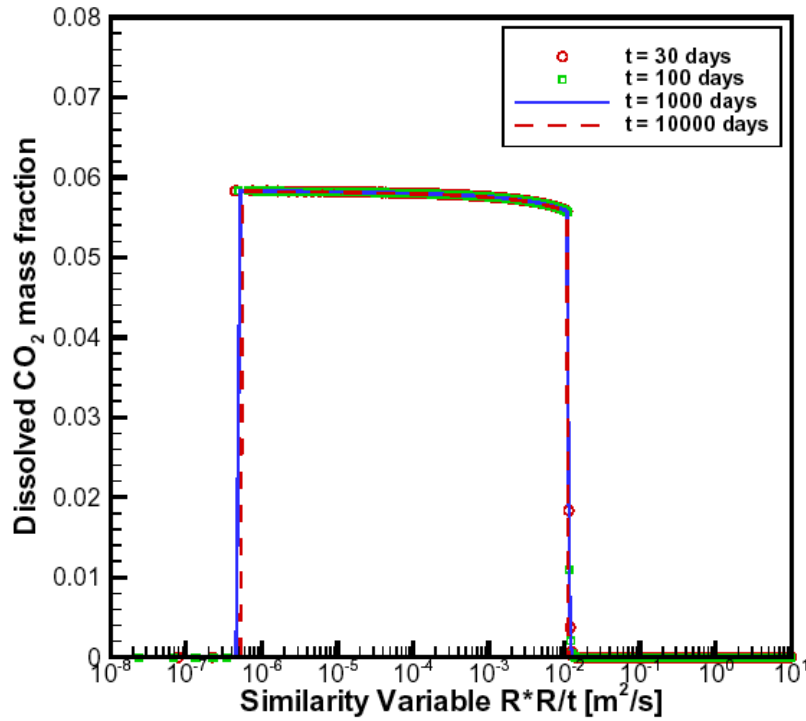


Figure 3.4 Simulated dissolved CO₂ mass fraction as a function of similarity variable (no salinity, results from LBNL group).

LBNL, CSIRO and IRL provided results for radial profiles at fixed time(s) and time series at fixed radial distance(s). IFP, ARC and PNNL reported results only for radial profiles. For all groups, a similarity check was performed by plotting the results for different times or locations as a function of the similarity variable. Among the different groups, IFP was the only one showing small deviations from the similarity property for the pressure profile. IFP results for gas saturation and dissolved CO₂ mass fraction showed that the similarity property was well preserved. A possible explanation for the behavior of pressure is that pressure is more sensitive to grid discretization and boundary effects (IFP, Yann le Gallo, personal communication).

In order to perform the comparison between the codes we selected a profile from each group and plotted them together in a single graph. Pressure results from different groups are shown in Figure 3.5; the agreement is satisfactory. Results for CO₂ gas saturations in Fig. 3.6 expose some differences, especially near the well ($R^2/t \leq 5 \times 10^{-6} \text{ m}^2/\text{s}$), since not all models can treat formation dry-out. The codes agree in placing the transition from two-phase to single-phase liquid conditions at the same location, $R^2/t \approx 10^{-2} \text{ m}^2/\text{s}$. The logarithmic scale for the similarity variable makes differences in gas saturations appear more significant than they are. Note that the region $R^2/t \leq 10^{-6} \text{ m}^2/\text{s}$ with largest differences represents at most ($t = 10,000$ days) the first 30 meters.

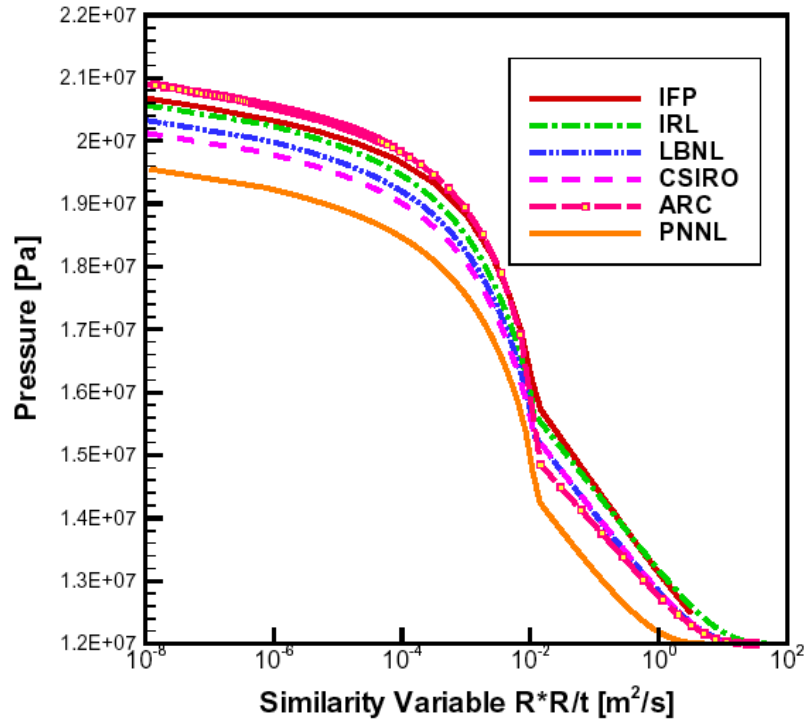


Figure 3.5 Simulated pressures in Problem 3 (no salinity).

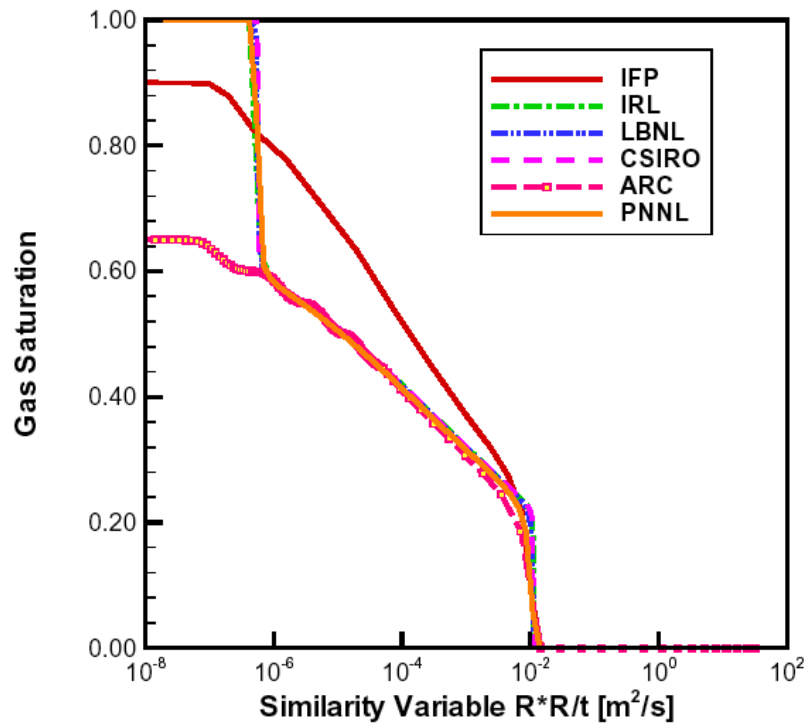


Figure 3.6 Simulated gas saturations in Problem 3 (no salinity).

Figure 3.7 shows that dissolved CO₂ mass fractions span a range of values between 0.044 to 0.066, reflecting differences in solubility formulations between the codes.

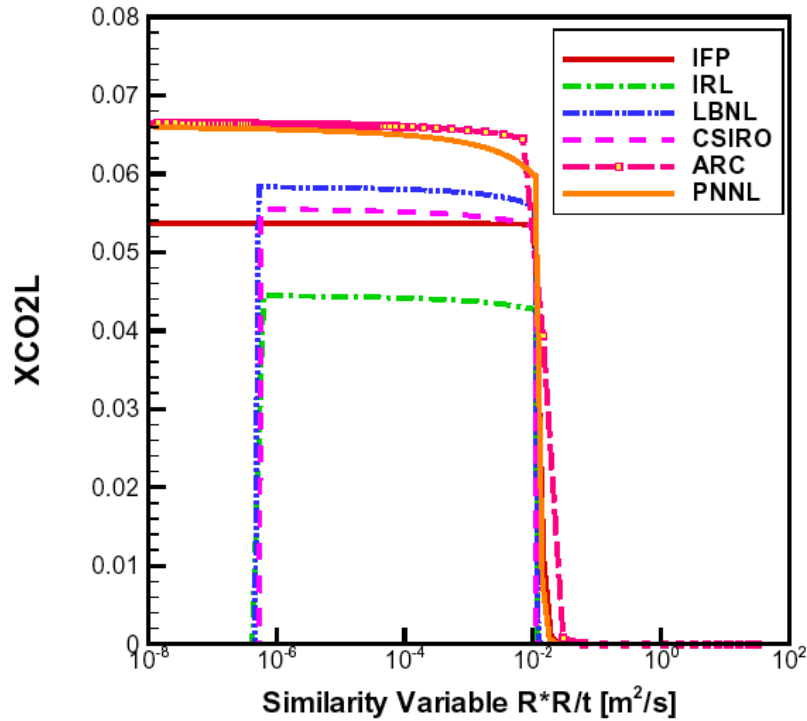


Figure 3.7 Simulated mass fractions of CO₂ dissolved in the aqueous phase in Problem 3 (no salinity).

Reported fluid properties as used in the simulations by different groups for the case without salinity are shown in Figures 3.8 and 3.9. Fluid property data are given at $T = 45\text{ }^{\circ}\text{C}$ for pressures of $P = 120, 160, 200,$ and 240 bar . Some significant differences are apparent, with high and low values differing by about 1.8 % for water density, 3.5 % for density of water with dissolved CO₂, 10.9 % for CO₂ density, 0.7 % for water viscosity, 6.6 % for viscosity of aqueous solutions of CO₂, and as much as 33 % for CO₂ viscosity, and 52 % for CO₂ solubility. No details on PVT correlations or solubility models used were provided by the individual groups. It is recommended that the code developers check their property correlations against experimental data and improve on inaccuracies that may be present.

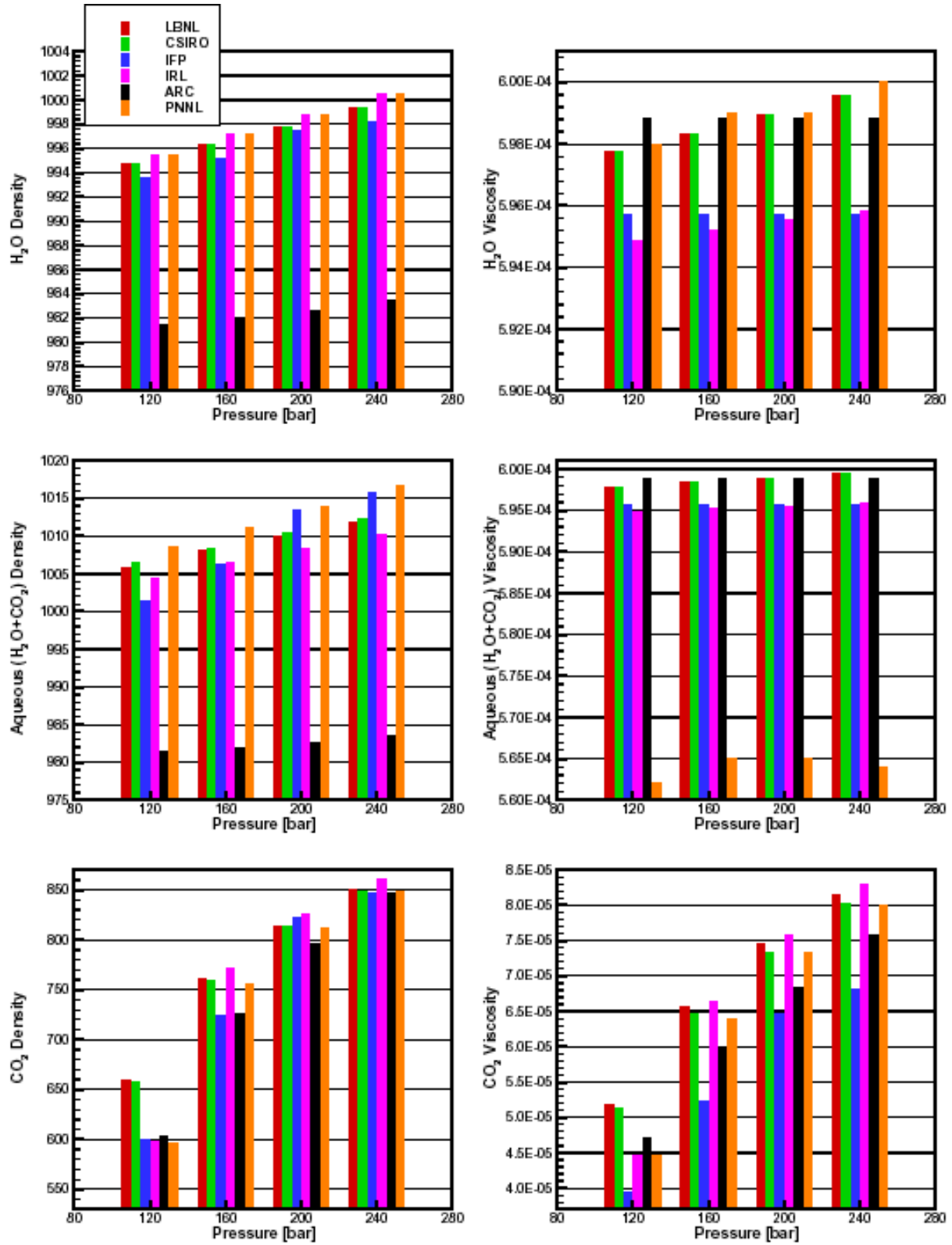


Figure 3.8 Properties of pure fluids and aqueous phase at $T=45^{\circ}\text{C}$ (no salinity; the bars are arranged from left to right in the same order as in the legend).

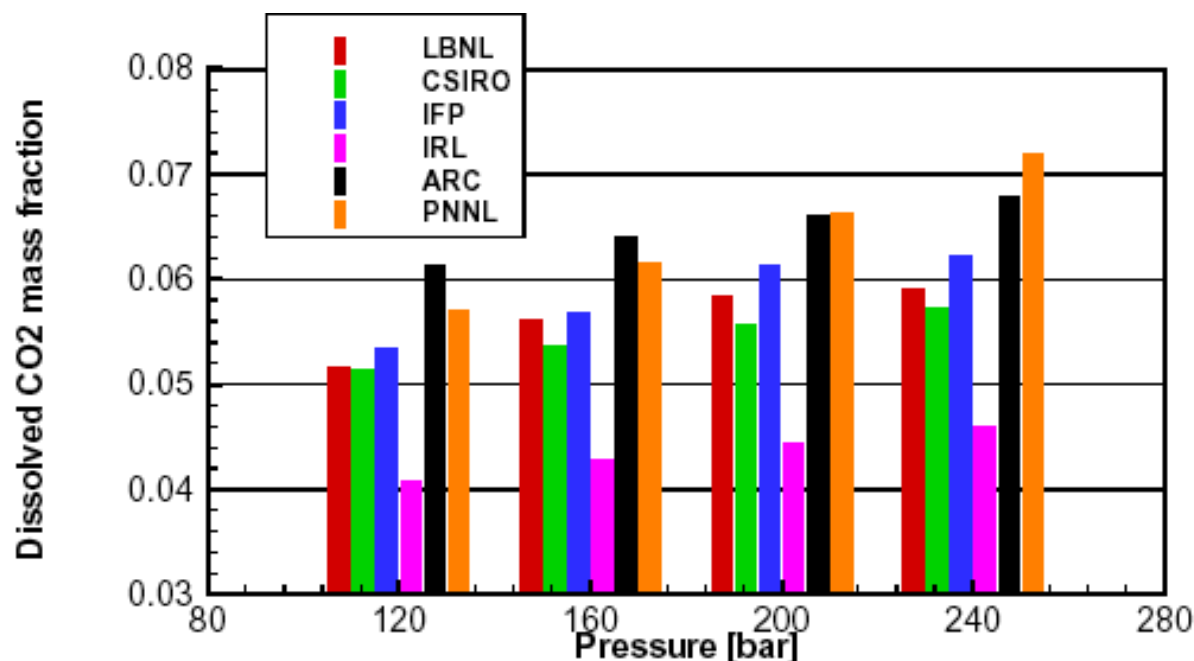


Figure 3.9 Dissolved CO₂ mass fraction in aqueous phase at T = 45 °C (no salinity).

3.3 Results With Salinity

The presence of salt in the system induces additional processes, particularly salt precipitation near the injection well. Not all of the codes have a capability for modeling salt precipitation and tracking the corresponding solid phase saturation. Four groups submitted results that include salinity effects, namely LBNL, CSIRO, IFP and PNNL.

Figures 3.10 through 3.13 compare results for pressure, gas saturation, dissolved CO₂ mass fraction and solid saturation (salt precipitation) as a function of the similarity variable. The LBNL and CSIRO results are almost identical. IFP and PNNL pressures are approximately 3 % high and low, respectively, in comparison. Dissolved mass fractions are similar except for the dry-out region at small R^2/t . IFP shows a considerably different profile of gas saturation.

Figures 3.14 and 3.15 present the reported fluid properties used in the simulations by different groups, again at T = 45 °C and pressures of P = 120, 160, 200, and 240 bar, with a salinity of 15 % by weight in the aqueous phase. Differences between high and low values are 1.3 % for brine density, 0.9 % for aqueous phase density with dissolved CO₂, 4.6 % for brine viscosity with or without dissolved CO₂, and 26 % for CO₂ solubility. Again, comparisons with experimental data are recommended to confirm a realistic description of fluid properties.

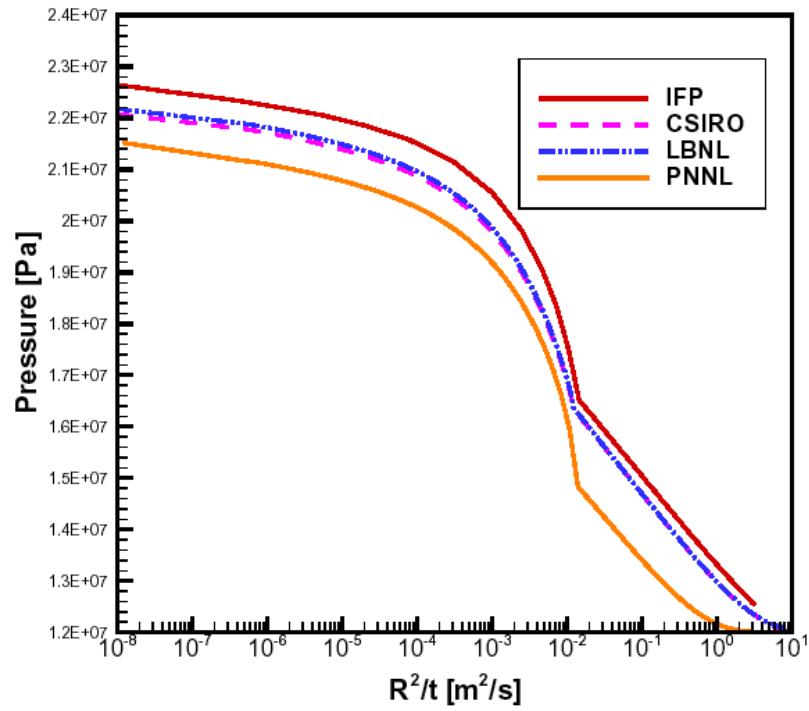


Figure 3.10 Simulated pressures in Problem 3 (15 weight % salinity).

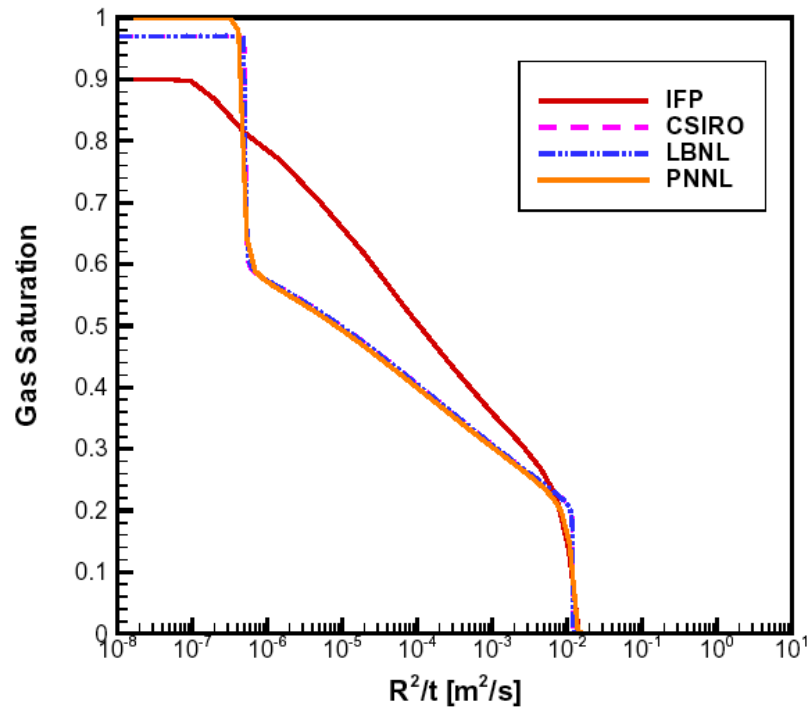


Figure 3.11 Simulated gas saturations in Problem 3 (15 weight % salinity).

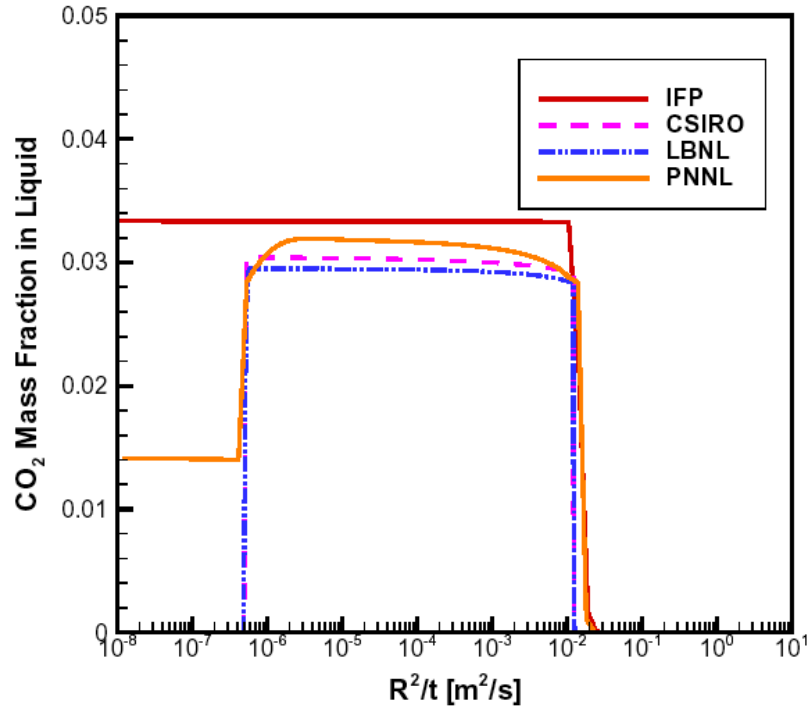


Figure 3.12 Simulated mass fractions of CO₂ dissolved in the aqueous phase in Problem 3 (15 weight % salinity).

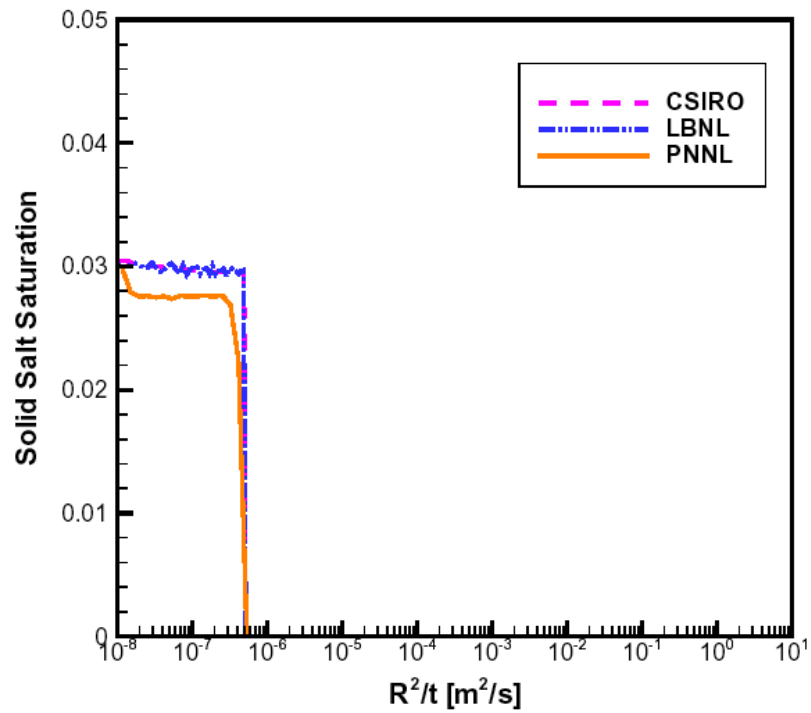


Figure 3.13 Simulated solid saturations in Problem 3 (15 weight % salinity).

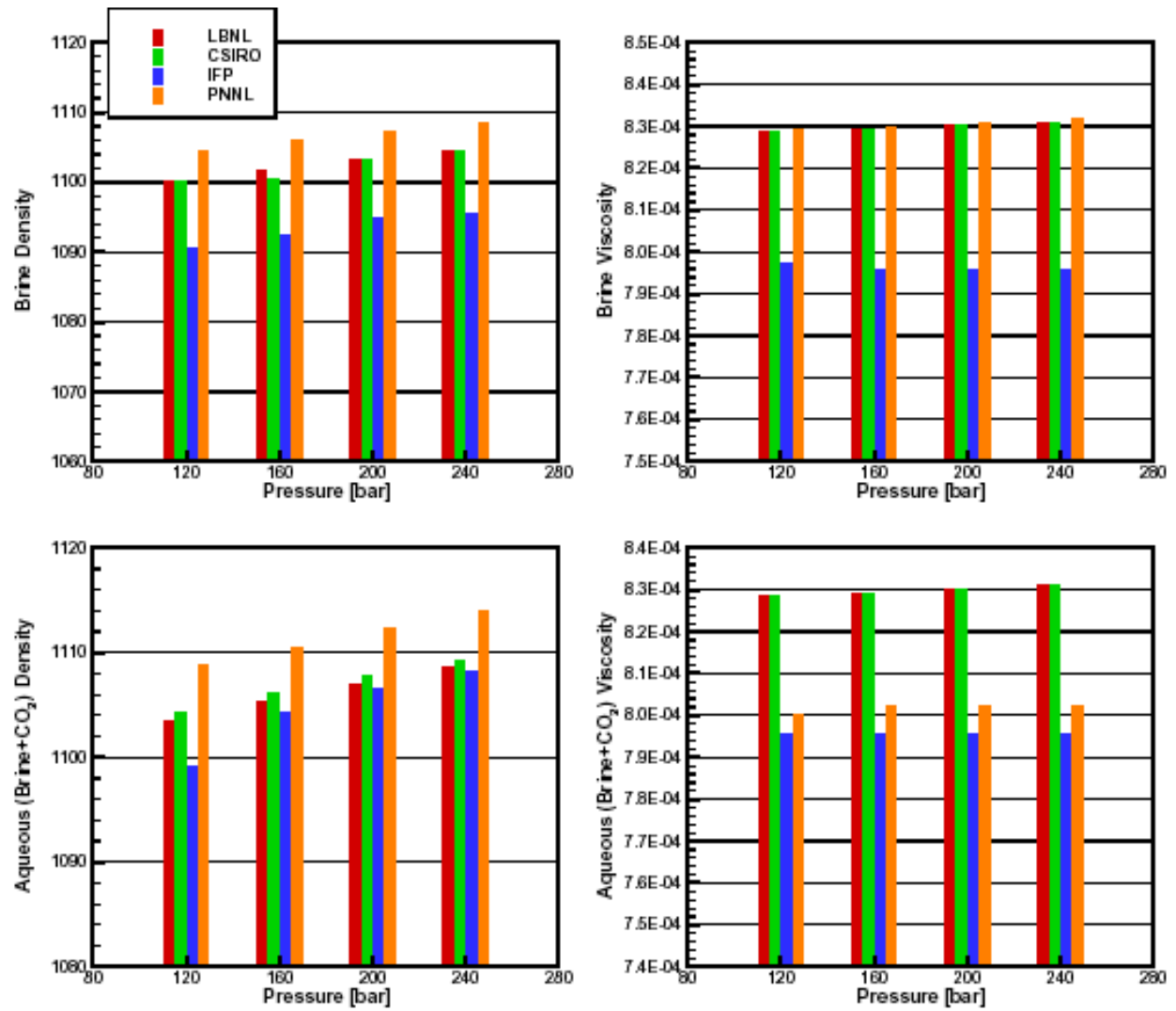


Figure 3.14 Properties of aqueous fluids at T=45 °C (15 weight % salinity).

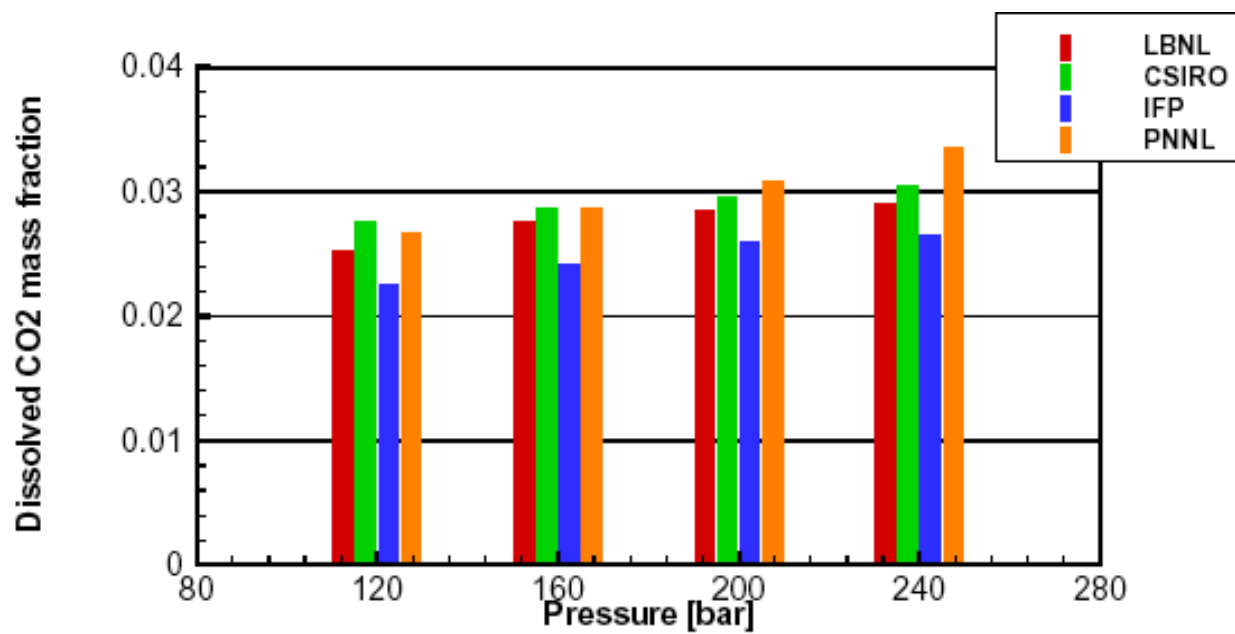


Figure 3.15 Dissolved CO2 mass fraction in aqueous phase at $T = 45^{\circ}\text{C}$ (15 weight % salinity).

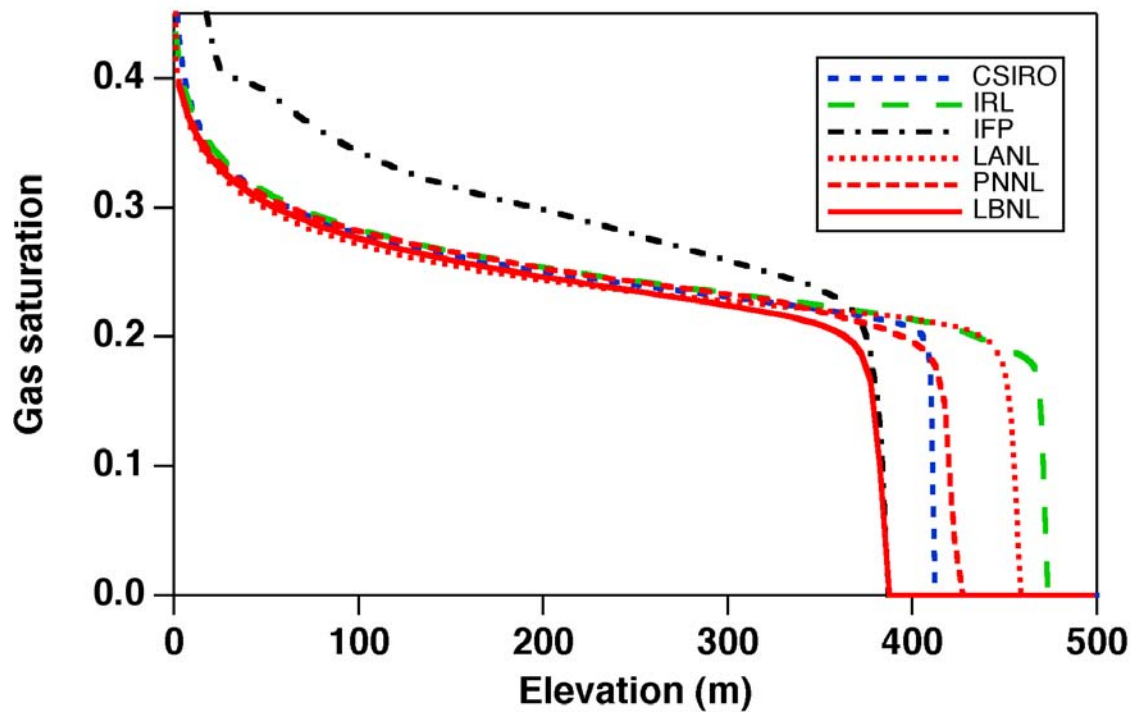
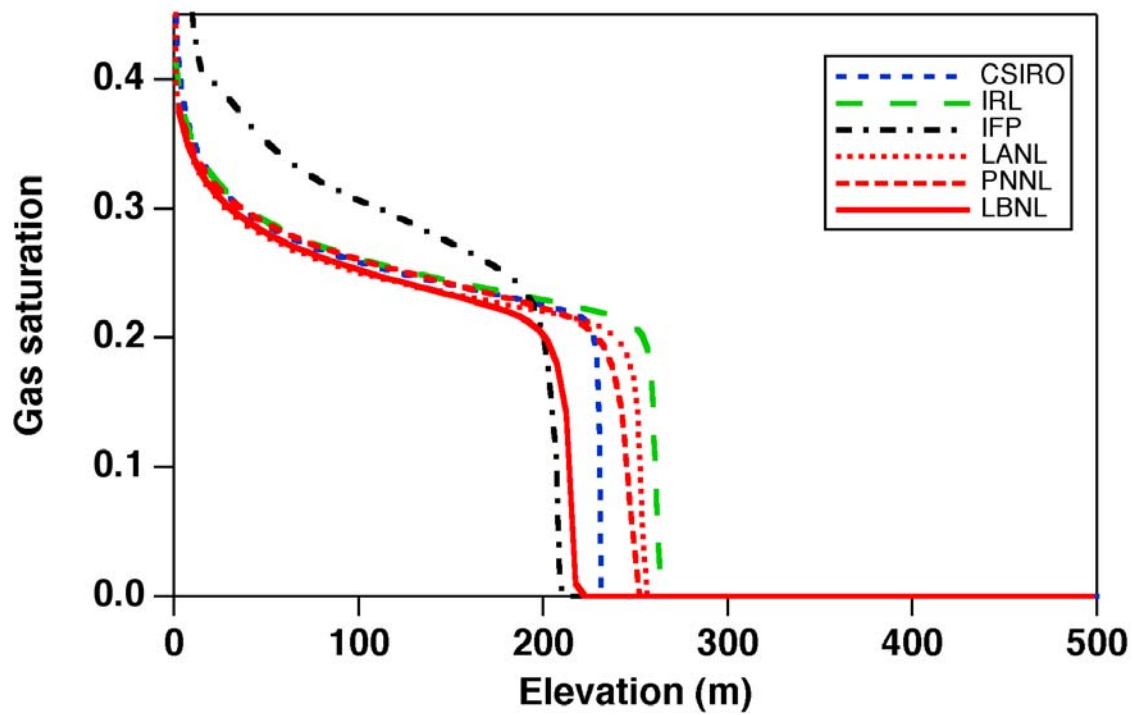


Figure 4.2 Gas saturations for CO₂ migrating up a fault zone at times of 10^7 seconds (top) and 2×10^7 seconds (bottom).

the displacement front at times of 10^7 and 2×10^7 seconds, respectively, are shown in Fig. 4.2. Here and in what follows we refer to the supercritical CO₂-rich phase as “gas” for simplicity. All simulations except IFP are seen to agree well for the displacement profile, but there is a considerable range in the predicted location of the displacement front, indicating differences in total CO₂ volume in the gas phase. The different shape of the saturation profile calculated by IFP suggests differences in fractional flow (relative mobilities) of gas and liquid phases (Buckley and Leverett, 1942). It was hypothesized that this may be due to differences in relative permeabilities and/or fluid viscosities, but an effort to determine the cause(s) of the discrepancy remained unsuccessful. Differences in fluid properties such as CO₂ viscosity may account for some of the differences, but do not seem to be able to fully explain them (fluid properties here are the same as for problem 3, see above). PNNL also found an error in their calculation of aqueous phase densities, that has some impact on simulation results (Mark White, personal communication). Their revised results were submitted too late to be included in this report, but the CO₂ inventories corresponding to the corrected solution are given in Table 4.1, below.

Differences in the advancement of the saturation front can be explained in terms of differences in CO₂ solubilities between the codes, see Fig. 4.3. Dissolution of CO₂ in the liquid (aqueous) phase for the thermodynamic conditions of this problem (temperature of 45 °C, pressures in the range of 100 to 250 bar) is subject to strong non-idealities, which are approximated differently by the different codes. The solubility formulation used by IRL, CSIRO, and LBNL shows a very small increase of dissolved CO₂ mass fractions for the higher pressures at lower elevations, while LANL, IFP, and PNNL have significant increases in dissolved CO₂ mass fractions at the higher pressures below the displacement front. A review of experimental data indicates that CO₂ solubility in water is proportional to CO₂ partial pressures at pressures of a few bars, but increases only very weakly with pressure beyond 100 bar (Ennis-King, private communication 2001; Spycher et al., 2002). An earlier simulation of problem 4 by LBNL had neglected the Poynting correction for CO₂ solubility (Prausnitz et al., 1986), and resulted in solubilities that were too large and increased too much with pressure (Pruess et al., 2002).

For the three simulations with nearly pressure-independent CO₂ solubility (IRL, CSIRO, LBNL), the relative positions of the displacement fronts are consistent with the solubility differences, with lowest solubility (IRL) corresponding to the most advanced front. Differences in gas front position between LANL and PNNL are also consistent with their differences in solubilities.

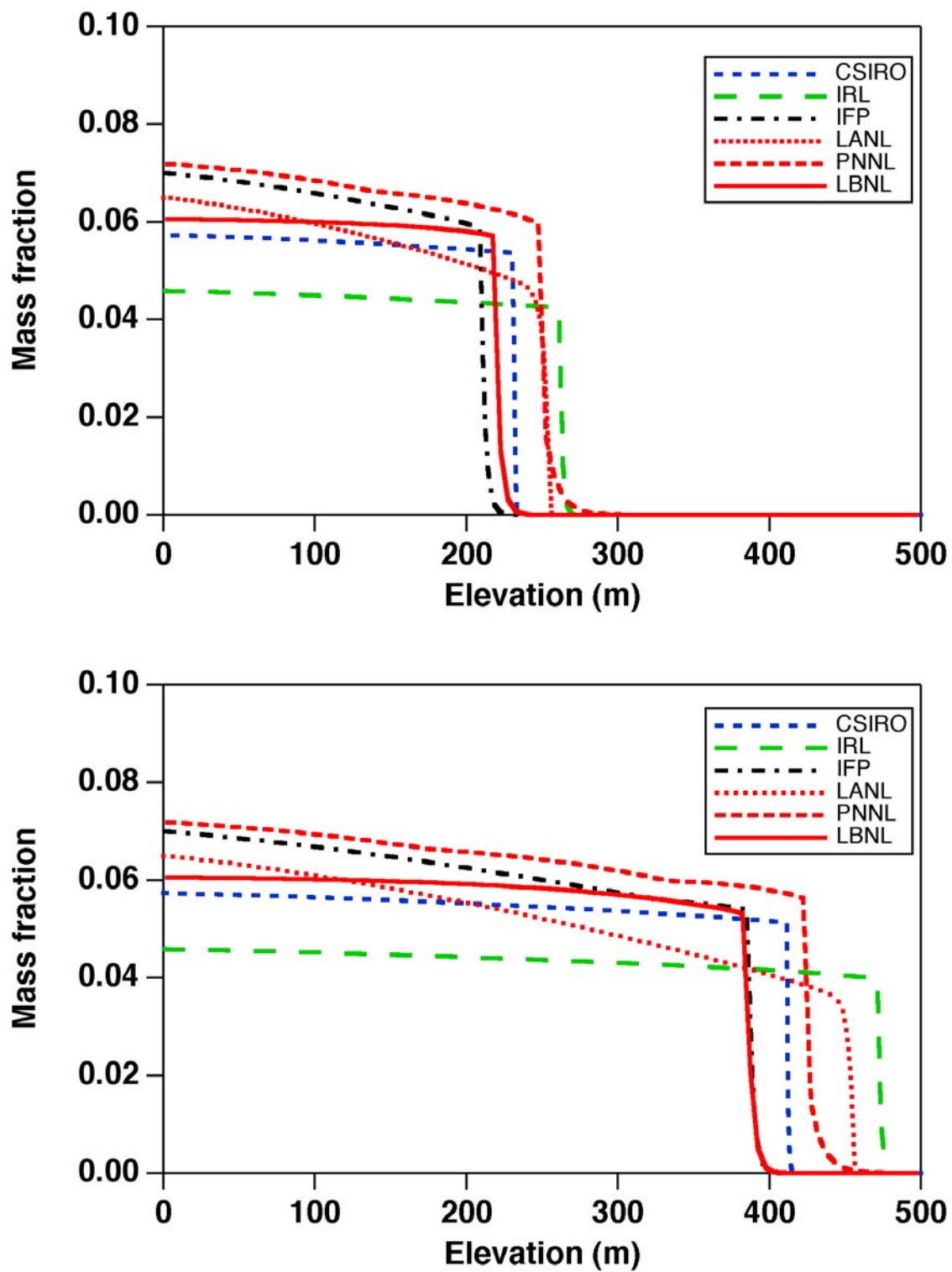


Figure 4.3 Mass fractions of CO₂ dissolved in the liquid (aqueous) phase at times of 10⁷ seconds (top) and 2x10⁷ seconds (bottom).

Another interesting aspect of the fault discharge problem is the time dependence of water and CO₂ fluxes, see Figs. 4.4 through 4.6. CO₂ flux entering the fault is very large at early time, due to the step change in boundary conditions, and then slowly decreases until, at about 2.5×10^7 s, the CO₂ front breaks through at the top boundary (Figs. 4.4, 4.5). Outflow of water at the top starts after about 10^4 s, when the pressure pulse from CO₂ injection reaches the top boundary. Water outflow increases rapidly at first, then goes through a quasi-steady period as the displacement front advances up the fault. CO₂ breakthrough at the top is accompanied by a rapid drop in water flux, followed by a long period of slow decline which corresponds to the gradual drying out of the system as water evaporates into the CO₂ stream. The simulations shown in Figs. 4.4 - 4.6 agree well in the representation of this complicated transient behavior. Non-monotonic behavior is evident in the PNNL simulation for CO₂ inlet flux at early times, which is probably due to space and time discretization effects.

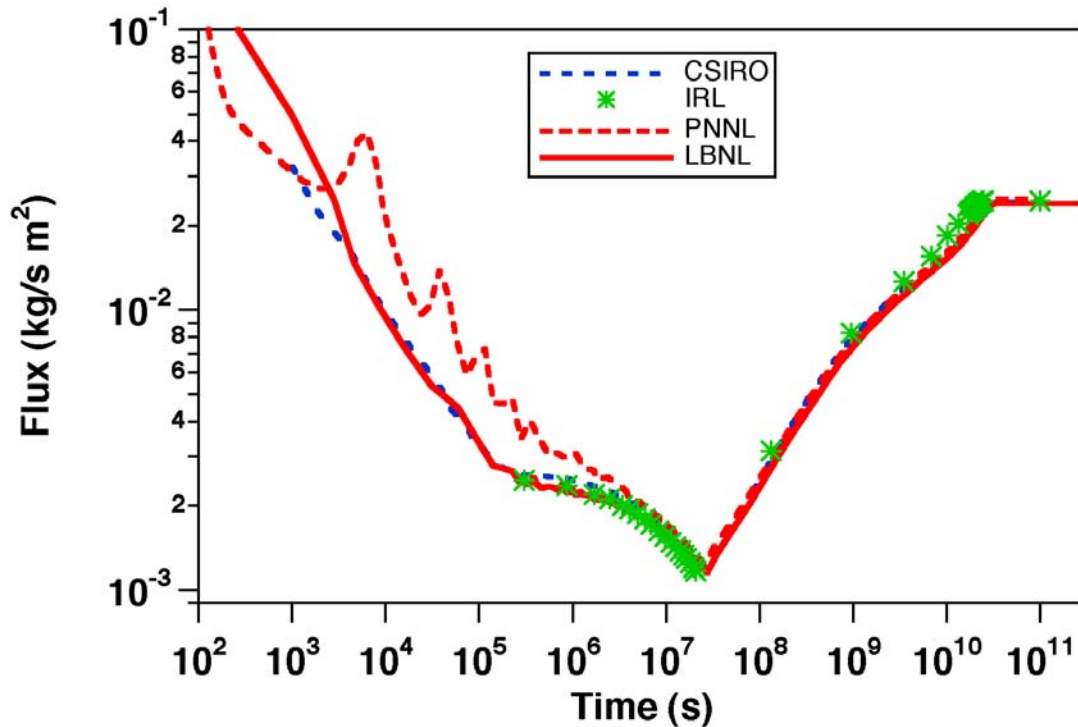


Figure 4.4 CO₂ flux at the bottom of the fault zone.

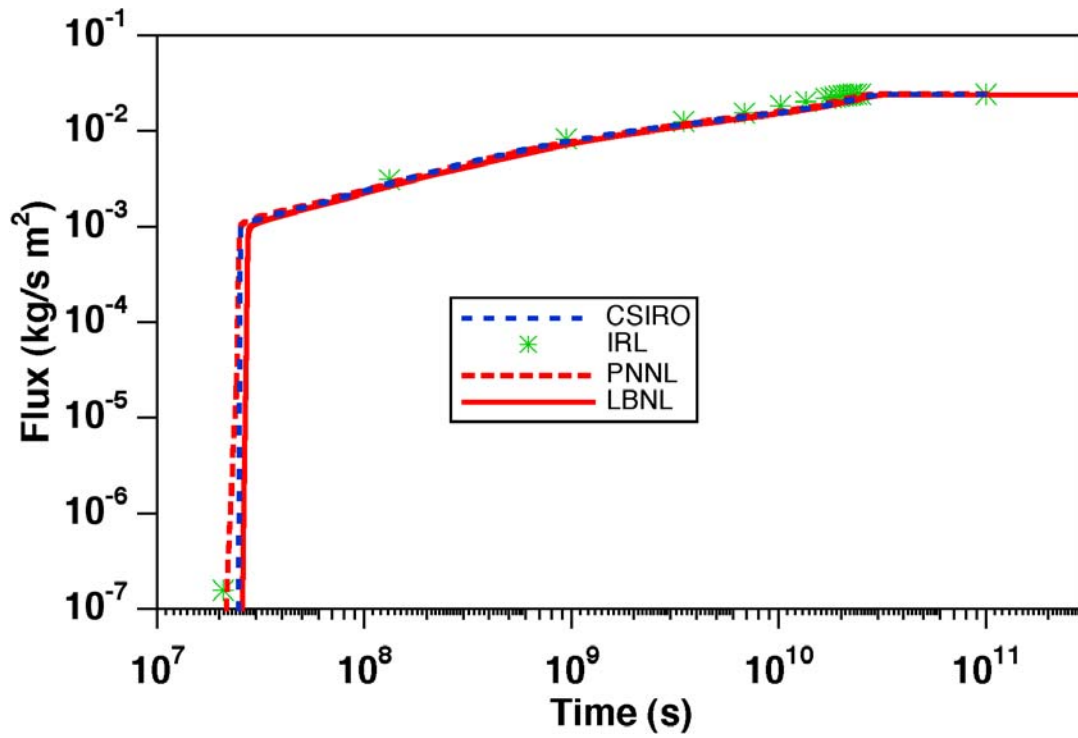


Figure 4.5 CO₂ flux at the top of the fault zone.

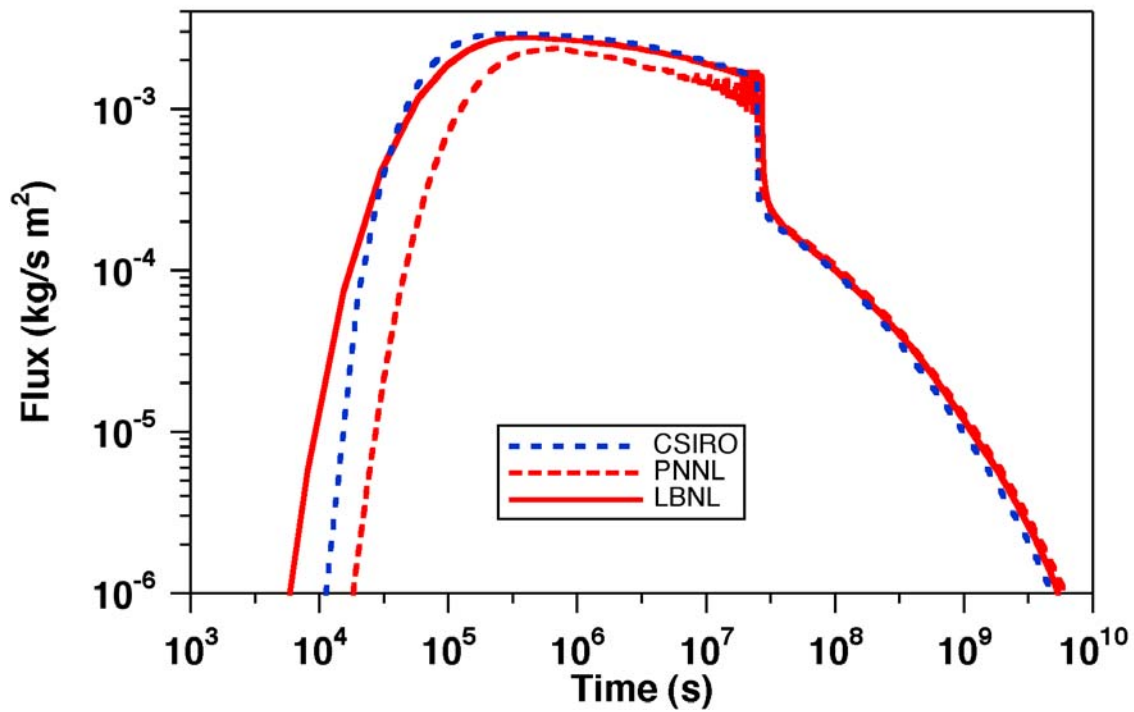


Figure 4.6 Water flux at the top of the fault zone.

Total CO₂ inventories in the fault zone are given in Table 4.1 for two different times, separately for gas and liquid phases. (Results labeled “PNNL I” correspond to the simulation results given in the figures, above, while “PNNL II” is for a revised calculation in which an error in the aqueous phase density calculation was corrected.) For some parameters there is close agreement between different groups, while for others, such as inventory of CO₂ dissolved in the liquid phase, discrepancies are almost a factor 2 between the IRL and PNNL I calculations. The main reason for the large differences in dissolved CO₂ inventory is the substantially larger dissolved mass fraction in the PNNL I calculation (Fig. 4.3), due to different correlations for CO₂ solubility. Gas phase inventories are in better agreement, with differences between highest and lowest figures of 15.1 % at $t = 10^7$ s, and 9.2 % at 2×10^7 s. The LBNL calculation shows the least advancement of the saturation front (Fig. 4.2), hence the lowest gas inventory. CO₂ densities of CSIRO and LBNL are very close (Fig. 3.8), and the differences in gas phase inventories between these two calculations are consistent with the CSIRO saturation front being somewhat more advanced, Fig. 4.2. PNNL I shows considerably higher gas inventories than IRL, even though the latter has a larger gas volume (Fig. 4.2), and slightly larger CO₂ density (Fig. 3.8). It does not seem possible to reconcile this particular discrepancy with the data reported in Figs. 3.8 and 4.2.

Table 4.1 Simulated CO₂ inventories (metric tonnes) per 1 m thickness of the fault zone in gas and liquid phases after 10^7 and 2×10^7 seconds.

		CSIRO	IRL	PNNL I	PNNL II	LBNL
10^7 s	gas	437.7	420.0	456.6	398.0	396.7
	liquid	84.7	65.0	126.8	102.5	86.8
2×10^7 s	gas	746.7	700.0	754.1	692.7	690.5
	liquid	148.5	116.0	206.2	171.5	147.9

In conclusion we note that the codes used for problem 4 are capable of simulating two-phase flow subject to pressure, gravity, and capillary forces, and partial dissolution of CO₂ in the aqueous phase. Intercomparison of results showed substantial agreement, as well as some differences that are partially due to differences in fluid property correlations, may partially be due to discretization effects, and in some cases remain unexplained. Examples of the latter include the different shape of the saturation profile in the IFP calculation (Fig. 4.2), and the modest but unexplained discrepancies in gas inventories between IRL and PNNL.

5. Test Problem 5. Mineral Trapping in a Glauconitic Sandstone Aquifer⁵

5.1 Problem Description

This problem addresses geochemical effects of CO₂ injection into a glauconitic sandstone aquifer, and analyzes the impact of CO₂ immobilization through carbonate precipitation. Batch reaction modeling of the geochemical evolution of this aquifer is performed in the presence of CO₂ at high pressure. The problem is based on Gunter et al. (1997), who modeled water-rock reactions when CO₂ is injected into a glauconitic sandstone aquifer in the Alberta Sedimentary Basin, Canada. The current modeling considers (1) equilibrium aqueous-aqueous and aqueous-gas reactions, (2) redox, (3) the presence of organic matter, (4) the kinetics of chemical interactions between the host rock minerals and the aqueous phase, and (5) CO₂ solubility dependence on pressure, temperature and salinity of the system.

The glauconitic sandstone aquifer (Alberta Sedimentary Basin, Canada) is a medium- to fine-grained litharenite. The average mineral composition is 87% quartz, 2% potassium-feldspar, 1% plagioclase, 5% glauconite, 2% kaolinite, 1% calcite, 1% dolomite, and 1% siderite. The average porosity is 12%. Gunter et al. (1997) modeled water-rock reactions driven by the formation of carbonic acid when CO₂ is injected into deep aquifers using PATHARC.94 (Perkins and Gunter, 1995). In their simulations, the CO₂ injection pressure was set at 260 bar. Annite was used as a substitute for glauconite. Plagioclase was simulated by assuming the presence of discrete fractions of end member components, anorthite and albite. In developing the specifications for the present problem, LBNL initially assumed the same mineralogy as Gunter et al. (1997). The simulation showed that annite is rapidly destroyed with precipitation of siderite (FeCO₃), the latter being the principal mineral trap for CO₂. A maximum of about 40 kg of CO₂ per m³ of host rock medium could be sequestered in mineral phases. Results were similar to those of Gunter et al. (1997).

The use of annite as a substitute for glauconite overestimates the availability of Fe²⁺, the amount of siderite (FeCO₃) precipitation, and hence the degree of CO₂ sequestration. Therefore, the model mineral assemblage was modified to reflect more closely the composition expected in a glauconitic sandstone. A representative glauconite chemical composition and thermodynamic properties were estimated from descriptions of the mineralogical compositions of glauconite and its paragenesis as reported in the published literature (Xu et al., 2001). Oligoclase was incorporated as a solid solution of plagioclase, and the thermodynamic properties of oligoclase were calculated from calorimetric studies of plagioclase solid solutions reported in the literature. Furthermore, organic

⁵ proposed by Tianfu Xu; e-mail: Tianfu_Xu@lbl.gov

matter was assumed to be present in the glauconitic sandstone, and was represented by the generic composition, CH_2O . The decomposition of organic matter is a complex process. A more realistic representation of organic matter should be investigated in the future. Also, instead of using muscovite as a proxy for illite, illite was actually included as a primary mineral. We believe the modified mineralogy more accurately represents the natural conditions. The problem considers redox-sensitive couples such as $\text{Fe}^{3+}/\text{Fe}^{2+}$, $\text{CO}_2(\text{aq})/\text{CH}_4(\text{aq})$, $\text{H}_2\text{O}(\text{aq})/\text{H}_2(\text{aq})$, and $\text{SO}_4^{2-}/\text{HS}^-$, which are very important in the geochemical evolution of sedimentary basins.

The specifications originally stipulated for Problem 5 are given in appendix E, Table E.1. Mineral abundances are based on previous work (Hitchon, 1996, p. 138), but with the addition of a 2.64% volume fraction of organic matter. In the course of this study, goethite (FeOOH) was added as a possible secondary mineral phase, following a suggestion from Peter Lichtner (private communication, 2002). This was the only revision made to the original problem specifications as given in appendix E. Goethite precipitates and competes with siderite for iron, which could reduce the amount of CO_2 sequestration. Goethite parameters were chosen identical to smectite-Ca, see Table E.1. The primary mineral dissolution is considered to be kinetically-controlled, as given by Eq. (E.2) in appendix E. Precipitation of possible secondary minerals (Table E.1, with an initial mineral volume fraction of zero) is represented using the same kinetic rate expression as that for dissolution. However, precipitation can differ in several respects, as nucleation, Ostwald ripening, crystal growth processes, and reactive surface areas must be taken into account in some circumstances (Plummer et al., 1978; Steefel and van Capellen, 1990). To simplify the description of precipitation kinetics, the precipitation kinetic constant for a secondary mineral is assumed to be one order of magnitude greater than its corresponding dissolution rate constant. Note that all rate constants in Table E.1 (including secondary phases) are for dissolution. Because the rate constants assumed for precipitation reactions are larger than those for dissolution, formation of secondary minerals occurs effectively at conditions close to local equilibrium. The reactive surface areas for secondary minerals are set to $0.25 \text{ m}^2/\text{dm}^3$ at all times. Surface areas for illite, kaolinite, smectite-Na, and smectite-Ca are increased by two orders of magnitude, corresponding to the actual predicted geometric surface area based on the assumption that the particles are in the range of 0.1 to $1 \text{ }\mu\text{m}$ in diameter and $0.01 - 0.1 \text{ }\mu\text{m}$ thick. The surface area for glauconite is increased by only one order of magnitude because authigenic glauconite is usually more coarsely crystalline than other clay minerals, as it is commonly observed in crystallites up to 10 mm in diameter.

The geochemical simulations consider 1 m^3 of water-saturated medium. A CO_2 injection pressure of 260 bar was considered. This pressure is the same as that chosen by Gunter et al. (1997) for the glauconitic sandstone aquifer, and is based on the assumption that the aquifer is

1500 m deep, and can sustain CO₂ disposal injection pressures of that magnitude. In the present simulation, the CO₂ gas pressure is assumed to be in equilibrium with the solution at all times. Thus, the CO₂ gas is treated as an exterior boundary condition with a constant pressure. The solubility of CO₂ in the aqueous phase depends on pressure, temperature, and salinity. The detailed formulation of these factors in the model is given in Xu et al. (2001). Reactant phases are those minerals initially present in the aquifer formation. The reactant minerals dissolve progressively into the formation water, thus modifying the water composition and leading to precipitation of product phases, with sequestration of CO₂ upon precipitation of carbonates.

5.2 Results and Discussion

Simulation results were reported by three groups, LBNL, LANL, and IRL, using the simulators TOUGHREACT (Xu and Pruess, 2001), FLOTRAN (Lichtner, 2001) and CHEM-TOUGH (White, 1995), respectively. With the instantaneous imposition of a constant CO₂ pressure of 260 bar on the formation water, the reactant minerals dissolve and secondary mineral phases precipitate. Initially a lower pH (Figure 5.1) is obtained, which is mainly buffered by the CO₂ gas pressure. Later pH increases gradually due to mineral dissolution and precipitation. Note that the time in Fig. 5.1 is plotted in logarithmic scale, in order to show the detailed evolution at early time. The aqueous oxygen concentrations (redox indicator) are presented in Figure 5.2.

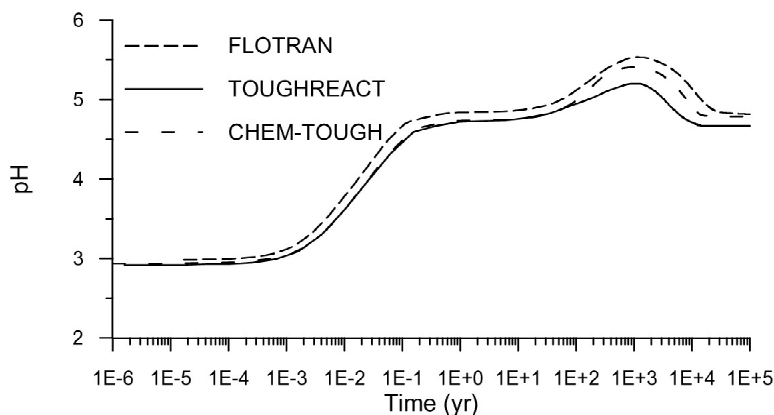


Figure 5.1 pH evolution in glauconitic sandstone with CO₂ injected at 260 bar.

The cumulative sequestration of CO₂, including dissolution in water (solubility trapping) and precipitation of carbonate minerals (mineral trapping), is presented in Figure 5.3. Results from the three codes agree closely. The mineral trapping is caused by alteration of primary minerals and precipitation of secondary minerals. The evolution of individual mineral phases is presented in Figure 5.4. Illite, glauconite, oligoclase, and kaolinite (Figures 5.4a through 5.4d) dissolve under the high gas pressure. Calcite dissolution and dolomite precipitation occur to a limited extent (Figures

5.4e and 5.4f). Siderite precipitation (Figure 5.4g) is significantly greater than dolomite because of lower solubility and rapid glauconite dissolution. Most CO₂ is sequestered through siderite (FeCO₃) precipitation. The pattern of the CO₂ sequestration curve (Figure 5.3) is consistent with that of siderite precipitation. Only minor quantities of CO₂ are sequestered through dolomite precipitation. Goethite initially precipitates, competing for iron with siderite, but later dissolves when glauconite disappears. Precipitation of k-feldspar and smectite-Na can also be observed (Figures 5.4i and 5.4j).

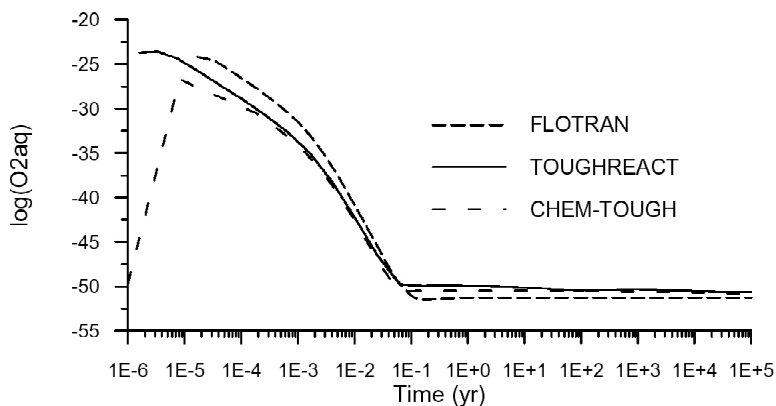


Figure 5.2 Evolution of aqueous oxygen concentration.

Results from the three codes agree reasonably well. Very similar patterns of mineral dissolution and precipitation were obtained in all cases, with some differences in the magnitude of values. The differences in abundances of some minerals may be caused by the slight differences in pH. For example, the TOUGHREACT simulation has the lowest pH (4.67), leading to more calcite dissolution and dolomite precipitation. The primary reason for the difference could be differences in the CO₂ solubility correction as a function of pressure, temperature and salinity. It may be also caused by the following possible differences among the three simulations: (1) thermodynamic data, (2) interpolation coefficients and functions for equilibrium constants, (3) activity coefficients of aqueous species, (4) numerical methods, and (5) time stepping.

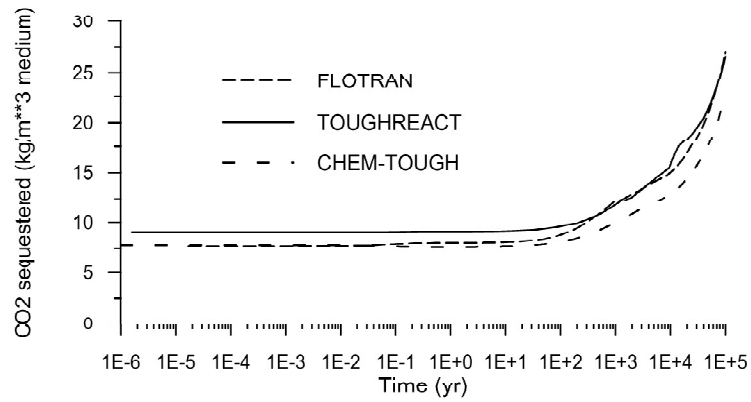


Figure 5.3 Cumulative CO₂ sequestration in glauconitic sandstone with CO₂ injected at 260 bar.

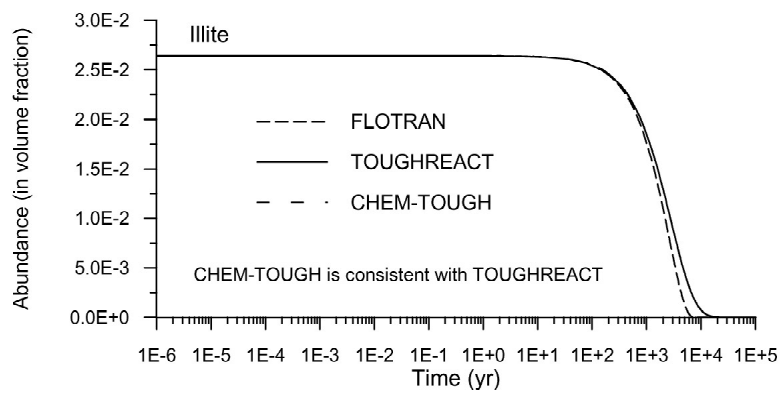


Figure 5.4a

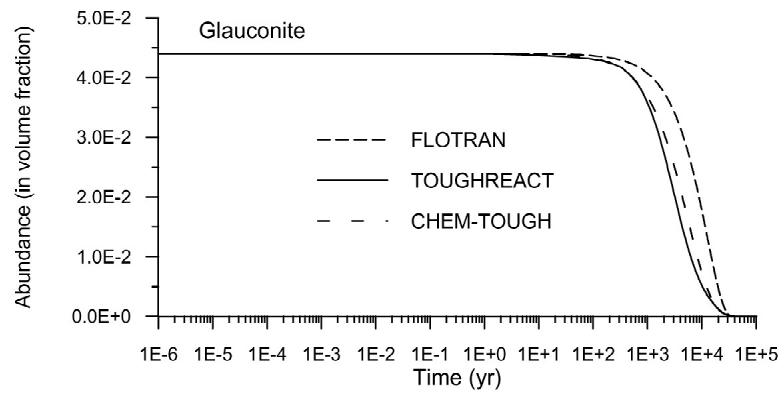


Figure 5.4b

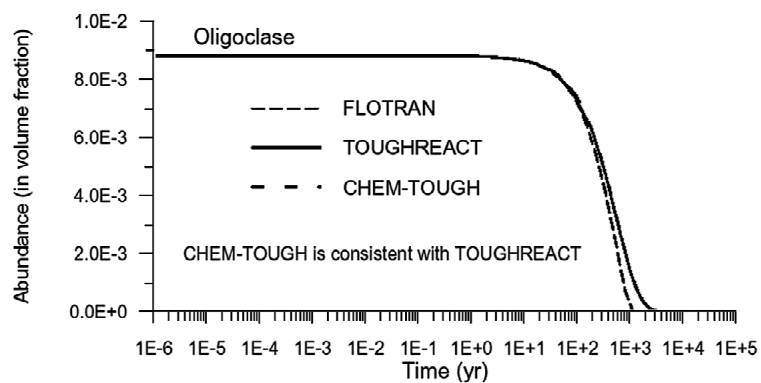


Figure 5.4c

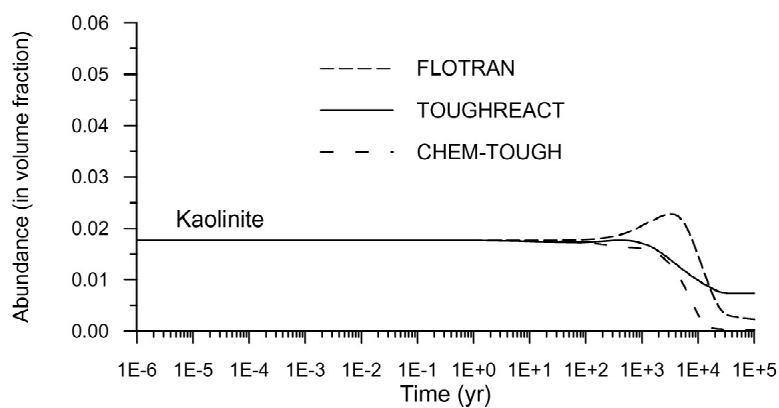


Figure 5.4d

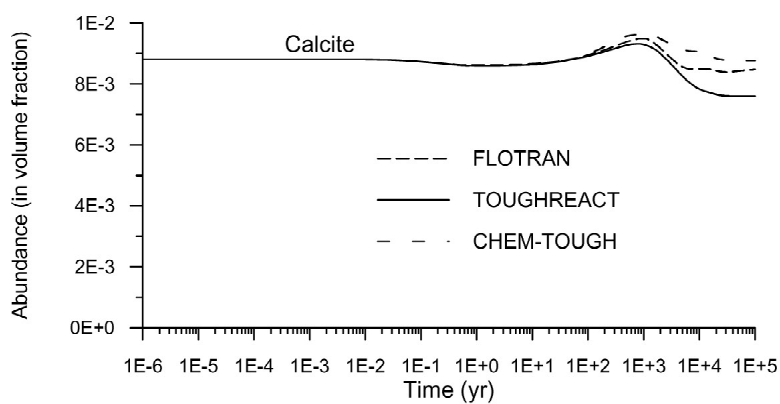


Figure 5.4e

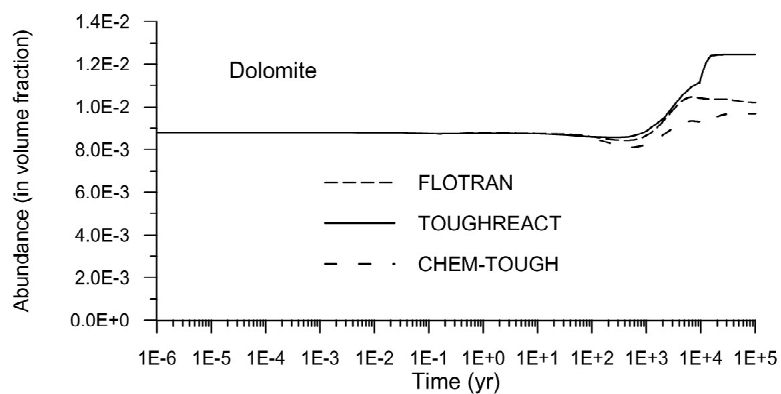


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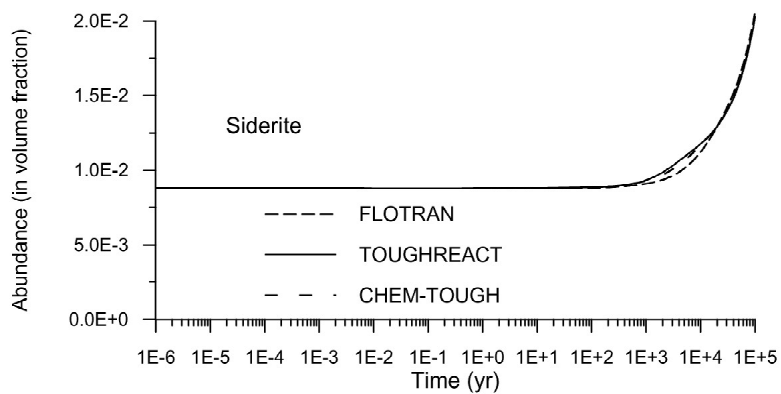


Figure 5.4g

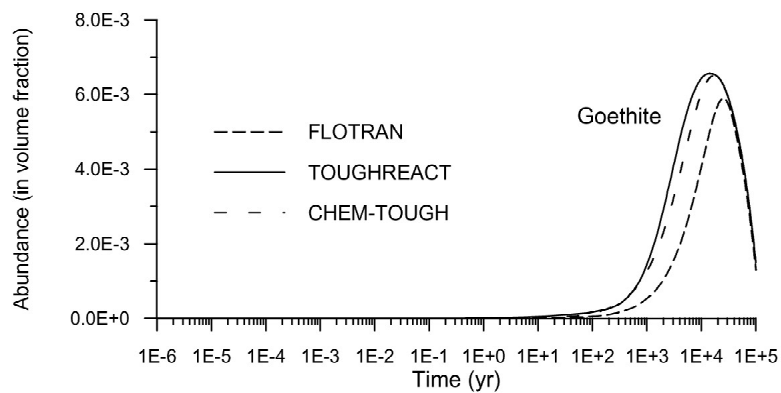


Figure 5.4h

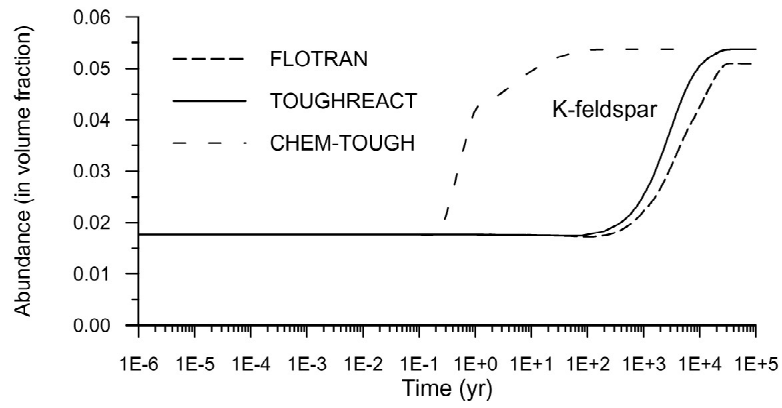


Figure 5.4i

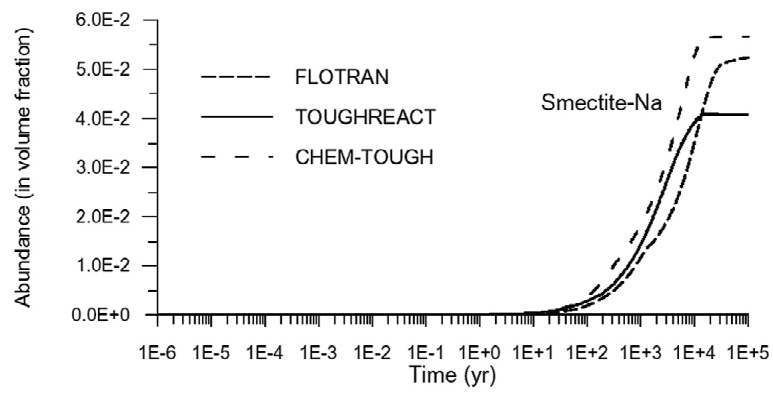


Figure 5.4j

Figure 5.4 Evolution of mineral abundances in glauconitic sandstone with CO₂ injected at 260 bar.

6. Test Problem 6. Hydromechanical Responses During CO₂ Injection into an Aquifer-Caprock System⁵

6.1 Problem Description

Test Problem 6 addresses coupled hydromechanical (HM) changes in an aquifer-caprock system during injection of CO₂ (Figure 6.1). In general, coupled HM interactions during underground fluid injection are governed by changes in effective stress and pore volume, which are accompanied by changes in hydraulic and mechanical properties (Rutqvist and Stephansson, 2003). This test problem is limited to elastic (reversible) deformation with associated changes in porosity and permeability.

Test Problem 6 is simplified to a one-dimensional column according to Figure 6.1. Detailed specifications including material properties, initial conditions and boundary conditions are given in Appendix F. The aquifer has a porosity of 10% and a permeability of $1 \times 10^{-13} \text{ m}^2$, while the caprock has a porosity of 1% and a permeability of $1 \times 10^{-16} \text{ m}^2$. The medium above the caprock is assumed to have the same properties as the aquifer. Both porosity and permeability depend on the effective mean stress, where the effective mean stress is the total mean stress less fluid pressure. The injection operation is simulated by injecting pure CO₂ at 1500 meters depth (Figure 6.1). During an injection period of 30 years, the injection pressure is kept constant at 30 MPa, which is about 90% of the lithostatic pressure at 1500 meters depth.

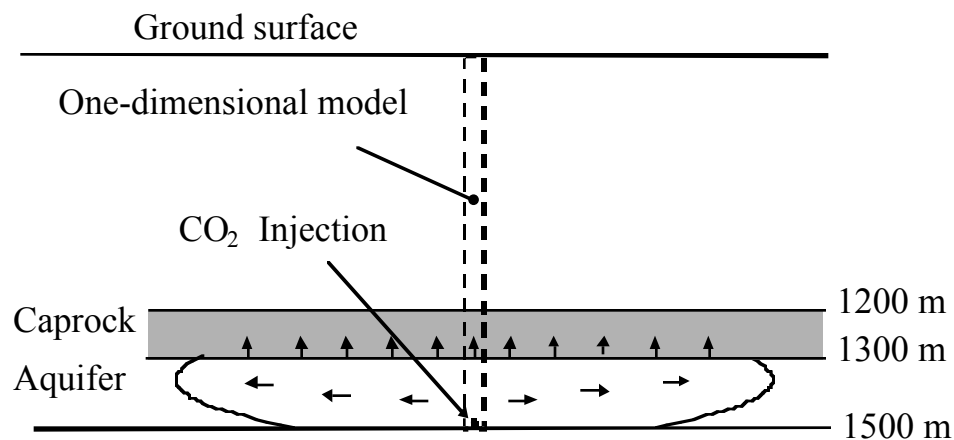


Figure 6.1 One-dimensional model of Test Problem 6 in a general three-dimensional aquifer-caprock system. The exact boundary and initial conditions of the one-dimensional model are given in Appendix F.

⁵ proposed by Chin-Fu Tsang and Jonny Rutqvist; e-mail: CFTsang@lbl.gov, JRutqvist@lbl.gov

6.2 Results

Test Problem 6 has been solved by LBNL using the TOUGH-FLAC simulator (Rutqvist et al., 2002). No solutions were obtained from other groups, and the results should be considered preliminary until confirmed by an independent simulation. The most relevant results of the LBNL solution are presented below.

Figure 6.2 presents fluid pressure versus depth. An apparent steady pressure distribution is obtained after 1 year of injection. At the injection point (1500 meter), the fluid pressure is about 90% of the lithostatic stress. At the lower part of the caprock (1300 meter), the fluid pressure is slightly lower than the lithostatic stress. However, fluid pressure does not exceed lithostatic stress at any part of the column (Figure 6.2).

Figure 6.3 presents effective mean stress versus depth. The initial effective mean stress (at $t = 0$) is equal to the initial isotropic *in situ* stress minus initial hydrostatic fluid pressure. The figure shows that effective mean stress reduces by about 5 MPa in the aquifer, except near the bottom, where a larger reduction is obtained. The 5 MPa decrease in effective mean stress obtained in the aquifer (Figure 6.3) is about 1/3 of the increase in fluid pressure (Figure 6.2). Effective mean stress changes less than fluid pressure because the effective stress cannot change in two horizontal directions (in the plane of Figure 6.1 and normal to it) as no lateral expansion is allowed in the model. The vertical effective stress, on the other hand, reduces by a magnitude of $\Delta\sigma'_v = \Delta\sigma_v - \Delta P = 0 - 15 = -15$ MPa. In this calculation the total stress in the vertical direction is constant (i.e. $\Delta\sigma_v = 0$) because the ground surface is mechanically free. The resulting change in effective mean stress can then be calculated as $\Delta\sigma_m = (\Delta\sigma_v + \Delta\sigma_{H1} + \Delta\sigma_{H2}) / 3 = (-15 - 0 - 0) / 3 = -5$ MPa.

The flow of CO2 through the aquifer-caprock system is depicted in Figures 6.4 to 6.6. Figure 6.4 shows that CO2 breaks through the upper part of the cap (1200 meters depth) after about 19 years, and the flow rate reaches a maximum at 30 years, when the injection is stopped. After 30 years, CO2 continues to flow through the cap as long as an excess fluid pressure (above hydrostatic) remains in the aquifer. Figure 6.5 shows that it takes more than 10 years for the CO2 to reach the lower part of the cap, but after 30 years the CO2 has already penetrated the cap and migrated up to about 1000 meters depth. Figure 6.6 shows that after 100 years, the CO2 saturation above the cap and in the lower part of the injection aquifer is close to the value of residual gas saturation ($S_{gr} = 0.05$) assigned for the CO2 relative permeability function. In the upper part of the aquifer, the gas saturation is close to $1 - S_{lr}$, where $S_{lr} = 0.3$ is the residual liquid saturation.

The effect of hydromechanical coupling is depicted in Figures 6.7 and 6.8. Figure 6.7 shows that CO₂ migrates upwards slightly faster when HM coupling is considered. This increased CO₂ migration rate is caused by a stress-induced increase in permeability as shown in Figure 6.8. However, for the material properties assumed in Test Problem 6, stress-induced changes in permeability are small, a factor 2 or less. Consequently, the effect of HM coupling in Figure 6.7 is small also.

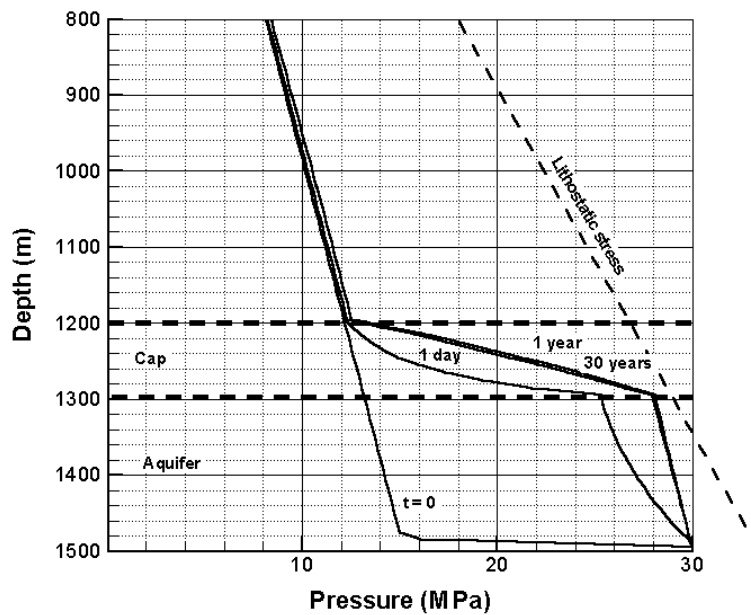


Figure 6.2 Calculated fluid pressure using the TOUGH-FLAC simulator. Note that the fluid pressure does not exceed the lithostatic stress at any point in the vertical column.

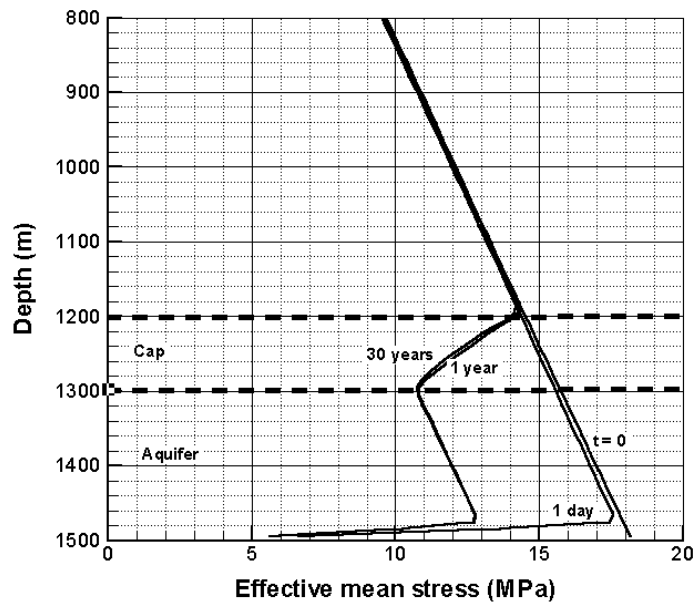


Figure 6.3 Calculated effective mean stress using TOUGH-FLAC simulator. Note that the magnitude of effective means stress changes about 1/3 of the fluid pressure changes at corresponding depth.

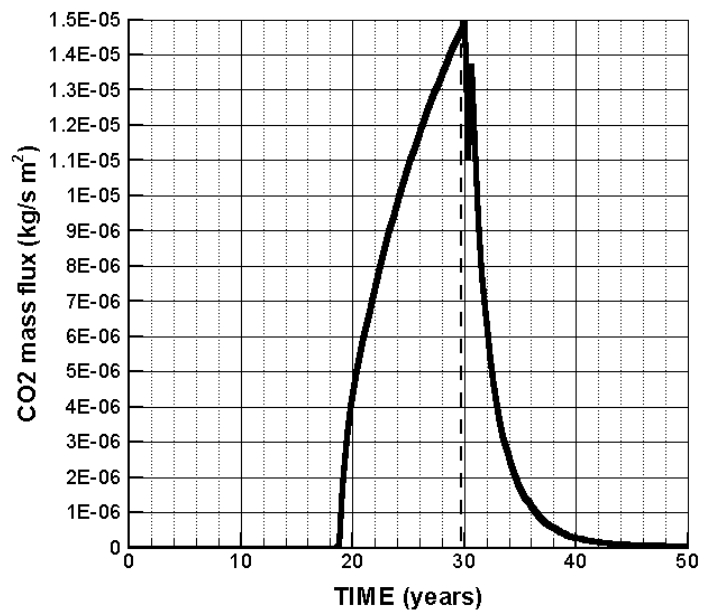


Figure 6.4 Calculated CO₂ mass flux through the upper part of the caprock (1200 meters). Note that CO₂ penetrates the cap at 19 years.

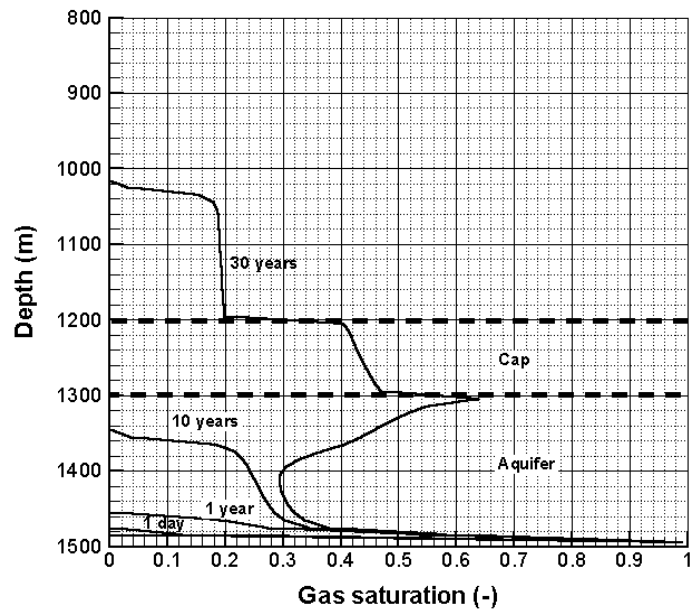


Figure 6.5 Calculated CO₂ gas saturation at various times during 30-year injection of CO₂.

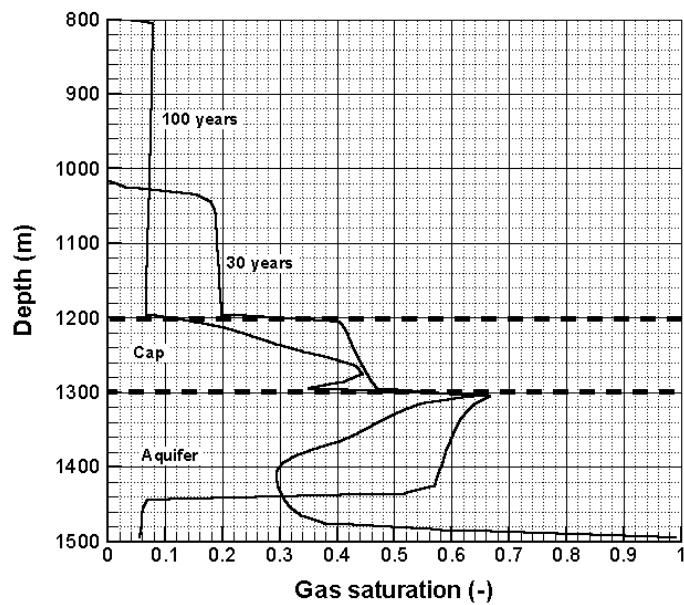


Figure 6.6 Calculated CO₂ gas saturation after 30 and 100 years. The CO₂ injection stopped at 30 years.

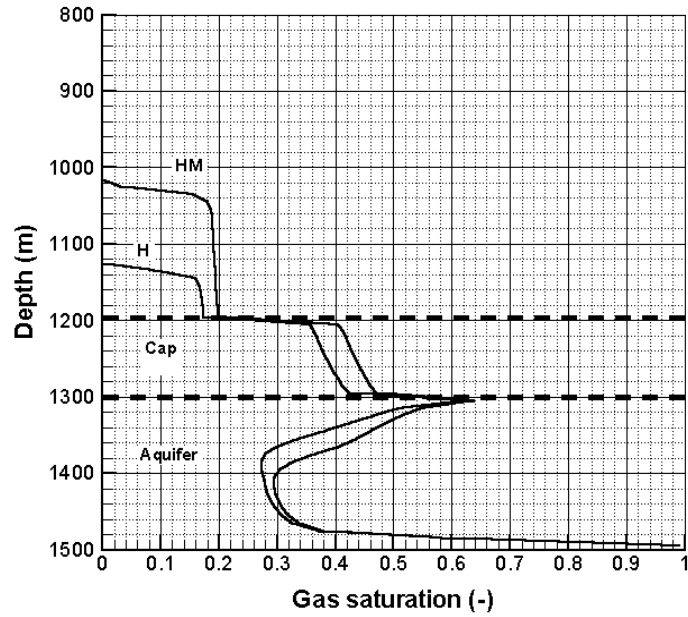


Figure 6.7 Calculated CO₂ gas saturation at 30 years for a pure hydraulic calculation (H) and a coupled hydromechanical (HM) calculation.

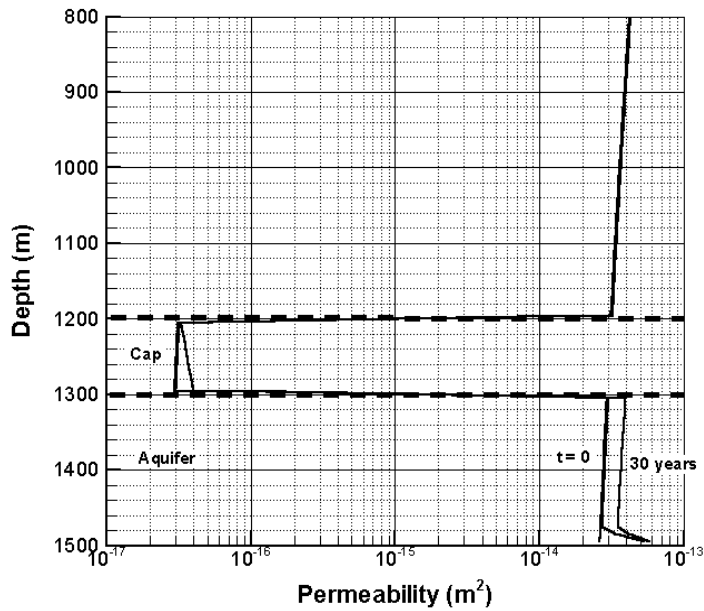


Figure 6.8 Calculated permeability profile at various times. The maximum change of permeability after 30 years is less than a factor of 2.

6.3 Discussion

This problem can be considered a first basic test of HM capabilities of coupled THMC codes for analysis of geologic sequestration of CO₂. In this test case, the effect of HM coupling is small for the properties assumed. With the assumed stress-permeability function, the permeability could theoretically increase by one order of magnitude if the mean stress would go to zero. However, as shown in Figure 6.3, the mean stress changes much less than the increase in fluid pressure, and therefore the permeability does not change dramatically. A far more dramatic effect on permeability could be obtained in fractured media and especially if fracture opening and shear slip is induced along pre-existing fractures (Rutqvist and Stephansson, 2003). Analysis of shear-slip and local fracture opening in a heterogeneous aquifer-caprock system would require two- or three-dimensional analysis as conducted by Rutqvist and Tsang (2002). Such problems in HM coupling should be tackled in code intercomparison studies once the one-dimensional problem has been solved by several independent codes.

7. Test Problem 7. CO₂ Injection into a 2-D Layered Brine Formation⁷

7.1 Introduction and General Description

This problem is intended to represent the dominant physical processes associated with the injection of supercritical CO₂ into the Utsira Formation at the Sleipner gas field in the North Sea (Kongsjorden et al., 1997; Lindeberg et al., 2002). Many of the features of the actual injection are captured in the test problem, including the thickness of the overall Utsira Formation at the injection site, the CO₂ injection rate (1,000,000 tonnes per year), the permeability of the sand layers in the Utsira, and the approximate pressure of the Utsira. In order to make a tractable problem for comparison of the various codes, however, some simplifications of the real situation at Sleipner have been made, the most important of which is the assumption of isothermal conditions (37 °C). Injection of the supercritical CO₂, which is less dense than the saline formation waters of the Utsira, causes it to rise through the formation. Its rate of ascent, however, is limited by the presence of four relatively low permeability shales included in the simulation, the presence of which are suggested by seismic profiling of the CO₂ plume at the Sleipner field. The top and bottom of the Utsira Formation are assumed to be impermeable. The only reactive chemistry considered in this problem is the dissolution of CO₂ in the aqueous phase. Problem specifications are given in appendix G. All numerical and mesh specifications were left to the users. It was determined that a 5% difference in results between final modeling results for the test case is acceptable.

7.2 Results

A large “bubble” of supercritical CO₂ forms in the aquifer as the result of injection over the course of two years (Figure 7.1). The ascent of the CO₂ is impeded by the presence of four relatively low permeability shale horizons, which also cause the plume to spread laterally. The simulations predict some slight overpressuring of the formation, with pressures rising from 11 MPa (110 bars) at the injection well before the start of injection to about 12.6 MPa (126 bars) after two years of injection (Figure 7.2). Predictions of the amount of CO₂ “sequestered” in the aqueous phase vary between the different codes from about 21% to 31% (see Table 7.1).

⁷ proposed by Carl Steefel; e-mail: steefell@llnl.gov

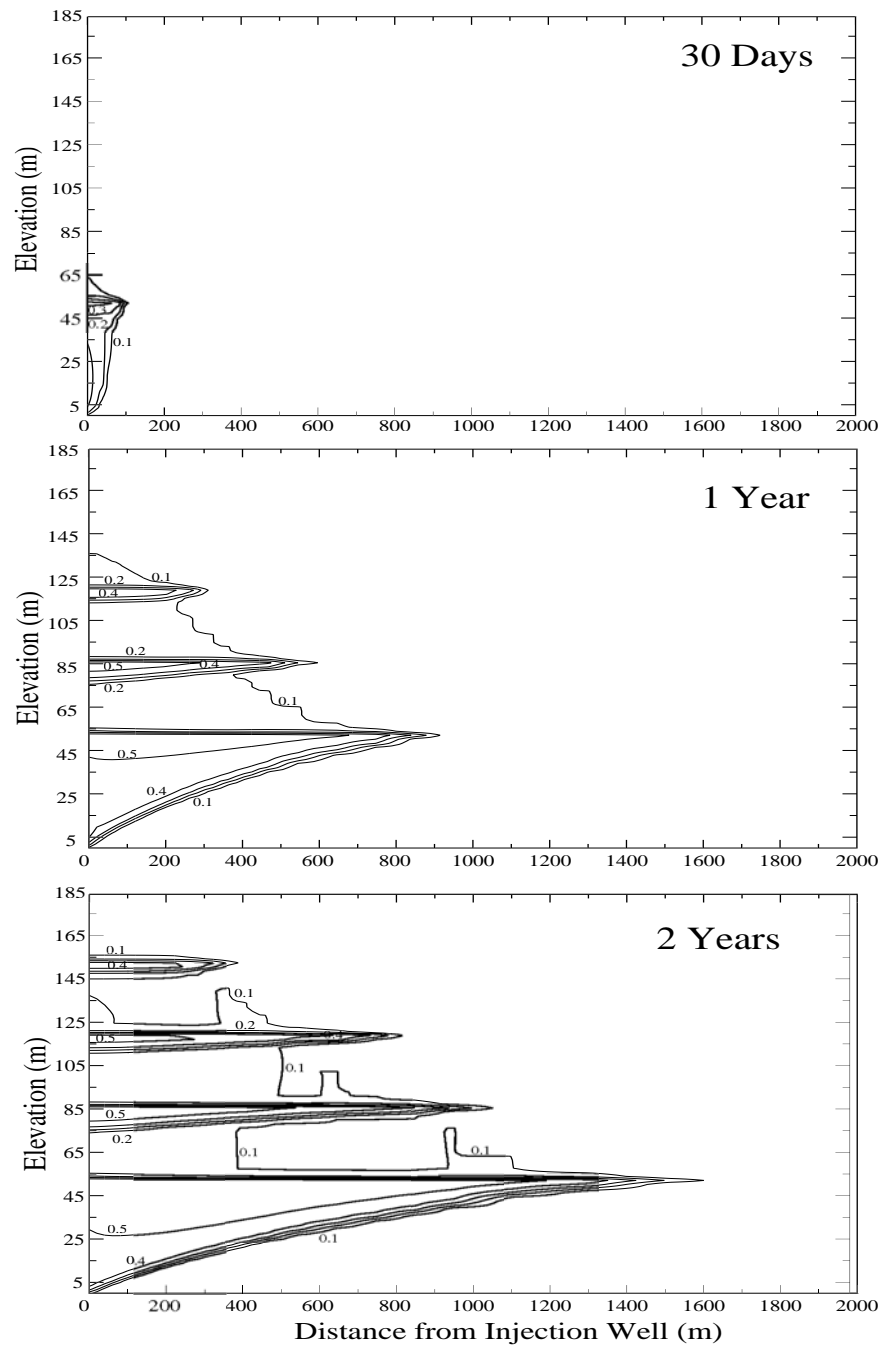


Figure 7.1 Supercritical CO₂ phase saturation as a function of time in Problem 7.

Table 7.1 Comparison of CO₂ mass balances (in units of kg) and “sequestration efficiency” after 2 years of injection.

Code	Total CO ₂	CO ₂ injected	Aqueous CO ₂	Supercritical CO ₂	Fraction CO ₂ in Aqueous
NUFT	9.991x10 ⁶	1x10 ⁷	3.085x10 ⁶	6.906x10 ⁶	0.309
TOUGH2	9.999x10 ⁶	1x10 ⁷	2.149x10 ⁶	7.849x10 ⁶	0.215

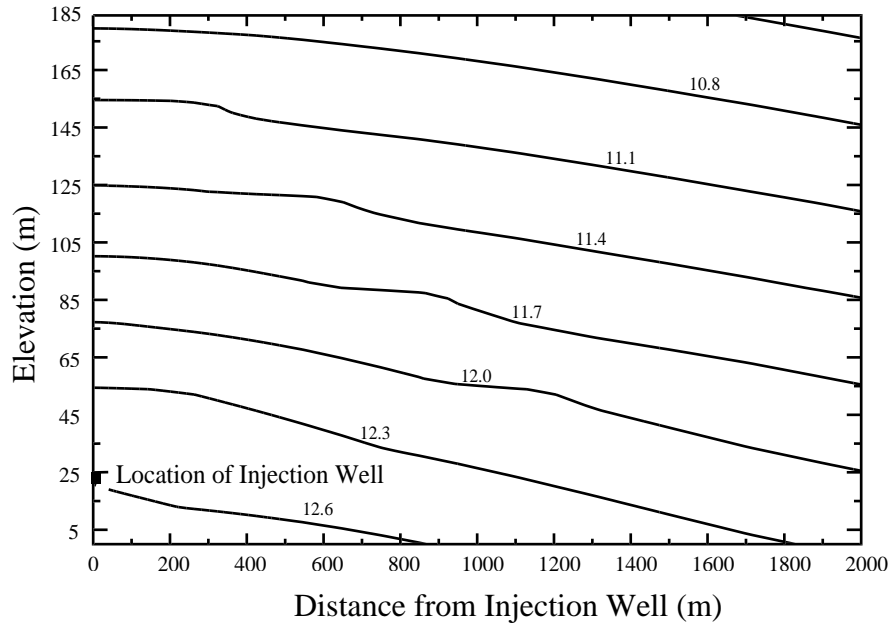


Figure 7.2 Pressure distribution after two years of CO₂ injection.

In evaluating the results from the multiphase flow codes, probably the most unambiguous comparison is provided by time history plots of the amount of CO₂ in the various horizons within the formation. Figure 7.3 compares the total amount of CO₂ (aqueous and supercritical fluid) in the five different sands within the formation as a function of time. Sand 1 is the lowest in the formation and contains the injection well, Sand 5 is the highest. Results are presented for the LBNL (TOUGH2), LLNL (NUFT), and CSIRO multiphase flow codes for the case of a saline pore water (3.2 wt % NaCl). In Sand 1, the agreement is excellent between the three codes. The discrepancy between NUFT and the other two codes worsens as successively higher sands within the formation are considered, but this is primarily the result of the use of too large an initial CO₂ concentration in the case of the NUFT runs (compare the masses of CO₂ in the topmost sand at 30 days). This difference is magnified when smaller total CO₂ masses are considered, as is the case in Sand 5.

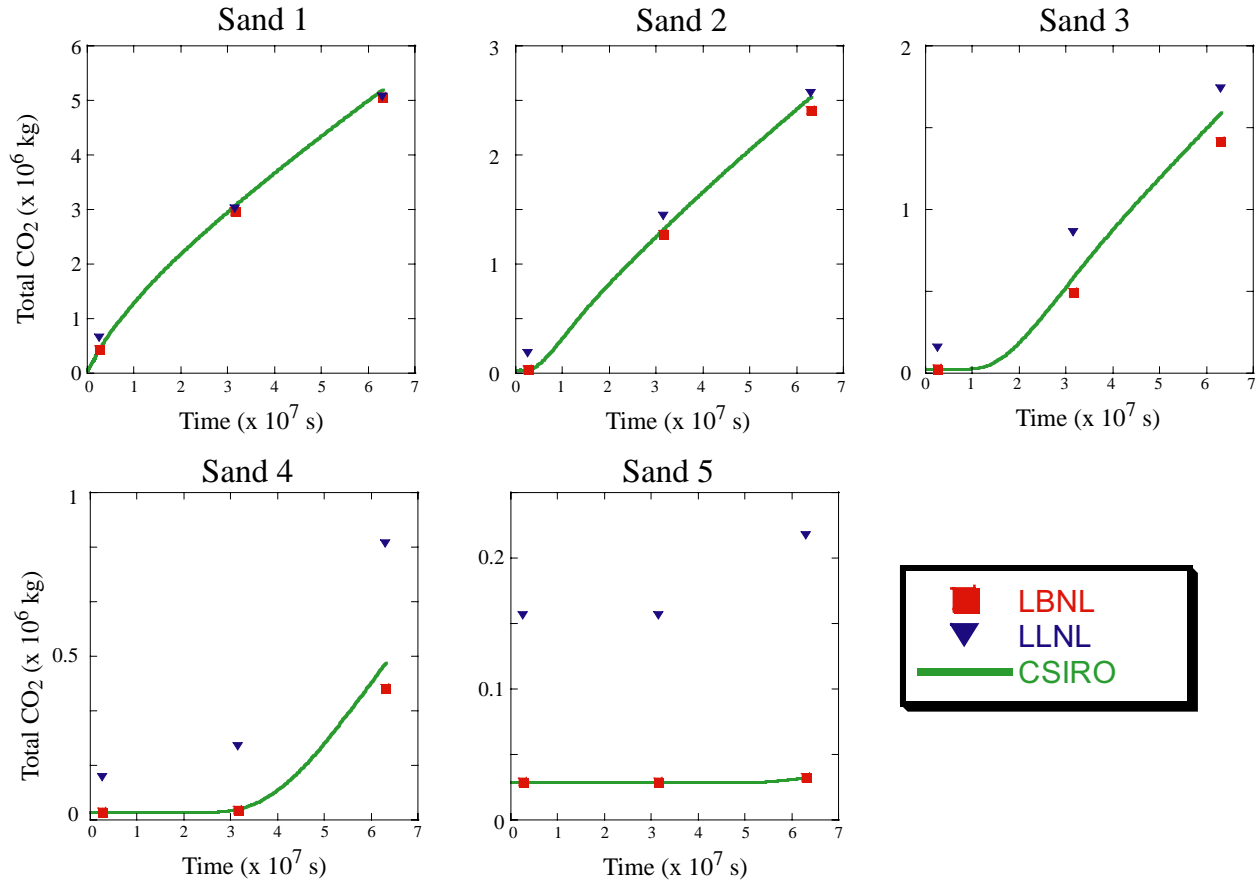


Figure 7.3 Time histories of total CO₂ for the various sands within the formation. Sand 1 is the lowest sand in the formation, Sand 5 the highest. The discrepancy in total CO₂ apparent in Sands 4 and 5 is primarily the result of the use of a higher initial concentration of CO₂ in the aqueous phase in the case of LLNL.

Another difference between the NUFT results and both TOUGH2 and the CSIRO codes, however, is apparent in the time history for Sand 4 (Figure 7.3). The discrepancy becomes slightly larger with time due to the use of a lower Henry's Law coefficient for CO₂ in the case of NUFT, thus resulting in slightly higher partitioning of CO₂ into the aqueous phase. This is also apparent in the total mass balances of CO₂ in the aqueous and supercritical phases (which provide a measure of the "sequestration efficiency") calculated by TOUGH2 and NUFT, with NUFT predicting almost 31 % of the total CO₂ injected being partitioned into the aqueous phase while TOUGH2 predicts about 21%.

Comparisons between the saline and "fresh" pore water cases indicate only very small differences in the results. Since a larger group carried out the fresh pore water simulations, only these will be considered further here. Figure 7.4 shows vertical profiles of the CO₂ supercritical

phase distribution as a function of time at a horizontal distance of 10 meters from the injection well. At 30 days and 2 years, all of the codes predict the position of the leading edge of the CO₂ bubble within about 5% or less. At 1 year, the discrepancy is slightly larger, with the MUFTE_UG code (University of Stuttgart, Germany) and NUFT predicting the CO₂ bubble to have risen about 20 to 30 meters past the position predicted by the other codes. Spatial snapshots of this kind, however, can be somewhat deceptive, since a slightly earlier breakthrough through a low permeability shale unit can result in significant spatial separation as the CO₂ bubble then moves through the high permeability sand. Some of the discrepancy may also be due to the slightly lower pressure used in the MUFTE_UG runs which is traceable to a lack of clarity in the original problem formulation on the part of the problem organizer (Figure 7.5). The use of slightly different pressure boundary conditions results in about 4 to 5 bars lower pressure in the case of the MUFTE_UG results, which in turn results in slightly lower densities for the CO₂ phase. This slightly lower CO₂ density may account for the slightly faster rate of ascent of the CO₂ bubble. A higher buoyancy for the CO₂ bubble in the MUFTE_UG and perhaps in the IFP case may also account for less lateral spreading of the CO₂ plume that is apparent after 1 year of injection (Figure 7.6).

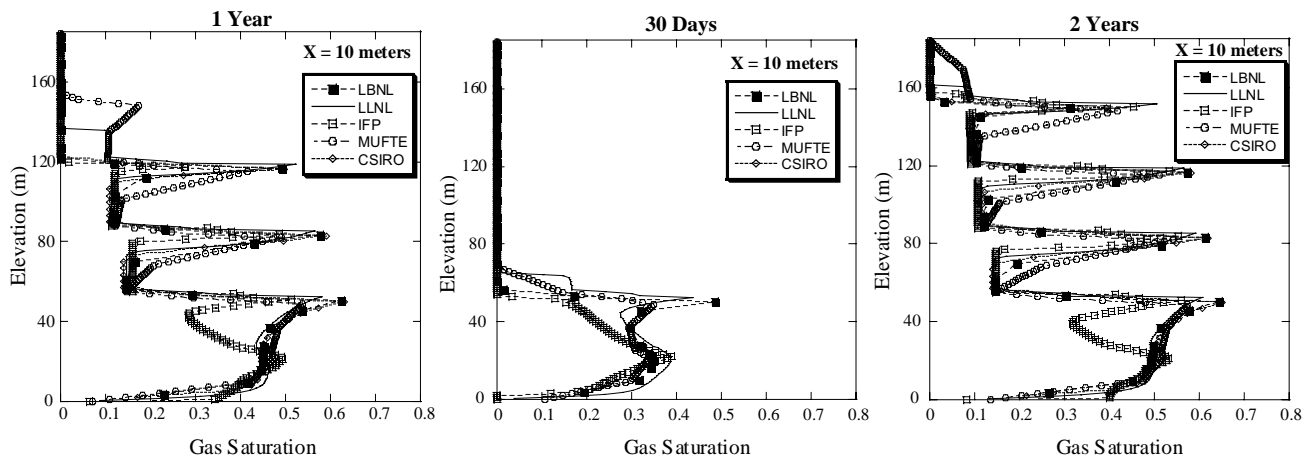


Figure 7.4 Vertical profiles of CO₂ phase saturation at a horizontal distance of 10 meters from the injection well.

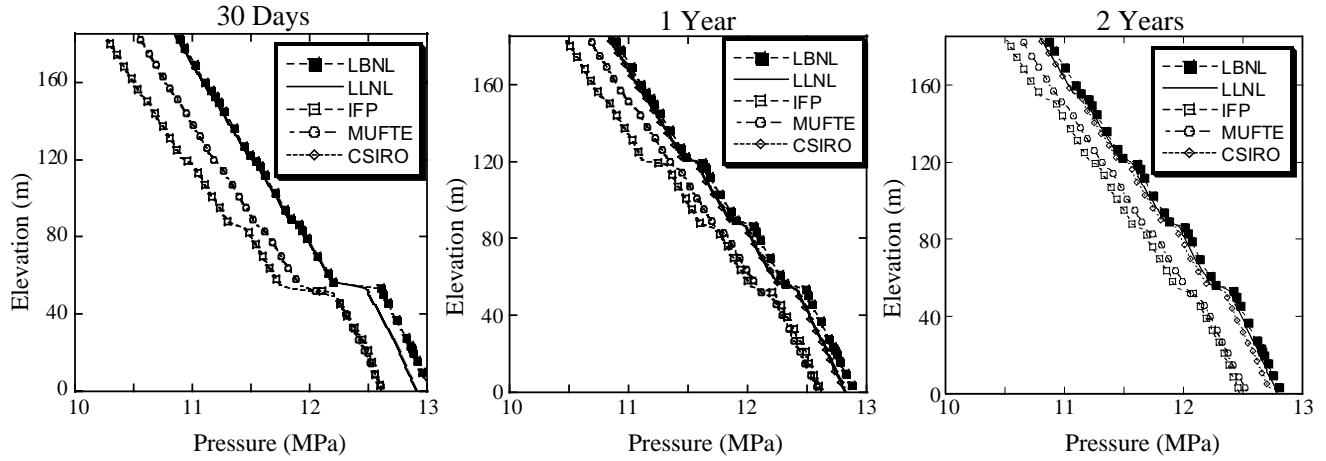


Figure 7.5 Pressure distributions at a horizontal distance of 10 meters from the injection well.

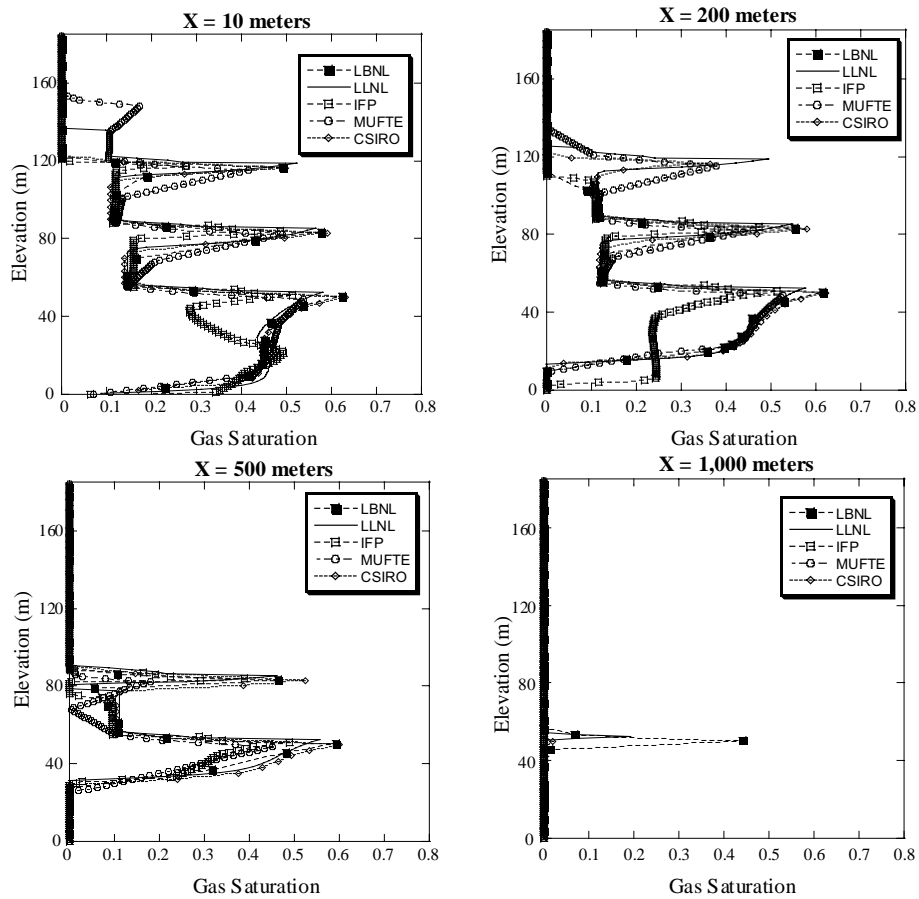


Figure 7.6 Vertical profiles of CO_2 phase saturations after 1 year of injection at various horizontal distances from the injection well.

This same feature, however, is not really apparent after 2 years of injection, with all of the codes giving very similar results (Figure 7.7). Any differences in the CO₂ phase saturation apparent in Figures 7.3 through 7.7 cannot be attributed to the use of differing equations of state. Densities and viscosities of the CO₂ phase as a function of pressure (at the ambient temperature of 37°C) used by the various codes are very similar (Figure 7.8).

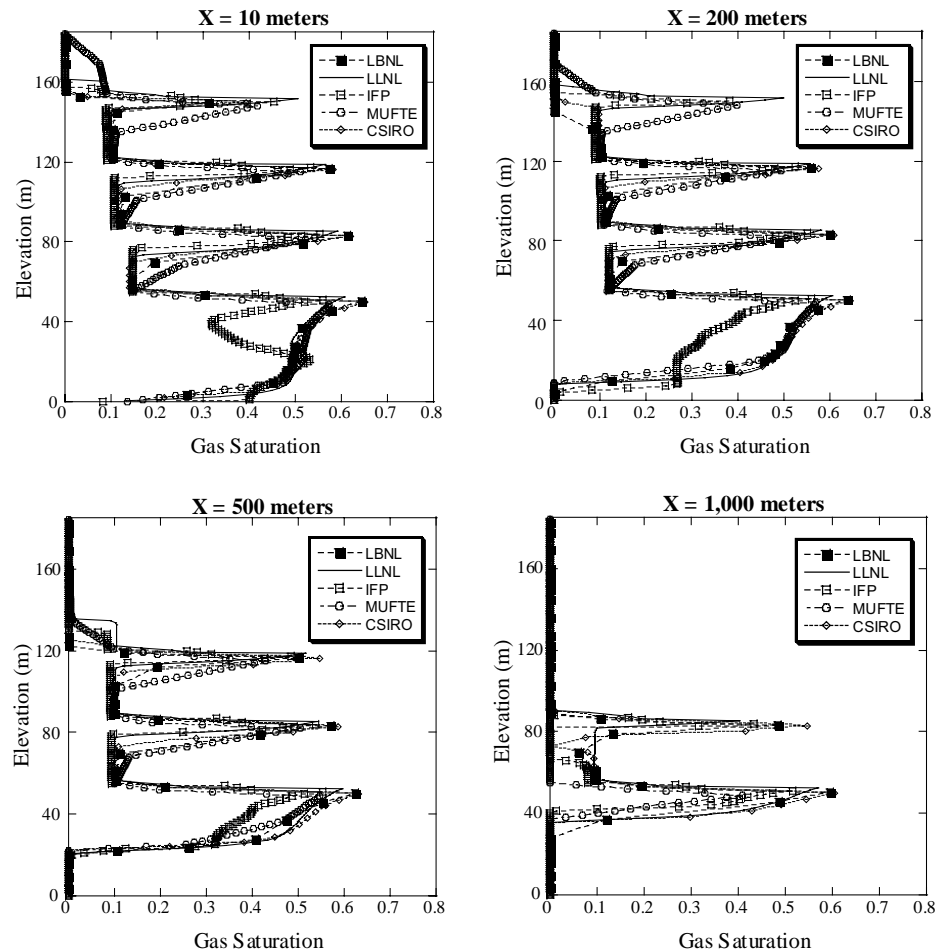


Figure 7.7 Vertical profiles of CO₂ phase saturations after 2 years of injection at various horizontal distances from the injection well.

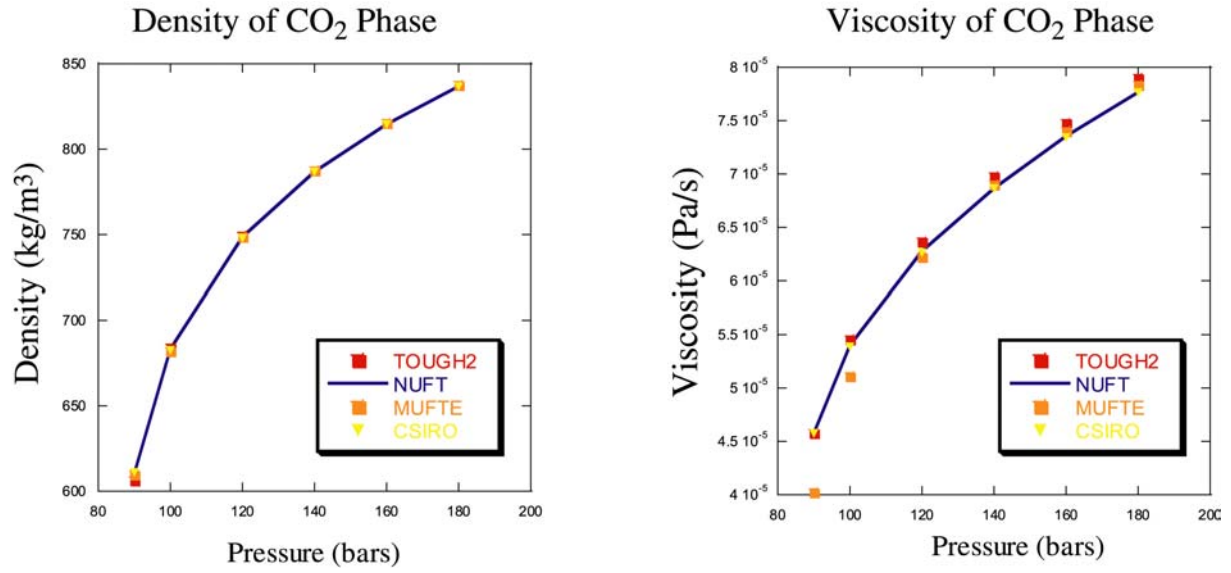


Figure 7.8 Density and viscosity of the supercritical CO₂ phase at 37°C as a function of pressure used by the various codes applied to Problem 7.

8. Test Problem 8. CO₂-Oil Displacement and Phase Behavior¹

8.1 Problem Description

This problem examines our ability to predict the interplay of CO₂-oil phase behavior with multiphase flow. CO₂ is injected into an oil-containing medium under two different conditions leading to immiscible and miscible displacement. Numerical exercises study the representation of multiphase flow, the description of miscibility and phase behavior in the presence of CO₂, the formulation of constitutive relations (such as density, viscosity, and CO₂ solubility), and the degree of dispersion in numerical solutions.

The problem is posed in a one-dimensional geometry so that direct comparison can be made to analytical solutions available for the CO₂-oil flow problem (Monroe *et al.* 1990, Orr *et al.* 1993). These solutions do not include the effects of capillary and hydrodynamic dispersion, but the effect of volume change on mixing is computed. Input data consist of oil composition, injection composition, and multiphase flow properties, see Appendix H.

8.2 Results

Solutions obtained were generated: (1) analytically, (2) by Stanford University (SU) using a research finite-difference simulator, (3) by Alberta Research Council (ARC) via the commercial code GEM (CMG, 2001), and (4) by Los Alamos National Laboratory (LANL) using the commercial code ECLIPSE 300 (Schlumberger, 2001). The research simulator is based on a fully-explicit formulation, whereas GEM and ECLIPSE 300 are finite-difference simulators with variable implicitness and automatic time stepping. GEM and ECLIPSE simulations were run with 5000 and 50 grid blocks, respectively, in the fully implicit mode.

Gas or vapor saturation, S_g , and the total mole fraction composition, z_i , of each component along the one-dimensional medium were requested. For consistency and to obtain a dimensionless formulation, the abscissa is plotted as x_D/t_D where the dimensionless distance, x_D , is defined as x/L , the dimensionless time, t_D , is $q_{inj}t/\phi AL$, and A is the cross-sectional area of the medium.

Case (1) represents immiscible injection of CO₂. Results are summarized in Fig. 8.1. The solid line marked "MOC" denotes the analytical solution obtained by the method of characteristics. The other lines are labeled by participant: SU, ARC, and LANL. Figure 8.1 demonstrates that all results track well, generally, the position of the gas saturation front. Nevertheless all numerical

¹ proposed by Tony Kavscek; email: kavscek@pangea.stanford.edu

solutions display dispersion. Both the research code and GEM were run with 5000 grid blocks and these solutions still display dispersion. The research code displays less dispersion because time stepping occurs in a fully-explicit fashion. The research code run with 100 grid blocks, labeled "SU 100", and ECLIPSE 300 run with 50 grid blocks examine the effect of discretization on dispersion. As the results in Fig. 8.1 demonstrate, resolution decreases with the number of grid blocks.

Similarly, Fig. 8.1 shows that the numerical solutions track the position and shape of the profiles of each component with accuracy that increases as the number of grid blocks increases. The interplay of phase behavior and two-phase flow causes chromatographic separation of the components. The components present in the oil form banks and waves that are ordered according to their equilibrium K values. Methane is the most volatile component, as characterized by its K -value. Hence, the leading bank contains all of the methane. Decane is the least volatile component and so it traverses the system most slowly. Again, a substantial number of grid blocks are required to overcome the effects of numerical dispersion. Examine the composition profile for methane. The hydrocarbon bank just downstream of the vapor saturation front at x_D/t_D of roughly 0.9 is almost entirely methane. GEM nearly reproduces the shape of the methane bank although bank position is somewhat farther downstream than the analytical solution. As the number of grid blocks decreases in the respective simulations, resolution of this bank decreases.

In Case (2), injection of CO_2 occurs under a near-miscible condition. Comparison of the analytical solutions in Figs. 8.1 and 8.2 indicates that the leading shock moves more slowly at high pressure, whereas the trailing shocks accelerate. Thus, the two-phase flow region is compressed, as indicated by Fig. 8.2. If the pressure were increased to 12.1 MPa, the system would indeed be multicontact miscible and all saturation shocks would merge resulting in piston-like displacement. Again the numerical solutions approximate the analytical solution with accuracy that decreases in proportion to the number of grid blocks. Figure 8.2 illustrates an interesting counterpoint regarding dispersion in miscible and immiscible finite difference simulations. The position of the leading vapor saturation shock is retarded by the effects of numerical dispersion. The profile for CO_2 concentration in Fig. 8.2 is significantly smeared by the 100 grid block research code, labeled SU 100, and ECLIPSE 300 simulations, labeled LANL. The smearing delays the accumulation of sufficient CO_2 to cause a phase transition

The challenge for any numerical reservoir simulator that incorporates multiphase flow and phase behavior is to track accurately the path that a displacement follows in composition space. Figure 8.3 illustrates this point graphically for Case (1). Such a diagram is used to illustrate the equilibrium phase behavior and/or the route through composition space that a solution follows. The

points labeled "oil" and "gas" represent the initial oil composition and the injected gas composition, respectively. In Figure 8.3, each vertex of the pyramid indicates 100% of a particular component. The figure shows the composition path obtained from the analytical result, dashed line, as well as that predicted by the research finite-difference code, solid line. As the number of grid blocks becomes fewer, the route followed by a finite difference simulation approaches a straight line connecting the oil and gas compositions. This straight line is sometimes referred to as the dilution line. Figure 8.3 also shows quite well that the effects of dispersion as a function of grid resolution are more pronounced for solutions that are farther, in space or time, from the injection point. More thorough discussions of the relationship between phase behavior, finite-difference simulation, and dispersion are available in the literature (Walsh and Orr, 1990; Jessen et al., 2002).

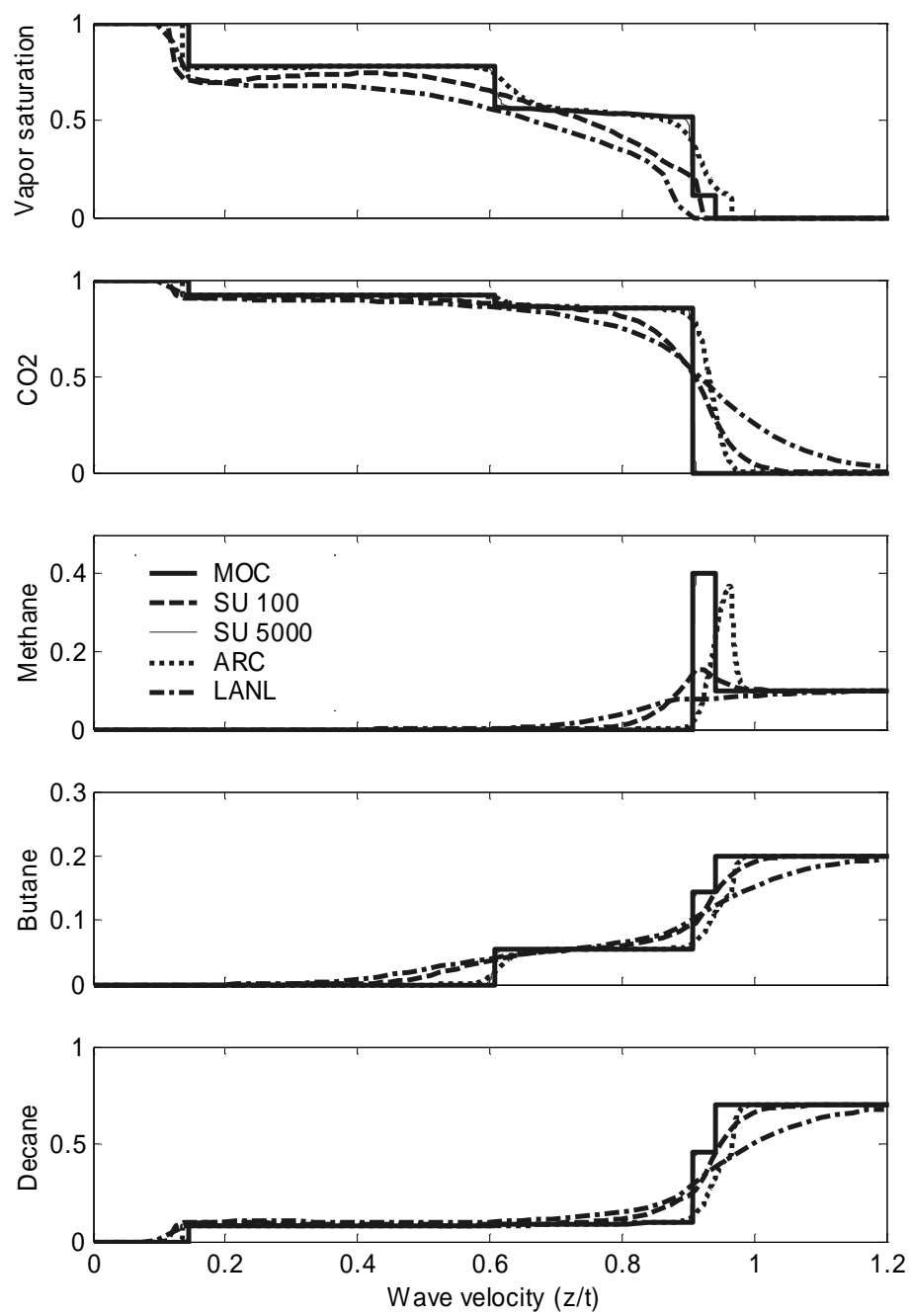


Figure 8.1 Comparison of simulation results at 11 MPa, case (1).

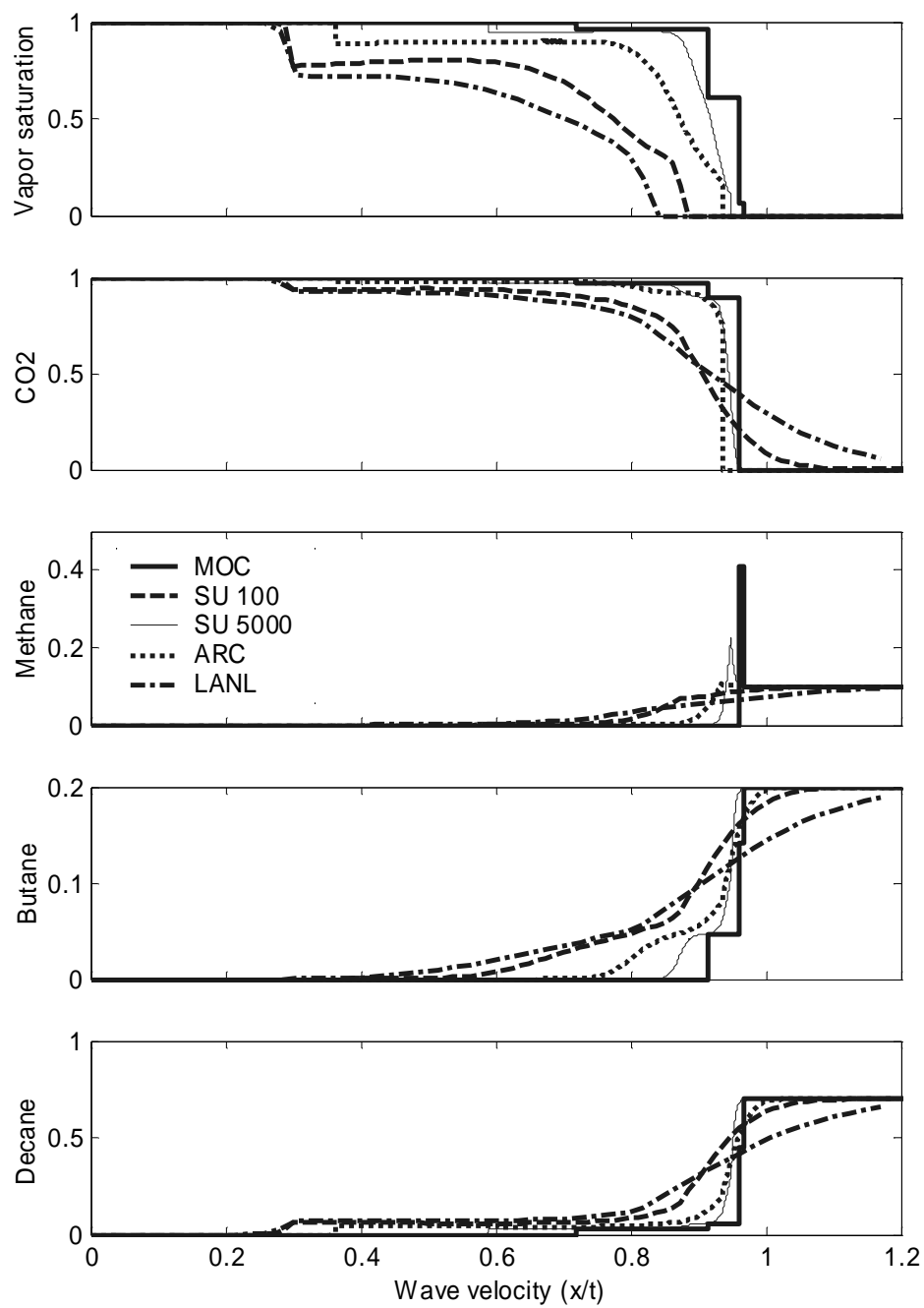


Figure 8.2 Comparison of simulation results at 12 MPa, case (2).

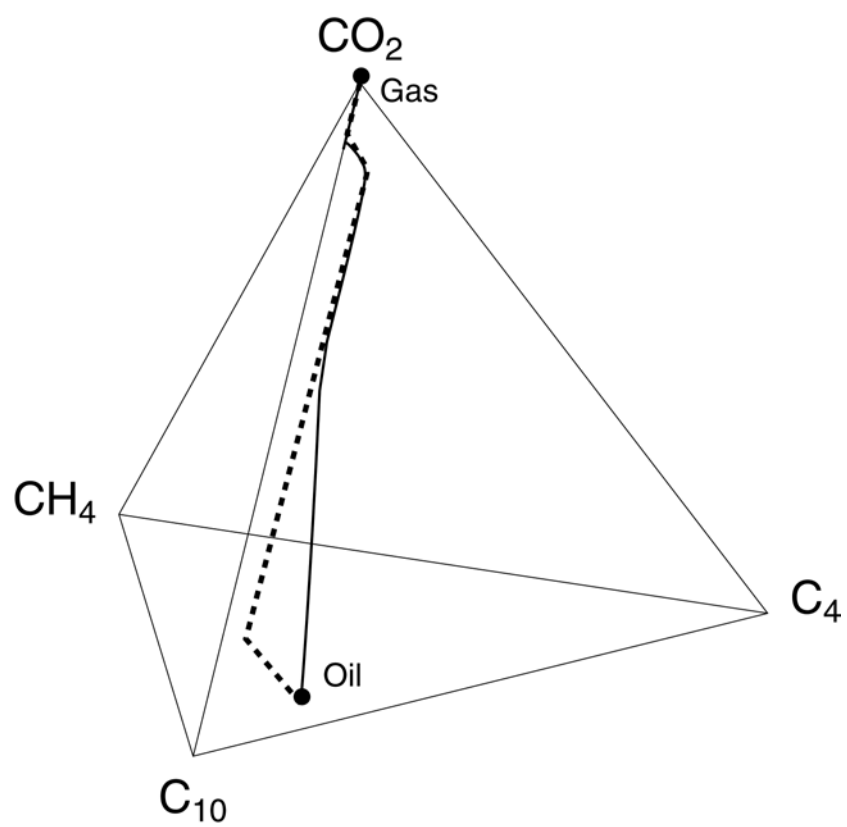


Figure 8.3 Solution route in composition space. Analytical solution (broken line) and FD 100 simulation results.

9. Concluding Remarks

The study reported here has documented the capabilities of currently available numerical simulation codes to represent physical and chemical processes that would accompany CO₂ disposal into geologic formations, including oil and gas reservoirs, and brine aquifers. Codes from ten participating groups have been exercised on a series of eight test problems that probed advective and diffusive mass transport in multiphase conditions, with partitioning of CO₂ between gas and aqueous phases; two problems also involved solid minerals and oil phases, respectively. In the course of the study a number of bugs were found and corrected in several simulation codes. Substantial agreement was found between results predicted from different simulators, but there are also areas with only fair agreement, as well as some significant discrepancies. Most disagreements could be traced to differences in fluid property descriptions, and this clearly is an area that will require continuing efforts by code developers to assure that realistic results can be obtained. Some disagreements are due to effects from space and time discretization, while in some cases discrepancies were noted for which no rational explanation could be found. Although code development work undoubtedly must continue, this work has shown that codes are available now that can model the complex phenomena accompanying geologic storage of CO₂ in a robust manner, and with quantitatively similar results.

It should be noted that the test problems studied here, although prototypical for field problems, make many simplifications and approximations that should be overcome in future work. Subsurface reservoirs generally have complex heterogeneity on different scales, flows are three-dimensional, and are coupled to geochemical and geomechanical effects. Non-isothermal phenomena may also come into play, and a broad range of time scales is of interest in connection with geologic sequestration. It is hoped that future code intercomparisons will address coupled processes in fully three-dimensional heterogeneous media, constrained by actual field observations.

Acknowledgement

This work was supported as part of the GeoSeq project by the National Energy Technology Laboratory (NETL) of the U.S. Department of Energy under Contract No. DE-AC03-76SF00098. We thank Andreas Bielinski, Jonathan Ennis-King, Yann Le Gallo, Kristian Jessen, David H.-S. Law, Peter Lichtner, Rajesh Pawar, Bryan Travis, Steve White and Mark White for participating in this study and submitting results. Nic Spycher (LBNL) provided the reference solubility values in Tables 2.1 and 2.2. For assistance and reviews of parts of the manuscript we thank Peter Sammon, Mohamed Hassam, Y. Wang, and J. Zhu. We are grateful to Sally Benson for her review of the manuscript and valuable suggestions.

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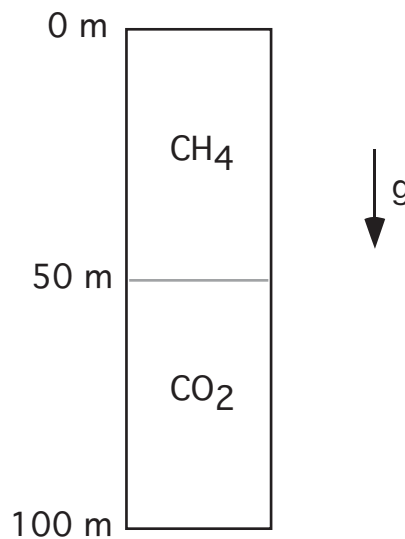
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Appendix: Specifications of Test Problems

APPENDIX A. Test Problem 1: Mixing of Stably Stratified Gases[#]

1. INTRODUCTION AND GENERAL DESCRIPTION

In this problem, CO₂ and CH₄ gases are placed in contact one on top of the other and allowed to mix as controlled by diffusion and associated flow at 40 bars, 40 °C. Mixing in the system is limited because the denser gas (CO₂) is on the bottom and the lighter gas (CH₄) is on the top. The diffusion and flow are assumed to be one-dimensional. A residual liquid water saturation of 0.1 exists within the pores.



2. LIST OF PROCESSES BEING STUDIED

Molecular diffusion.

Density, viscosity, and solubility formulations of water, CO₂, and CH₄ as functions of pressure, temperature, and composition (P, T, X).

Advection in response to pressure gradients induced by equimolar diffusion of species with different molecular weights.

3. DEFINITION OF THE PROBLEM AND INPUT DATA

Boundary conditions:

No heat or mass flux through any boundaries (i.e., all boundaries are no-flow).

[#] proposed by Curt Oldenburg; e-mail: CMOldenburg@lbl.gov

Initial conditions:

T = 40 °C (isothermal throughout)

P (Z = 0 m) = 40 bars

X initially stratified with CO₂ occupying the bottom half of the domain and CH₄ occupying the top half.

Input data:

- a) Porosity, tortuosity, residual liquid saturation (0.1, 1., 0.1, respectively)
- b) Molecular diffusivity ($1 \times 10^{-7} \text{ m}^2 \text{ s}^{-1}$)
- c) Permeability and relative permeability ($k = 10^{-14} \text{ m}^2$, linear k_{rg} , liquid immobile)
- d) Density, viscosity, and solubility in water of CO₂ and CH₄ as functions of P, T, and X.
- e) Vapor-liquid equilibrium properties of water.

4. PROBLEM VARIATIONS

- a) Diffusion only with no gas-phase flow.
- b) Low pressure scenario (P = 1 bar).
- c) High pressure scenario (P = 100 bar)
- d) Mixing by Dusty Gas Model instead of advective-diffusive Fickian model.

5. DEFINITION OF RESULTS TO BE CALCULATED

Vertical profiles at various times of :

- a) CO₂ and CH₄ masses in liquid and gas phases per unit volume.
- b) Pressure.
- c) Density of the gas mixture.

6. COMPARISON CRITERIA

Profiles at the same times should match within 5%.

7. REFERENCES

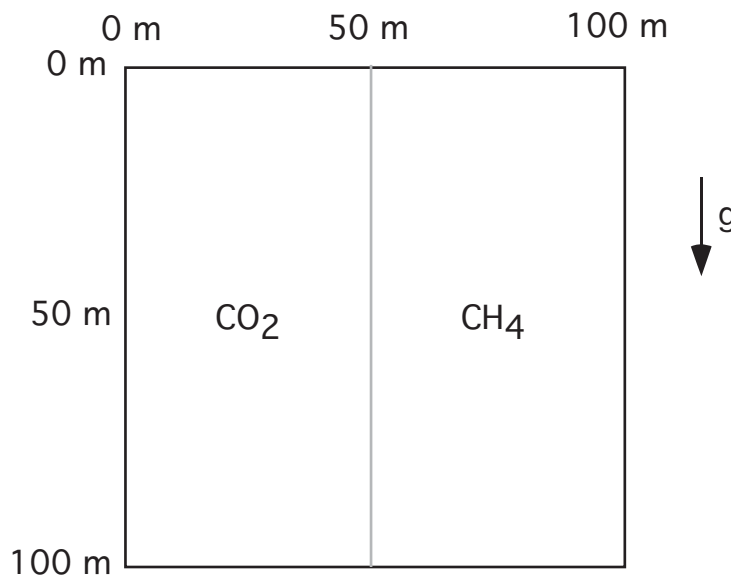
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APPENDIX B. Test Problem 2: Advective-Diffusive Mixing Due to Lateral Density Gradient[#]

1. INTRODUCTION AND GENERAL DESCRIPTION

In this problem, CO₂ and CH₄ gases are placed side-by-side in a container and allowed to mix by advection and diffusion. The strong lateral density gradient between the dense CO₂ gas and the relatively light CH₄ gas causes a strong flow where CO₂ tends to move downward and CH₄ tends to move upward to the top of the container. The flow and diffusion are assumed to be two-dimensional. A residual liquid water saturation of 0.1 exists within the pores.



2. LIST OF PROCESSES BEING STUDIED

Gravity-driven advection in response to strong lateral density gradient.

Molecular diffusion.

Density, viscosity, and solubility formulations as functions of pressure, temperature, and composition (P, T, X).

Because of the strong advection, numerical dispersion will arise for most numerical methods.

3. DEFINITION OF THE PROBLEM AND INPUT DATA

Boundary conditions:

No heat or mass flux through any boundaries (i.e., all boundaries are no-flow).

[#] proposed by Curt Oldenburg; e-mail: CMOldenburg@lbl.gov

Initial conditions:

$T = 40\text{ }^{\circ}\text{C}$ (isothermal throughout)

$P(Z = 0\text{ m}) = 40\text{ bars}$

Initial composition field with CO_2 on the left-hand half of the domain and CH_4 on the right-hand half of the domain.

Input data:

- a) Porosity, tortuosity, liquid saturation (0.1, 1., 0.1, respectively)
- b) Molecular diffusivity ($1 \times 10^{-7}\text{ m}^2\text{ s}^{-1}$)
- c) Permeability and relative permeability ($k = 10^{-14}\text{ m}^2$, linear k_{rg} , liquid immobile)
- d) Density, viscosity, and solubility in water of CO_2 and CH_4 as functions of P , T , and X .
- e) Vapor-liquid equilibrium properties of water.

4. PROBLEM VARIATIONS

- a) Low pressure scenario ($P = 1\text{ bar}$).
- b) High pressure scenario ($P = 100\text{ bar}$).
- c) Mixing by Dusty Gas Model instead of advective-diffusive Fickian model.
- d) Substitute nitrogen (N_2) or air for CO_2 .

5. DEFINITION OF RESULTS TO BE CALCULATED

Horizontal profiles at $Z = 50\text{ m}$ at various times of

- a) CO_2 and CH_4 masses in gas and liquid phases per unit volume.
- b) Density of the gas mixture.

6. COMPARISON CRITERIA

Profiles at the same times should match within 5%.

7. REFERENCES

To be supplied.

APPENDIX C. Test Problem 3: Radial Flow from a CO₂ Injection Well[&]

1. INTRODUCTION AND GENERAL DESCRIPTION

This problem addresses two-phase flow of CO₂ and water for simplified flow geometry and medium properties. The aquifer into which injection is made is assumed infinite-acting, homogeneous, and isotropic. Gravity and inertial effects are neglected, injection is made at a constant mass rate, and flow is assumed 1-D radial (line source). Under the conditions stated the problem has a similarity solution where dependence on radial distance R and time t occurs only through the similarity variable $\xi = R^2/t$ (O'Sullivan 1981; Doughty and Pruess 1992).

2. LIST OF PROCESSES BEING STUDIED

Two-phase flow of CO₂ and water subject to relative permeability and capillary effects.
Change of fluid density, viscosity, and CO₂ solubility with pressure and salinity.
Formation dry-out with precipitation of salt.

3. DEFINITION OF THE PROBLEM AND INPUT DATA

Problem parameters are summarized in Tables C.1 and C.2

4. PROBLEM VARIATIONS

Neglect salinity of the aqueous phase. Include non-isothermal effects. Include permeability changes due to precipitation. Inject gas that is 50 % CO₂, 50 % N₂.

5. DEFINITION OF RESULTS TO BE CALCULATED

Data on CO₂ and brine density and viscosity, and CO₂ solubility, for the range of thermodynamic conditions encountered in the problem. Gas saturation, dissolved CO₂ mass fraction, fraction of void space containing precipitated salt, and fluid pressure as functions of the similarity variable $\xi = R^2/t$. (Use both profiles at constant time and time-series data at a specific location for plotting.)

6. COMPARISON CRITERIA

Results should match within +/- 5 %.

7. REFERENCES

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[&] proposed by Karsten Pruess; e-mail: K_Pruess@lbl.gov

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Table C.1 Hydrogeologic parameters.

Permeability	$k = 10^{-13} \text{ m}^2$
Porosity	$\phi = 0.12$
Pore compressibility	$c = 4.5 \times 10^{-10} \text{ Pa}^{-1}$
Aquifer thickness	100 m
Relative permeability	
liquid: van Genuchten function (1980)	
$k_{rl} = \sqrt{S^*} \left\{ 1 - \left(1 - [S^*]^{1/\lambda} \right)^\lambda \right\}^2$	$S^* = (S_l - S_{lr}) / (1 - S_{lr})$
irreducible water saturation exponent	$S_{lr} = 0.30$ $\lambda = 0.457$
gas: Corey curve (1954)	
$k_{rg} = (1 - \hat{S})^2 (1 - \hat{S}^2)$	$\hat{S} = \frac{(S_l - S_{lr})}{(1 - S_{lr} - S_{gr})}$
irreducible gas saturation	$S_{gr} = 0.05$
Capillary pressure	
van Genuchten function (1980)	
$P_{cap} = -P_0 \left([S^*]^{-1/\lambda} - 1 \right)^{1-\lambda}$	$S^* = (S_l - S_{lr}) / (1 - S_{lr})$
irreducible water saturation exponent	$S_{lr} = 0.0$
strength coefficient	$\lambda = 0.457$ $P_0 = 19.61 \text{ kPa}$

Table C.2 Initial conditions and injection specifications

Pressure	120 bar
Temperature	45 °C
Salinity	15 wt.-% NaCl
CO2 injection rate	100 kg/s

APPENDIX D. Test Problem 4: CO₂ Discharge Along a Fault Zone[&]

1. INTRODUCTION AND GENERAL DESCRIPTION

This problem explores CO₂ loss from storage through a leaky fault, using a highly simplified 1-D linear flow geometry. It is envisioned that an aquifer into which CO₂ disposal is made is intersected by a vertical fault, which establishes a connection through an otherwise impermeable caprock to another aquifer 500 m above the storage aquifer (Fig. D.1a). This situation is idealized by assuming 1-D flow geometry and constant pressure boundary conditions as shown in Fig. D.1b (Pruess and García, 2002a).

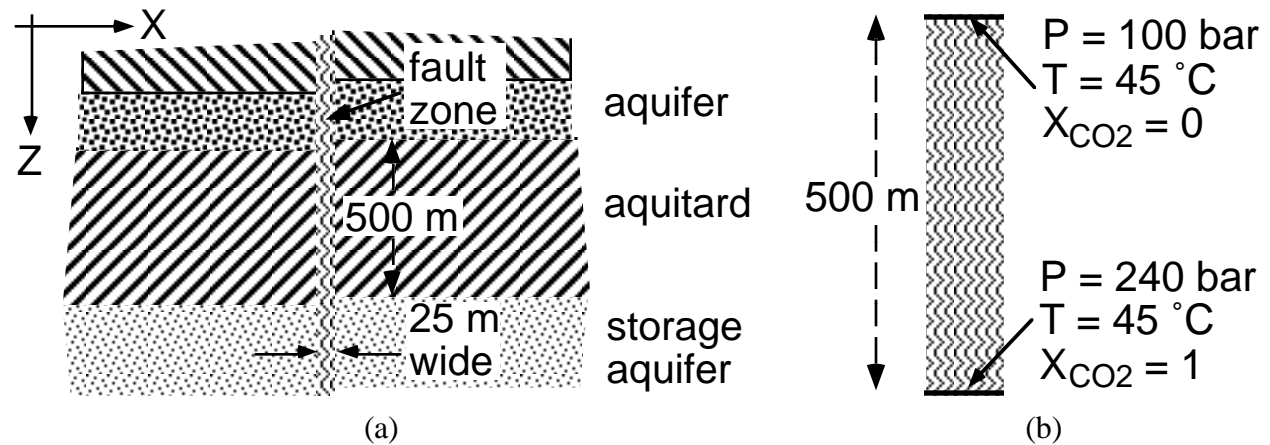


Figure D.1 Schematic of the fault zone model (a) and applied boundary conditions (b).

2. LIST OF PROCESSES BEING STUDIED

Immiscible displacement of water by CO₂ subject to pressure, gravity, and capillary pressure effects.

Change of fluid density, viscosity, and CO₂ solubility with pressure.

Formation dry-out.

3. DEFINITION OF THE PROBLEM AND INPUT DATA

Hydrogeologic parameters are identical to those of problem 3 (Table C.1), except that porosity is increased to 35 %. The fault zone is assumed to be 25 m wide and 500 m tall, with boundary conditions as given in Fig. D.1b. The reservoir fluid is assumed to be pure water (no salinity). Initial conditions are pressures in hydrostatic equilibrium relative to P = 100 bar at the top; temperature is held constant at T = 45 °C throughout.

[&] proposed by Karsten Pruess; e-mail: K_Pruess@lbl.gov

4. PROBLEM VARIATIONS

Include salinity of the aqueous phase and permeability changes due to precipitation. Include non-isothermal effects. Assume gas composition is 50 % CO₂, 50 % N₂.

5. DEFINITION OF RESULTS TO BE CALCULATED

Data on CO₂ and water density and viscosity, and CO₂ solubility, for the range of thermodynamic conditions encountered in the problem. Vertical profiles of gas saturation, fluid pressure, and dissolved CO₂ mass fraction at different times. CO₂ inventory in gas and liquid phases after 10⁷ seconds. Mass flow rates of CO₂ at the bottom and of water at the top vs. time (normalized for a 1 m thick section).

6. COMPARISON CRITERIA

Results should match to within +/- 5 %.

7. REFERENCES

Pruess, K. and J. García. Multiphase Flow Dynamics During CO₂ Injection into Saline Aquifers, *Environmental Geology*, Vol. 42, pp. 282 - 295, 2002a.

APPENDIX E. Test Problem 5: Mineral Trapping in a Glauconitic Sandstone Aquifer*

1. INTRODUCTION AND GENERAL DESCRIPTION

This problem addresses geochemical effects of CO₂ injection into a glauconitic sandstone aquifer, and analyzes the impact of CO₂ immobilization through carbonate precipitation. Batch reaction modeling of the geochemical evolution of this aquifer is performed in the presence of CO₂ at high pressure. The problem is based on Gunter et al. (1997), who modeled water-rock reactions when CO₂ is injected into a glauconitic sandstone aquifer in the Alberta Sedimentary Basin, Canada. Additional processes are considered such as presence of organic matter and its oxidation.

2. LIST OF PROCESSES BEING STUDIED

The following processes are considered: (1) equilibrium aqueous complexation, (2) redox processes, (3) the kinetics of chemical interactions between the host rock minerals and the aqueous phase (organic matter dissolution is a non-equilibrium processes), and (4) CO₂ solubility dependence on pressure, temperature and salinity of the system. In addition, changes in porosity are monitored during the simulations.

3. DEFINITION OF THE PROBLEM AND INPUT DATA

The initial condition used in the simulation is a pure 1.0 M solution of sodium chloride reacting with the primary minerals listed in Table E.1 at a temperature of 54 °C, a pH of 7, and an Eh of -0.1 V. Reactant phases are those minerals initially present in the aquifer formation (Table E.1). The reactant minerals dissolve progressively into the formation water, thus modifying the water composition and leading to precipitation of product phases. Two simulations are to be performed with the same initial conditions. The first simulation examines water-rock interaction under natural conditions without CO₂ injection. The second simulation considers a CO₂ injection pressure of 260 bar. The CO₂ gas pressure is assumed to be maintained in equilibrium with the solution at all times. A simulation time of 100,000 years is used for both simulations.

The rate law for kinetic mineral dissolution and precipitation is taken from Lasaga (1984) and Steefel and Lasaga (1994):

$$r_m = A_m k_m \left[1 - \left(\frac{Q_m}{K_m} \right)^\mu \right]^n \quad (\text{E.1})$$

* proposed by Tianfu Xu; e-mail: Tianfu_Xu@lbl.gov

where m is mineral index, r_m is the dissolution/precipitation rate (positive values indicate dissolution, and negative values precipitation), A_m is the specific reactive surface area per kg H_2O , k_m is the rate constant (moles per unit mineral surface area and unit time) which is temperature dependent, K_m is the equilibrium constant for the mineral-water reaction written for the destruction of one mole of mineral m , and Q_m is the ion activity product. The parameters μ and n are taken equal to unity. Rate constant dependency as a function of temperature is

$$k = k_{25} \exp \left[\frac{-E_a}{R} \left(\frac{1}{T} - \frac{1}{298.15} \right) \right] \quad (E.2)$$

where E_a is the activation energy, k_{25} is the rate constant at 25 °C, R is gas constant, T is absolute temperature. The kinetic parameters are also given in Table E.1. Precipitation of possible secondary minerals (Table E.1 with initial $V_f = 0$ where V_f is mineral volume fraction) is represented using the same kinetic rate expression as that for dissolution. The precipitation kinetic constant for a secondary mineral is assumed to be one order of magnitude greater than its corresponding dissolution rate constant. A total surface area of 10 m^2/dm^3 medium was used. The initial surface area of each primary mineral is calculated by multiplying its volume fraction with the total surface area (Table E.1). With time, the surface areas change in complex ways. We simply relate the surface areas of the primary minerals at some time to the mineral volume fraction by

$$A = A^0 \frac{V_f}{V_f^0} \quad (E.3)$$

where A and V_f are the reactive surface area and volume fraction of a primary mineral, respectively, and superscript zero indicates the values at time $t = 0$. The reactive surface areas for secondary minerals are set to 0.25 m^2/dm^3 at all times.

4. PROBLEM VARIATIONS

Neglect CO_2 solubility dependence on pressure, temperature and salinity. The reactive surface areas used for both primary and secondary minerals are uncertain and may be varied. The results also vary with thermodynamic and kinetic data.

5. DEFINITION OF RESULTS TO BE CALCULATED

The following variables are reported vs. time, (1) aqueous species concentrations, (2) pH and Eh, (3) changes of volume fraction of both primary and secondary minerals, (4) change of porosity, (5) the amounts of CO_2 trapped in both liquid and solid phases.

Table E.1. List of initial mineral volume fractions, potential secondary mineral phases, and their kinetic properties. All rate constants are listed for dissolution. The constants for precipitation are increased correspondingly by one order of magnitude.

Mineral	Chemical composition	Volume (%)	Surface area (m ² /dm ³ medium)	k ₂₅ (moles/m ² s)	E _a (kJ/mol)	Reference
<i>Primary:</i>						
quartz	SiO ₂	71.28	7.128	1.2589x10 ⁻¹⁴	87.50	Tester et al. (1994)
K-feldspar	KAlSi ₃ O ₈	1.76	0.176	1.00x10 ⁻¹²	67.83	Blum and Stillings (1995)
kaolinite	Al ₂ Si ₂ O ₅ (OH) ₄	1.76	0.176E2	1.00x10 ⁻¹³	62.76	Nagy (1995)
calcite	CaCO ₃	0.88	0.088	1.60x10 ⁻⁹	41.87	Svensson and Dreybrodt (1992)
dolomite	CaMg(CO ₃) ₂	0.88	0.088	0.60x10 ⁻⁹	41.87	assigned based on calcite
siderite	FeCO ₃	0.88	0.088	0.60x10 ⁻⁹	41.87	assigned based on calcite
illite	K _{0.6} Mg _{0.25} Al _{1.8} (Al _{0.5} Si _{3.5} O ₁₀)(OH) ₂	2.64	0.264E2	1.00x10 ⁻¹⁴	58.62	Knauss and Wolery (1989)
glauconite	K _{1.5} Mg _{0.5} Fe _{2.5} Fe _{0.5} AlSi _{7.5} O ₂₀ (OH) ₂	4.4	0.440E1	1.00x10 ⁻¹⁴	58.62	set to illite
organic	CH ₂ O	2.64	0.264	1.00x10 ⁻¹³	0.0	assigned based on kaolinite
oligoclase	CaNa ₄ Al ₆ Si ₁₄ O ₄₀	0.88	0.088	1.00x10 ⁻¹²	67.83	set to K-feldspar
porosity	-----	12				
total	-----	100				
<i>Secondary:</i>						
albite-low	NaAlSi ₃ O ₈	0.0	0.25	1.00x10 ⁻¹²	67.83	Blum and Stillings (1995)
smectite-Na	Na _{0.29} Mg _{0.26} Al _{1.77} Si _{3.97} O ₁₀ (OH) ₂	0.0	0.25E2	1.00x10 ⁻¹⁴	58.62	set to illite
smectite-Ca	Ca _{0.145} Mg _{0.26} Al _{1.77} Si _{3.97} O ₁₀ (OH) ₂	0.0	0.25E2	1.00x10 ⁻¹⁴	58.62	set to illite

6. COMPARISON CRITERIA

Results should match within +/- 5 %.

7. REFERENCES

- Blum, A. E., and Stillings, L. L., 1995, Feldspar dissolution kinetics, Chapter 7 of chemical weathering rates of silicate minerals, White, A.F., and Brantley, S. L. (eds), *Mineral Society of America*, v. 31, p. 291–351, Washington D. C.
- Gunter W. D., Wiwchar, B., and Perkins, E. H., 1997, Aquifer disposal of CO₂-rich greenhouse gases: extension of the time scale of experiment for CO₂-sequestering reactions by geochemical modeling, *Mineral. and Petrol.*, V. 59, p. 121-140.
- Knauss, K. G., and Wolery, T. J., 1989, Muscovite dissolution kinetics as a function of pH and time at 70°C.” *Geochimica et Cosmochimica Acta*, V. 53, p. 1493–1501.
- Lasaga, A. C., 1984, Chemical kinetics of water-rock interactions, *Journal of Geophysical Research*, v. 89, p. 4009-4025.
- Nagy, K. L., Dissolution and precipitation kinetics of sheet silicates, 1995, *Chemical Weathering Rates of Silicate Minerals*, V. 31, p. 291–351.

- Rudnicki, J. I., and Wawersik, W. R., 1999, Report looks at sequestering CO₂ beneath earth's surface, *EOS, Transactions of American Geophysical Union*, v. 80, No. 50, p. 607-608.
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- Svensson, U. and Dreybrodt, W., 1992. Dissolution kinetics of natural calcite minerals in CO₂-water systems approaching calcite equilibrium." *Chemical Geology*, v. 100, p. 129-145. Amsterdam, The Netherlands, Elsevier Science Publishers.
- Tester, J. W., Worley, G. W., Robinson, B. A., Grigsby, C. O., and Feerer, J. L., 1994, Correlating quartz dissolution kinetics in pure water from 25 to 625 °C., *Geochimica et Cosmochimica Acta*, v. 58, p. 2407-2420.

APPENDIX F. Test Problem 6: Hydromechanical Responses During CO₂ Injection into an Aquifer-Caprock System[%]

1. INTRODUCTION AND GENERAL DESCRIPTION

This problem addresses consequences of rock deformation, including potential change in permeability and porosity, during injection of CO₂ into a porous aquifer beneath a low permeable caprock. The problem is simplified to a one-dimensional vertical column of an aquifer-caprock system (Figure F.1). The injection is conducted at 1500 meters depth at a pre-determined constant pressure. The hydraulic boundary conditions are “no flow” except at the ground surface. As a consequence, the injected gas can only escape the aquifer through the low-permeability caprock. Because the permeability of the caprock is assumed to be stress dependent, the leakage rate will be affected by induced effective stress changes during the CO₂ injection. The test problem is designed to induce substantial porosity and permeability change to emphasize the coupled hydromechanical effects in the code comparison.

2. LIST OF PROCESSES BEING STUDIED

The following processes are considered: (1) injection of CO₂ gas into a fully water saturated aquifer with migration of gas upwards in the vertical column through a low permeability caprock; (2) mechanical stress changes and deformation in the aquifer and caprock as a consequence of changes in pore pressure during injection of CO₂ into the aquifer; and (3) changes in porosity and permeability caused by effective stress changes in both the aquifer and caprock. These processes do not induce any significant temperature changes and the simulation could therefore be conducted in isothermal mode. However, the effects of temperature on thermophysical properties of water and CO₂ should be taken into account.

Changes in the capillary pressure function with changes in porosity can be neglected. We also neglect effects of chemical reactions with minerals and dissolution of CO₂ in water.

3. DEFINITION OF THE PROBLEM AND INPUT DATA

The calculation should be done in two phases. First the pre-injection steady state conditions of stress, fluid pressure and temperature should be established. Thereafter, the actual injection simulation should be conducted.

Initial conditions of static equilibrium should be established in a steady state pre-injection calculation as follows.

[%] proposed by Chin-Fu Tsang and Jonny Rutqvist; e-mail: CFTsang@lbl.gov

- a) Initial isotropic stress field increasing with depth based on the weight of the overlying rock (bulk density = 2260 kg/m^3 and acceleration of gravity = 9.81 m/s^2)
- b) Initial fully saturated rock with a hydrostatic gradient calculated assuming a liquid pressure of $P_1 = 0.1 \text{ MPa}$ at the ground surface. Standard functions for water density (with temperature dependency) should be used.
- c) An initial temperature with a thermal gradient of $30 \text{ }^\circ\text{C/km}$ (assume fixed temperatures of $10 \text{ }^\circ\text{C}$ at the ground surface and $55 \text{ }^\circ\text{C}$ at 1500 meter depth).
- d) An initial porosity and permeability distribution which are dependent on the mean effective stress according to equations in Table F.1. That is, the initial porosity and permeability are decreasing with depth.

After achieving the steady state initial conditions, the injection operation should be simulated by injecting pure CO_2 at 1500 meter depth (at the lower boundary of the model). The injection pressure should be kept constant at 30 MPa (about 90% of the lithostatic pressure at 1500 meter depth) over a time period of 30 years.

Boundary conditions during the injection period:

- a) Mechanical boundary conditions are locked for normal displacements (roller boundaries) on all boundaries except at the ground surface, which is free to move.
- b) Gas pressure is kept constant (30 MPa) at the base of the model and the liquid pressure is kept constant at the ground surface (0.1 MPa).
- c) Temperature is kept constant ($55 \text{ }^\circ\text{C}$) at the base of the model and at the ground surface ($10 \text{ }^\circ\text{C}$).

The problem domain includes two materials:

- 1) a low-permeability caprock, which extends from 1200 to 1300 m depth;
- 2) a rock mass with aquifer properties above and below the caprock.

Both materials are assumed linear elastic, with functions of porosity-stress, permeability-porosity, relative permeability and capillary pressure given in Table F.1.

4. PROBLEM VARIATIONS

Include additional processes such as dissolution of CO_2 in the aqueous phase and changes of capillary pressure function with changes in porosity. Consider a two-dimensional model geometry with a vertical fault in the caprock.

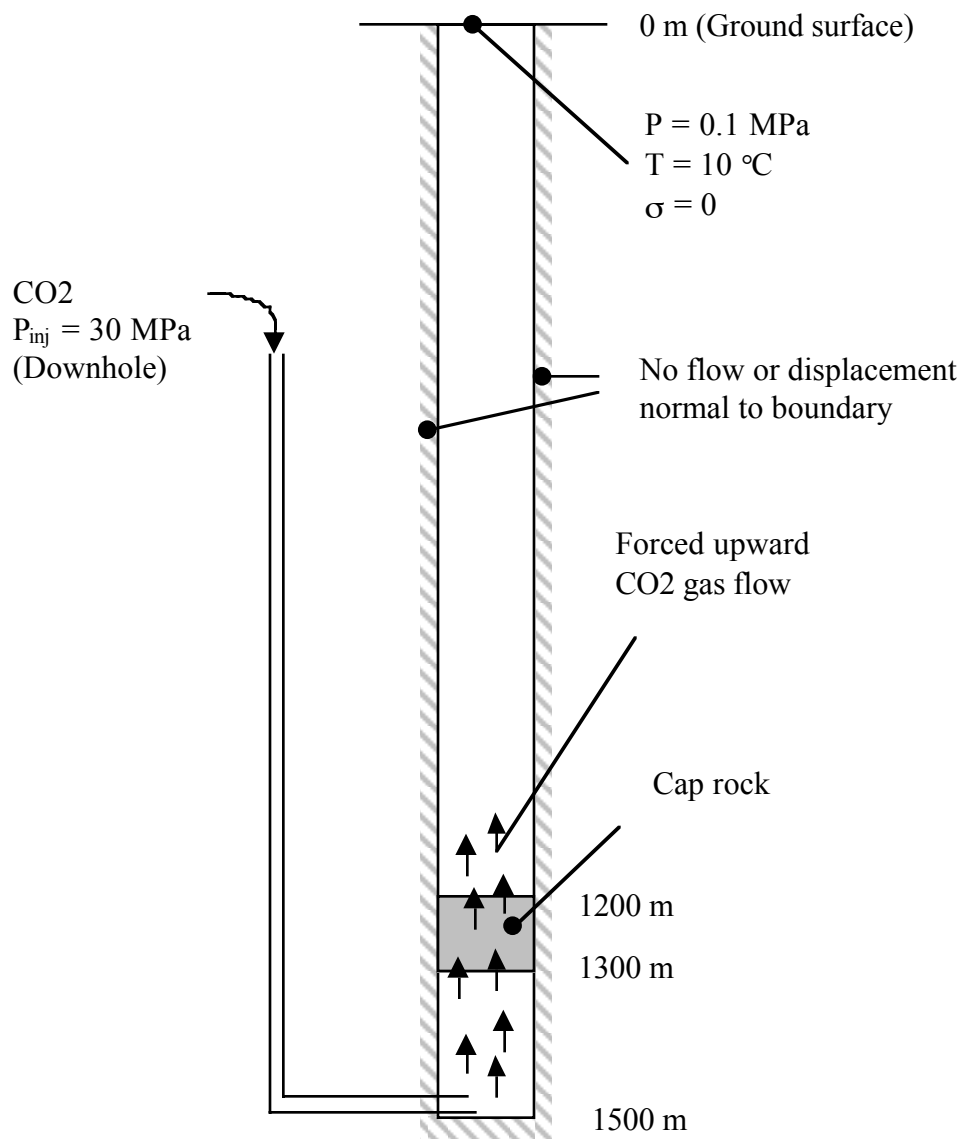


Figure F.1. Geometry of vertical column for hydromechanical test problem.

5. DEFINITION OF RESULTS TO BE CALCULATED

The simulation of the injection period (30 years) should be conducted with and without consideration of permeability and porosity changes.

For both simulations, provide vertical profiles at various times of:

- Gas saturation
- Total CO2 mass
- Fluid pressure

Table F.1. Rock properties.

Rock Property	Aquifer	Caprock
Young's modulus	$E = 1.0 \text{ GPa}$	$E = 1.0 \text{ GPa}$
Poisson's ratio	$\nu = 0.25$	$\nu = 0.25$
Saturated rock density	$\rho = 2260 \text{ kg/m}^3$	$\rho = 2260 \text{ kg/m}^3$
Porosity-stress function	$\phi = (\phi_0 - \phi_r) \exp(5 \cdot 10^{-8} \cdot \sigma'_M) + \phi_r$	$\phi = (\phi_0 - \phi_r) \exp(5 \cdot 10^{-8} \cdot \sigma'_M) + \phi_r$
Zero stress porosity	$\phi_0 = 0.1$	$\phi_0 = 0.01$
Residual porosity	$\phi_r = 0.09$	$\phi_r = 0.009$
Permeability-porosity function	$k = 2.284 \cdot 10^{-10} k_0 \exp(222 \cdot \phi)$	$k = 2.284 \cdot 10^{-10} k_0 \exp(2220 \cdot \phi)$
Zero stress permeability	$k_0 = 1.0\text{e-}13 \text{ m}^2$	$k_0 = 1.0\text{e-}16 \text{ m}^2$
Corey's (1954) relative permeability function	$k_{rl} = \hat{S}^4$ $k_{rg} = (1 - \hat{S})^2 (1 - \hat{S}^2)$ $\hat{S} = \frac{(S - S_{lr})}{(1 - S_{lr} - S_{gr})}$	$k_{rl} = \hat{S}^4$ $k_{rg} = (1 - \hat{S})^2 (1 - \hat{S}^2)$ $\hat{S} = \frac{(S - S_{lr})}{(1 - S_{lr} - S_{gr})}$
Irreducible gas saturation	$S_{gr} = 0.05$	$S_{gr} = 0.05$
Irreducible liq. saturation	$S_{lr} = 0.3$	$S_{lr} = 0.3$
van Genuchten's (1980) capillary pressure function	$P_{cap} = -P_0 ([S^*]^{-1/\lambda} - 1)^{1-\lambda}$ $S^* = (S_l - S_{lr}) / (1 - S_{lr})$	$P_{cap} = -P_0 ([S^*]^{-1/\lambda} - 1)^{1-\lambda}$ $S^* = (S_l - S_{lr}) / (1 - S_{lr})$
Irreducible liq. saturation	$S_{lr} = 0.0$	$S_{lr} = 0.0$
Exponent	$\lambda = 0.457$	$\lambda = 0.457$
Strength coefficient	$P_0 = 1.87 \text{ kPa}$	$P_0 = 59.1 \text{ kPa}$

- d) Mean stress
- e) Mean effective stress
- f) Permeability
- g) Porosity
- h) Vertical displacement

These should be provided for the following times:

- 1) Initial (just before injection)
- 2) 1 day

- 3) 1 year
- 4) 10 years
- 5) 30 years (end of injection period)
- 6) 100 years

The following transient monitoring data should be provided as a function of time:

- 1) The injection rate.
- 2) The rate of CO₂ flow (kg/sm²) at the top of caprock.

6. COMPARISON CRITERIA

Profiles at the same time should match within 5%.

7. REFERENCES

- Corey, A.T. The Interrelation Between Gas and Oil Relative Permeabilities, *Producers Monthly*, pp. 38 - 41, November 1954.
- van Genuchten, M.Th. A Closed-Form Equation for Predicting the Hydraulic Conductivity of Unsaturated Soils, *Soil Sci. Soc. Am. J.*, Vol. 44, pp. 892 - 898, 1980.

APPENDIX G. Test Problem 7: CO₂ Injection into a 2-D Layered Brine Formation[#]

1. INTRODUCTION AND GENERAL DESCRIPTION

This test problem is patterned after the CO₂ injection project at the Sleipner Vest field in the Norwegian sector of the North Sea, and is intended to investigate the dominant physical processes associated with the injection of supercritical CO₂ into a layered medium. Significant simplifications have been made, the most important of which is the assumption of isothermal conditions (37 °C, the ambient temperature of the formation). CO₂ injection rates (1,000,000 tonnes per year), system geometry, and system permeabilities correspond approximately to those at Sleipner, although no attempt was made to represent details of the permeability structure within the host formation. Injection of the supercritical CO₂, which is less dense than the saline formation waters into which it is injected, causes it to rise through the formation. Its rate of ascent, however, is limited by the presence of four relatively low permeability shales. The top and bottom of the formation is assumed to be impermeable. The only reactive chemistry considered in this problem is the dissolution of CO₂ in the aqueous phase.

2. LIST OF PROCESSES BEING STUDIED

- a) Gravity-driven advection in response to strong vertical and lateral density gradients induced by the injection of CO₂ into saline formation water.
- b) Density, viscosity, and solubility formulations of water and CO₂ as a function of pressure and temperature (P and T).

3. DEFINITION OF THE PROBLEM AND INPUT DATA

System Geometry:

The system is idealized as a two dimensional symmetric domain perpendicular to the horizontal injection well which has a screen length of 100 meters (Figure G.1). A one meter thick section perpendicular to the horizontal well is considered. The thickness of the formation at the injection site is 184 meters. The injection point is 940 meters below the sea floor, while the ocean depth at the site is 80 meters. The formation is assumed to consist of four lower permeability shale units 3 meters thick which are distributed within the high permeability sand. Each shale unit is separated by 30 meters. The well is 30 meters below the lowest shale unit, while the bottom of the aquifer is another 22 meters below the well.

[#] proposed by Carl Steefel; e-mail: steefel1@llnl.gov

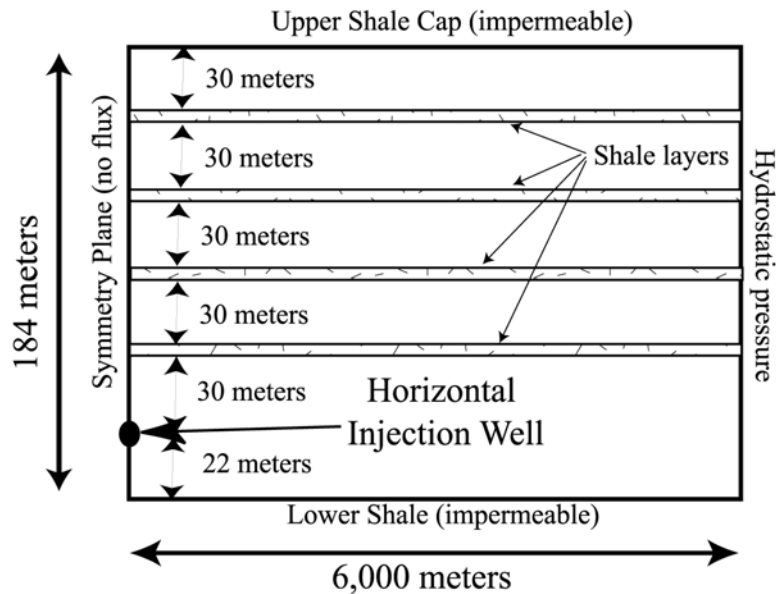


Figure G.1 Schematic representation of geometry for CO₂ injection in Utsira Formation.

Boundary conditions:

No heat or mass flux is allowed across any of the boundaries except the vertical boundary 6,000 meters from the injection well. This boundary is fixed at hydrostatic pressure, thus allowing flow into and out of the domain so as to avoid overpressuring the formation. The 6,000 meter boundary is chosen, however, to be far enough from the injection well that the CO₂ does not reach this boundary after 2 years of injection.

Initial conditions (Table G.1):

- $T = 37^{\circ}\text{C}$ (isothermal throughout)
- $P = \text{hydrostatic}$ (approximately 110 bars at injection point, approximately 90 bars at top of formation).
- CO₂ in the aqueous phase in equilibrium with a P_{CO_2} of 0.5 bars, a typical value for sedimentary formation waters at the temperature we are considering.

Table G.1 Initial conditions and injection specifications

Pressure at well	110 bar
Temperature	37 °C
Salinity	3.2 wt.-% NaCl
CO ₂ injection rate	0.1585 kg/s in half space

Injection specifications (Table G.1):

- a) Temperature = 37 °C
- b) Injection rate: 31.7 kg/s over entire screen length (100 meters), corresponding to 0.317 kg/s for the 1 meter thick section considered. Because of symmetry, injection rate in half space is therefore 0.1585 kg/s.
- c) Height of well cell: 1 meter.
- d) Injection time scale: 2 years

Input data (Table G.2):

- a) Capillary pressure and relative permeability described with van Genuchten parameters (both liquid and gas mobile). Porosity is 35% for sands, 10.25 % for shales.
- b) Fully saturated permeability ($k = 3 \times 10^{-12} \text{ m}^2$ in sand layers, 10^{-14} m^2 in shales)
- c) Density, viscosity, and solubility in water of CO₂ as functions of P and T (Span and Wagner, 1996).
- d) Vapor-liquid equilibrium properties of water.

4. PROBLEM VARIATIONS

Include non-isothermal effects by making the CO₂ injection temperature equal to 65 °C.

5. RESULTS TO BE CALCULATED

Liquid and gas saturations as a function of space and time. CO₂ concentration in the aqueous phase as a function of space. Gas and liquid fluxes.

6. COMPARISON CRITERIA

Results should match within +/- 5%.

Table G.2 Hydrogeologic parameters

Permeability Porosity Aquifer thickness	Sands: $3 \times 10^{-12} \text{ m}^2$; Shales: 10^{-14} m^2 Sands: $\phi = 0.35$; Shales: $\phi = 0.1025$ 184 m
Relative permeability	
liquid: van Genuchten function (1980) $k_{rl} = \sqrt{S^*} \left\{ 1 - \left(1 - [S^*]^{1/\lambda} \right)^\lambda \right\}^2$ irreducible water saturation exponent	$S^* = (S_l - S_{lr}) / (1 - S_{lr})$ $S_{lr} = 0.20$ $\lambda = 0.400$
gas: van Genuchten function (1980) $k_{rg} = \sqrt{S_g^*} \left\{ 1 - \left(1 - [S_g^*]^{1/\lambda} \right)^\lambda \right\}^2$ irreducible gas saturation exponent	$S_g^* = (S_g - S_{gr}) / (1 - S_{gr})$ $S_{gr} = 0.05$ $\lambda = 0.400$
Capillary pressure	
van Genuchten function (1980) $P_{cap} = -P_0 ([S^*]^{-1/\lambda} - 1)^{1-\lambda}$ irreducible water saturation exponent strength coefficient	$S^* = (S_l - S_{lr}) / (1 - S_{lr})$ $S_{lr} = 0.20$ $\lambda = 0.400$ Sand: $P_0 = 3.58 \text{ kPa}$; Shale: $P_0 = 62.0 \text{ kPa}$

7. REFERENCES

- van Genuchten, M.Th. A Closed-Form Equation for Predicting the Hydraulic Conductivity of Unsaturated Soils, *Soil Sci. Soc. Am. J.*, Vol. 44, pp. 892 - 898, 1980.
- Span, R. and W. Wagner. A New Equation of State for Carbon Dioxide Covering the Fluid Region from the Triple-Point Temperature to 100 K at Pressures up to 800 MPa, *J. Phys. Chem. Ref. Data*, Vol. 25, No. 6, pp. 1509 - 1596, 1996.

APPENDIX H. Test Problem 8: CO₂-Oil Displacement and Phase Behavior²

1. INTRODUCTION AND GENERAL DESCRIPTION

This problem probes our ability to predict accurately the interplay of CO₂-oil phase behavior and multiphase flow. CO₂ is injected into an oil-containing medium under two different conditions leading to miscible and immiscible displacement. This initial problem is posed in a one-dimensional geometry so that direct comparison can be made to available analytical solutions that have been derived for the CO₂-oil flow problem (Monroe *et al.* 1990, Orr *et al.* 1993). These solutions do not include the effects of capillary and hydrodynamic dispersion, but the effect of volume change on mixing will be computed.

2. LIST OF PROCESSES BEING STUDIED

Multiphase flow of CO₂ and oil subject to relative permeability and phase behavior effects.

Development of miscibility in CO₂-oil systems.

Numerical formulations for density, viscosity, and CO₂ solubility in oil.

Degree of numerical dispersion in numerical solutions.

3. DEFINITION OF THE PROBLEM AND INPUT DATA

- Oil composition: 10% CH₄, 20% C₄, and 70% C₁₀.
- Injected gas composition: 100% CO₂
- Injection P: case (a) P= 11.0 MPa and case (b) P= 12.0 MPa.
- Injection condition: constant volumetric rate
- Temperature: T = 71.1 °C and isothermal throughout.
- Geometry: one dimensional.
- Permeability and porosity: comparisons will be made in nondimensional form and so need not be specified.
- Relative permeability: $k_{rg} = \left(\frac{S_g}{1 - S_{or}} \right)^2$; $k_{ro} = \left(\frac{1 - S_g - S_{or}}{1 - S_{or}} \right)^2$ where $S_{or} = 0.2$
- Phase behavior: Reference results will be computed from the Peng-Robinson equation of state (Peng and Robinson, 1976) with the critical properties, volume corrections, and interaction coefficients tabulated by Orr *et al.* (1993). For comparison purposes, any phase behavior package can be employed.

² proposed by Tony Kavscek; email: kavscek@pangea.stanford.edu

4. PROBLEM VARIATIONS

Extend to more than 4 components to examine degree of chromatographic separation of various components. Include other combustion gases and N₂ in the injection gas. Examine the accuracy of prediction of the minimum miscibility pressure.

5. DEFINITION OF RESULTS TO BE CALCULATED

Saturation and composition profiles along the one-dimensional medium. For consistency the abscissa should be x_D/t_D where the dimensionless distance, x_D , is defined as x/L , the dimensionless time, t_D , is $q_{inj}t/fAL$, and A is the cross-sectional area of the medium.

6. COMPARISON CRITERIA

Profiles should reproduce the location of saturation and composition shocks within $\pm 5\%$.

7. REFERENCES

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